

# Package: asbio (via r-universe)

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**Author** Ken Aho

**Maintainer** Ken Aho <kenaho1@gmail.com>

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agrostis	<i>Agrostis variabilis</i> cover measurements
----------	---

---

**Description**

Percent cover of the grass *Agrostis variabilis* at 25 alpine snowbank sites in the Absaroka-Beartooth Mountains.

**Usage**

```
data(agrostis)
```

**Format**

A data frame with 25 observations on the following 2 variables.

**site** Site number

**cover** Percent cover

**Source**

Aho, K. (2006) *Alpine and Cliff Ecosystems in the North-Central Rocky Mountains*. PhD dissertation, Montana State University, Bozeman, MT.

---

aids

*Aids and veterans dataset*


---

**Description**

The veterans administration studied the effect of AZT on AIDS symptoms for 338 HIV-positive military veterans who were just beginning to express AIDS. AZT treatment was withheld on a random component until helper T cells showed even greater depletion while the other group received the drug immediately. The subjects were also classified by race.

**Usage**

```
data(aids)
```

**Format**

A data frame with 338 observations on the following 3 variables.

race A factor with levels black, white.

AZT A factor with levels N, Y.

symptoms Presence/absence of AIDS symptoms.

**Source**

Agresti, A. (2012) *Categorical Data Analysis, 3rd edition*. New York. Wiley.

---

alfalfa.split.plot

*An agricultural split plot design*


---

**Description**

An experiment was conducted in Iowa in 1944 to see how different varieties of alfalfa responded to the last cutting day of the previous year (Snedecor and Cochran 1967). We know that in the fall alfalfa can either continue to grow, or stop growing and store resources belowground in roots for growth during the following year. Thus, we might expect that later cutting dates inhibits growth for the following year. On the other hand, if plants are cut after they have gone into senescence, there should be little effect on productivity during the following year. There are two factors: 1) variety of alfalfa (three varieties were planted in each of three randomly chosen whole plots), and 2) the date of last cutting (Sept 1, Sept. 20, or Oct. 7). The dates were randomly chosen split plots within the whole plots. Replication was accomplished using six blocks of fields.

**Usage**

```
data(alfalfa.split.plot)
```

**Format**

The dataframe contains four variables:

yield Alfalfa yield (tons per acre).

variety Alfalfa variety. A factor with three levels "L"= Ladak, "C" = Cosack, and "R" = Ranger describing the variety of alfalfa seed used.

cut.time Time of last cutting. A factor with three levels: "None" = field not cut, "S1" = Sept 1, "S20" = Sept. 20, or "O7" = Oct. 7.

block The block (whole plot replicate). A factor with six levels: "1", "2", "3", "4", "5", and "6".

**Source**

Snedecor, G. W. and Cochran, G. C. (1967) *Statistical Methods, 6th edition*. Iowa State University Press.

---

alpha.div

*Functions for calculating alpha diversity.*

---

**Description**

Alpha diversity quantifies richness and evenness within a sampling unit (replicate).

The function `alpha.div` runs `Simp.index` or `SW.index` to calculate Simpson's, Inverse Simpson's or Shannon-Weiner diversities.

Simpson's index has a straightforward interpretation. It is the probability of reaching into a plot and simultaneously pulling out two different species. Inverse Simpson's diversity is equivalent to one over the probability that two randomly chosen individuals will be the same species. These measures have been attributed to Simpson (1949). While it does not allow straightforward interpretation of results, the Shannon-Weiner diversity ( $H'$ ) is another commonly used alpha-diversity measure based on the Kullback-Leibler information criterion (Macarthur and Macarthur 1961).

**Usage**

```
alpha.div(x, index)
Simp.index(x, inv)
SW.index(x)
```



**Arguments**

x	A vector or matrix of species abundances (e.g. counts). The functions assume that species are in columns and sites are in rows.
index	The type of alpha diversity to be computed. The function currently has three choices. <code>simp</code> = Simpson's diversity, <code>inv.simp</code> =inverse Simpson's, <code>shan</code> = Shannon-Weiner diversity.
inv	Logical, indicating whether or not Simpson's inverse diversity should be computed.

**Value**

A single diversity value is returned if x is a vector. A vector of diversities (one for each site) are returned if x is a matrix.

**Author(s)**

Ken Aho

**References**

- Simpson, E. H. (1949) Measurement of diversity. *Nature*. 163: 688.  
 MacArthur, R. H., and MacArthur J. W. (1961) On bird species diversity. *Ecology*. 42: 594-598.

**Examples**

```
data(cliff.sp)
alpha.div(cliff.sp,"simp")
```

---

anm.ci

*Animation demonstrations of confidence intervals.*

---

**Description**

Provides animated depictions of confidence intervals for  $\mu$ ,  $\sigma^2$ , the population median, and the binomial parameter  $\pi$ .

**Usage**

```
anm.ci(parent=expression(rnorm(n)), par.val, conf = 0.95, sigma = NULL,
  par.type = c("mu", "median", "sigma.sq", "p"), n.est = 100,
  n = 50, err.col = 2, par.col = 4, interval = 0.1, ...)

anm.ci.tck()
```

**Arguments**

parent	A parental distribution; ideally a distribution with known parameters.
par.val	True parameter value which is being estimated.
conf	Confidence level: $1-P(\text{type I error})$ .
sigma	$\sigma$ from the normal pdf, if known.
par.type	The parameter whose confidence intervals to be estimated. There are currently four choices <code>c("mu", "median", "sigma.sq", "p")</code> . These are the normal pdf parameters $\mu$ and $\sigma^2$ , the population median, and the binomial parameter, $\pi$ .
n.est	The number of confidence intervals to be created.
n	The sample size used for each confidence interval.
err.col	The line color of the intervals which do not include the true value.
par.col	The line color denoting the parameter value.
interval	The time interval for animation (in seconds). Smaller intervals speed up animation
...	Additional arguments to <code>plot</code> .

**Details**

Provides an animated plot showing confidence intervals with respect to a known parameter. Intervals which do not contain the parameter are emphasized with different colors. Loading package `tcltk` allows use of function `anm.ci.tck` which provides an interactive GUI to run the function.

**Value**

Returns an animated plot.

**Author(s)**

Ken Aho

**See Also**

Additional documentation for methods provided in: `ci.mu.t`, `ci.mu.z`, `ci.median`, `ci.sigma`, and `ci.p`.

**Examples**

```
## Not run:
parent<-rnorm(100000)
anm.ci(parent, par.val=0, conf =.95, sigma =1, par.type="mu")
anm.ci(parent, par.val=1, conf =.95, par.type="sigma.sq")
anm.ci(parent, par.val=0, conf =.95, par.type="median")
parent<-rbinom(100000,1,p=.65)
anm.ci(parent, par.val=0.65, conf =.95, par.type="p")
##Interactive GUI, requires package 'tcltk'
anm.ci.tck()

## End(Not run)
```

---

anm.coin	<i>Animated demonstration of frequentist binomial convergence of probability using a coin flip.</i>
----------	---

---

### Description

Creates an animated plot showing the results from coin flips, and the resulting convergence in  $P(\text{Head})$  as the number of flips grows large.

### Usage

```
anm.coin(flips = 1000, p.head = 0.5, interval = 0.01, show.coin = TRUE, ...)  
anm.coin.tck()
```

### Arguments

flips	The number of desired coin flips.
p.head	User defined probability of a head; e.g., for a fair coin $p.\text{head} = 0.5$ .
interval	The time between animation frames, in seconds.
show.coin	Logical if <code>show.coin=TRUE</code> shows a second plot with coin flip results (head or tail).
...	Additional arguments to <code>plot</code> .

### Value

If `show.coin=TRUE`, returns two plots configured as a single graphical object. The first plot shows convergence in estimated  $P(\text{Head})$ , i.e., number of heads/number of trials, as the number of trials grows large. The second plot shows individual outcomes of coin flips. The second (smaller) plot is not returned if `show.coin=TRUE` is specified. Loading **teRtk** allows use of the function `anm.coin.tck`, which creates an interactive GUI to run `anm.coin`.

### Author(s)

Ken Aho

### See Also

[rbinom](#)

### Examples

```
## Not run: anm.coin()
```

anm.cont.pdf

*Animated demonstration of density for a continuous pdf*

---

**Description**

A continuous pdf is conceptually a histogram whose bin area sums to one. Infinite, infinitely small bins, however, are required to allow depiction of an infinite number of distinct continuous outcomes.

**Usage**

```
anm.cont.pdf(part = "norm", interval = 0.3)
```

```
see.pdf.conc.tck()
```

**Arguments**

part	Parent distribution, options are "norm" = $N(0, 1)$ , "t" = $t(10)$ , "exp" = $EXP(1)$ , and "unif" = $UNIF(0,1)$
interval	Animation interval

**Note**

May not work every time because random values may exceed histogram range.

**Author(s)**

Ken Aho

---

anm.die*Animated depiction of six-sided die throws.*

---

**Description**

Convergence in probability for fair (or loaded) six-sided die.

**Usage**

```
anm.die(reps = 300, interval = 0.1, show.die = TRUE, p = c(1/6, 1/6, 1/6,  
1/6, 1/6, 1/6), cl = TRUE)
```

```
anm.die.tck()
```

**Arguments**

reps	Number of die throws.
interval	Animation interval in frames per second.
show.die	Logical, indicating whether die outcomes should be shown.
p	A vector of length six which sums to one indicating the probability of die outcomes.
cl	Logical, Indicating whether or not color should be used.

**Author(s)**

Ken Aho

**See Also**

[anm.coin](#)

**Examples**

```
## Not run:  
anm.die()  
  
## End(Not run)
```

---

anm.ExpDesign

*Animated depiction of experimental designs*

---

**Description**

Describes random treatment allocation for fifteen experimental designs.

**Usage**

```
anm.ExpDesign(method="all", titles = TRUE, cex.text = 1, mp.col = NULL, lwda = 1,  
n = 10, EUcol = hcl.colors(n, palette = "Dark 3"), interval = 0.5, iter = 30)
```

```
ExpDesign(method="all", titles = TRUE, cex.text = 1, mp.col = NULL, lwda = 1, n = 10,  
EUcol = hcl.colors(n, palette = "Dark 3"),...)
```

```
anm.ExpDesign.tck()
```

**Arguments**

method	A character vector listing the experimental methods to be demonstrated (see <b>Details</b> below).
titles	A logical argument specifying whether or not plots should have main titles.
interval	Time length spent on each frame in animation (in seconds).
iter	Number of random iterations in animation.
cex.text	Text character expansion plots.
mp.col	Arrow colors in "matched" plot. Either a vector of length 3 or a single color.
lwda	Arrow line widths.
n	Sample size (number of experimental units). Currently only implemented for method = "CRD"
EUcol	Color of text identifying experimental units (or in some designs, treatments). Currently only implemented for method = "CRD", method = "factorial2by2", method = "RCBD", and method = "nested"
...	Additional arguments from <a href="#">plot</a> .

**Details**

The function returns a plot or series of plots illustrating the workings of experimental designs. Random apportionment of treatments of experimental units (EUs) is illustrated for each of twelve experimental designs. A character string can be specified in the method argument using a subset of any of the following:

"CRD": a one-way completely randomized design,

"factorial2by2": a 2 x 2 design with four EUs,

"factorial2by2by2": a 2 x 2 x 2 factorial designs with 8 EUs,

"nested": a nested design with two levels of nesting,

"RCBD" a randomized complete block design with two blocks, two treatments and four EUs,

"RIBD": a randomized incomplete block design with three blocks, three treatments, and six EUs,

"split": a split plot design with a whole plot (factor A) and a split plot (factor B),

"split.split": a split split-split plot design,

"SPRB": split plots in randomized blocks,

"strip.split": strip-split plot design,

"latin": a Latin squares design with  $r = 3$ , and

"pairs": a matched pairs design.

The function `anm.ExpDesign.tck` provides an interactive GUI. Details on these designs are given below.

**Completely randomized design (CRD)**

In a **completely randomized design** experimental units are each randomly assigned to factor levels without constraints like blocking. This approach can (and should) be implemented in one way ANOVAs, and in more complex formats like factorial and hierarchical designs.

### Factorial design

Treatments can be derived by combining factor levels from the multiple factors. This is called a **factorial design**. In a fully crossed factorial design with two factors, A and B, every level in factor A is contained in every level of factor B.

### Randomized block design (RBD)

In a **randomized block design** a researcher randomly assigns experimental units to treatments separately within units called blocks. If all treatments are assigned exactly once within each block this is known as a **randomized complete block design (RCBD)**

### Latin squares

**Latin squares designs** are useful when there are two potential blocking variables. These can figuratively or literally be represented by rows and columns. All treatments are assigned to each row and to each column, and for each row and column treatment assignments differ. Of course this stipulation limits the number of ways one can allocate treatments.

### Nested design

In a **nested design** factor levels from one factor will be contained entirely in one factor level from another factor. Consider a design with two factors A and B. When every level of factor A appears with every level of factor B, and vice versa, then we have a fully crossed factorial design (see above). Conversely, when levels of B only occur within a single level of A, then B is nested in A.

### Split plot design

A **split plot** design contains two nested levels of randomization. At the highest level are whole plots which are randomly assigned factor levels from one factor. At a second nested level whole plots are split to form split plots. The split plots are randomly assigned factor levels from a second factor. Split plot designs are replicated in units called blocks. **Split-split plot** design will have two levels of split plot nesting: C (split-split plots) are split plots within B (split plots), and B are split plots within A (whole plots). We can see obvious and confusing similarities here to nested designs. A **split plot randomized block (SPRB)** design will have whole plots randomly assigned within blocks, and split plots randomly assigned within the whole plots. Thus, levels of A (whole plot) are assigned randomly to a block, and split plots containing levels of B (split plot) are assigned within a level of A.

### Strip plot design

Closely related to split plot designs are strip plots. **Strip plots** can be used address situations when relatively large experimental units are required for each of two factors in an experiment. A strip plot will have a row and column structure. Let the number of columns equal to the number of levels in factor A, and let the number of rows be equal to the number of levels in factor B. Levels in A are randomly assigned to columns only (across all rows) in a RBD format, and levels in B are assigned to rows only (across all columns). Interestingly, the levels in A serve as split plots in B and vice versa. However, unlike a split plot design assignment of treatments at this level is not entirely random since rows are assigned single levels in A, while columns are assigned single levels in B. Compared to a factorial design strip plots allow for greater precision in the measurement

of interaction effects while sacrificing precision in the measurement of main effects. Split-block design discussed by Littell et al. (2006), are indistinguishable from strip plots, described earlier, except that they are placed in the context of blocks. They are also indistinguishable from SPRBs except that the design has an explicit row/column structure (one level of A for each column, one level of B for each row), resulting in larger experimental units for A and B. Conversely, in a SPRB, different levels of A and B can be assigned within columns and rows respectively. A final type of split/strip plot design is known as a **strip-split plot**. Strip-split plots are three way designs (cf. Hoshmand 2006, Milliken and Johnson 2009). In these models a conventional two factor strip plot is created (factors A and B) and split plots are placed in the resulting cells (levels in factor C). The design is indistinguishable from a split-split plot design except for the fact that "columns" always constitute the same levels in A, while "rows" always constitute the same levels in B, allowing larger experimental units for A and B, and reflecting the strip plot relationship of A and B. Other, even more complex variants of split and strip plots are possible. For instance, Littell et al. (2006) discuss a case study they describe as strip-split-split plot design!

### Matched pairs

In a **matched pairs** design treatments are compared by using the same (or highly similar) experimental units. If treatments are assigned at particular time segments it is assumed that outcomes within an experimental unit are independent, i.e., there is no "carryover" effect from the previous treatment. Violation of this assumption may result in ashpericity and prevent conventional approaches.

### Author(s)

Ken Aho

### References

- Hoshmand, A. R. (2006) *Design of Experiments for Agriculture and the Natural Sciences 2nd Edition*. CRC Press.
- Littell, R. C., Stroup, W. W., and R. J. Fruend (2002) *SAS for linear models*. Wiley, New York.
- Milliken, G. A., and D. E. Johnson (2009) *Analysis of messy data: Vol. I. Designed experiments, 2nd edition*. CRC.

### See Also

[samp.design](#)

### Examples

```
ExpDesign()  
## Not run: anm.ExpDesign()
```



---

anm.geo.growth      *Animated depictions of population growth*

---

## Description

Animated depictions of geometric, exponential, and logistic growth.

## Usage

```
anm.geo.growth(n0, lambda, time = seq(0, 20), ylab = "Abundance",
xlab = "Time", interval = 0.1, ...)
```

```
anm.exp.growth(n, rmax, time = seq(0, 20), ylab = "Abundance",
xlab = "Time", interval = 0.1, ...)
```

```
anm.log.growth(n, rmax, K, time = seq(0, 60), ylab = "Abundance",
xlab = "Time", interval = 0.1, ...)
```

```
anm.geo.growth.tck()
```

```
anm.exp.growth.tck()
```

```
anm.log.growth.tck()
```

## Arguments

n0	Population size at time zero for geometric population growth.
lambda	Geometric growth rate.
time	A time sequence, i.e. a vector of integers which must include 0.
ylab	Y-axis label.
xlab	X-axis label
interval	Animation interval in seconds per frame.
...	Additional arguments to <a href="#">plot</a>
n	Initial population numbers for exponential and logistic growth
rmax	The maximum intrinsic rate of increase
K	The carrying capacity

## Details

Presented here are three famous population growth models from ecology. Geometric, exponential and logistic growth. The first two model growth in the presence of unlimited resources. Geometric growth is exponential growth assuming non-overlapping generations, and is computed as:

$$N_t = N_0 \lambda^t,$$

where  $N_t$  is the number of individuals at time  $t$ ,  $\lambda$  is the geometric growth rate, and  $t$  is time.

Exponential growth allows simultaneous existence of multiple generations, and is computed as:

$$\frac{dN}{dt} = r_{max}N,$$

where  $r_{max}$  is the maximum intrinsic rate of increase, i.e. max(birth rate - death rate), and  $N$  is the population size. With logistic growth, exponential growth is slowed as  $N$  approaches the carrying capacity. It is computed as:

$$\frac{dN}{dt} = r_{max}N \frac{K - N}{K},$$

where  $r_{max}$  is the maximum rate of intrinsic increase,  $N$  is the population size, and  $K$  is the carrying capacity

Package **tcltk** allows implementation of all three models using GUIs.

### Author(s)

Ken Aho

### See Also

[anm.LVexp](#), [anm.LVcomp](#)

### Examples

```
## Not run:
anm.geo.growth(10,2.4)

## End(Not run)
```

---

anm.loglik

*Animated plots of log-likelihood functions*

---

### Description

Plots the normal, exponential, Poisson, binomial, and "custom" log-likelihood functions. By definition, likelihoods for parameter estimates are calculated by holding data constant and varying estimates. For the normal distribution a fixed value for the parameter which is not being estimated ( $\mu$  or  $\sigma^2$ ) is established using MLEs.

**Usage**

```
anm.loglik(X, dist = c("norm", "poi", "bin", "exp", "custom"),
plot.likfunc = TRUE, parameter = NULL, func = NULL, poss = NULL,
plot.density = TRUE, plot.calc = FALSE, xlab = NULL, ylab = NULL,
conv = diff(range(X))/70, anim = TRUE, est.col = 2, density.leg = TRUE,
cex.leg = 0.9, interval = 0.01, ...)
```

```
loglik.norm.plot(X, parameter = c("mu", "sigma.sq"), poss = NULL,
plot.likfunc = TRUE, plot.density = TRUE, plot.calc = FALSE,
xlab = NULL, ylab = NULL, conv = 0.01, anim = TRUE, est.col = 2,
density.leg = TRUE, cex.leg = 0.9, interval = 0.01, ...)
```

```
loglik.pois.plot(X, poss = NULL, plot.likfunc = TRUE,
plot.density = TRUE, plot.calc = FALSE, xlab = NULL, ylab = NULL,
conv = 0.01, anim = TRUE, interval = 0.01, ...)
```

```
loglik.binom.plot(X, poss = NULL, xlab = NULL, ylab = NULL,
plot.likfunc = TRUE, plot.density = TRUE, conv = 0.01, anim = TRUE,
interval = 0.01, ...)
```

```
loglik.exp.plot(X, poss = NULL, plot.likfunc = TRUE,
plot.density = TRUE, plot.calc = FALSE, xlab = NULL, ylab = NULL,
conv = 0.01, anim = TRUE, est.col = 2, density.leg = TRUE,
cex.leg = 0.9, interval = 0.01, ...)
```

```
loglik.custom.plot(X, func, poss, anim = TRUE, interval = 0.01,
xlab, ylab, ...)
```

```
anm.loglik.tck()
```

**Arguments**

X	A vector of quantitative data. The function does not currently handle extremely large datasets, $n > 500$ . Data should be integers (counts) for the Poisson log-likelihood function, and binary responses (0,1) for the binomial log likelihood function. Data elements for the exponential log likelihood function must be greater than zero.
parameter	The parameter for which ML estimation is desired in <code>loglik.norm.plot</code> . Specification of either "mu" or "sigma.sq" is required for the normal log-likelihood function. No specification is required for exponential, Poisson, and binomial log-likelihood functions since these distributions are generally specified with a single parameter, i.e., $\theta$ for the exponential, $\lambda$ for the Poisson distribution, and $p$ (the probability of a success) for the binomial distribution.
poss	An optional vector containing a sequence of possible parameter estimates. Elements in the vector must be distinct. If <code>poss</code> is not specified a vector of appropriate possibilities is provided by the function. This argument can be used to set <code>xlim</code> in the likelihood function and density plots.

<code>dist</code>	The type of assumed distribution there are currently five possibilities: "norm", "poi", "binom", "exp", and "custom". Use of custom distributions requires specification of a custom likelihood function in the argument <code>func</code> .
<code>plot.likfunc</code>	A logical command for indicating whether a graph of the log-likelihood function should be created.
<code>plot.density</code>	A logical command for indicating whether a second graph, in which densities are plotted on the pdf, should be created.
<code>plot.calc</code>	A logical command for indicating whether a third graph, in which log-densities are added to one another, should be created.
<code>xlab</code>	Optional X-axis label.
<code>ylab</code>	Optional Y-axis label.
<code>conv</code>	Precision of likelihood function. Decreasing <code>conv</code> increases the smoothness and precision of the ML function. Decreasing <code>conv</code> will also slow the animation.
<code>anim</code>	A logical command indicating whether animation should be used in plots.
<code>est.col</code>	Color used in depicting estimation.
<code>density.leg</code>	Logical. Should the legend for density be shown?
<code>cex.leg</code>	Character expansion for legend.
<code>interval</code>	Speed of animation, in seconds per frame. May not work in all systems; see <a href="#">Sys.sleep</a> .
<code>func</code>	Custom likelihood function to be specified when using <code>loglik.custom.plot</code> . The function should have two arguments. An optional call to data, and the likelihood function parameter (see example below).
<code>...</code>	Additional arguments from <code>plot</code> can be specified for likelihood function plots.

## Details

These plots are helpful in explaining the workings of ML estimation for parameters. Animation is included as an option to further clarify processes. When specifying `poss` be sure to include the estimate that you "want" the log-likelihood function to maximize in the vector of possibilities, e.g. `mean(X)` for estimation of  $\mu$ .

## Value

Three animated plots can be created simultaneously. The first plot shows the normal, Poisson, exponential, binomial, or custom log-likelihood functions. The second plot shows the pdf with ML estimates for parameters. On this graph densities of observations are plotted as pdf parameters are varied. By default these two graphs will be created simultaneously on a single graphics device. By specifying `plot.calc = TRUE` a third plot can also be created which shows that log-likelihood is the sum of the log-densities. Animation in this third plot will be automatically sped up, using a primitive routine, for large datasets, and slowed for small datasets. The third plot will not be created for the binomial pdf because there will only be a single outcome from the perspective of likelihood (e.g. 10 successes out of 22 trials). The second and third plots will not be created for custom likelihood functions. Loading package **tktk** allows use of the function `anm.loglik.tck` which provides an interactive GUI to run `anm.loglik`.

**Author(s)**

Ken Aho

**See Also**[dnorm](#), [dpois](#), [dexp](#), [dbinom](#)**Examples**

```
## Not run:
##Normal log likelihood estimation of mu.
X<-c(11.2,10.8,9.0,12.4,12.1,10.3,10.4,10.6,9.3,11.8)
anm.loglik(X,dist="norm",parameter="mu")

##Add a plot describing log-likelihood calculation.
anm.loglik(X,dist="norm",parameter="mu",plot.calc=TRUE)

##Normal log likelihood estimation of sigma squared.
X<-c(11.2,10.8,9.0,12.4,12.1,10.3,10.4,10.6,9.3,11.8)
anm.loglik(X,dist="norm",parameter="sigma.sq")

##Exponential log likelihood estimation of theta
X<-c(0.82,0.32,0.14,0.41,0.09,0.32,0.74,4.17,0.36,1.80,0.74,0.07,0.45,2.33,0.21,
0.79,0.29,0.75,3.45)
anm.loglik(X,dist="exp")

##Poisson log likelihood estimation of lambda.
X<-c(1,3,4,0,2,3,4,3,5)
anm.loglik(X,dist="poi")

##Binomial log likelihood estimation of p.
X<-c(1,1,0,0,0,1,0,0,0,0)#where 1 = a success
anm.loglik(X,dist="bin",interval=.2)

##Custom log-likelihood function
func<-function(X=NULL,theta)theta^5*(1-theta)^10
anm.loglik(X=NULL,func=func,dist="custom",poss=seq(0,1,0.01),
xlab="Possibilities",ylab="Log-likelihood")

##Interactive GUI, requires package 'tcltk'
anm.loglik.tck()

## End(Not run)
```

anm.ls

*Animated plot of least squares function.***Description**

Depicts the process of least squares estimation by plotting the least squares function with respect to a vector of estimate possibilities.

**Usage**

```
anm.ls(X, poss=NULL, parameter = "mu", est.lty = 2, est.col = 2,
conv=diff(range(X))/50, anim=TRUE, plot.lsfunc = TRUE, plot.res = TRUE,
interval=0.01, xlab=expression(paste("Estimates for ", italic(E),
"(",italic(X),")", sep = "")),...)
```

```
anm.ls.tck()
```

**Arguments**

X	A numeric vector containing sample data.
poss	An ordered numeric sequence of possible parameter estimates. Inclusion of the least squares estimate in the vector (e.g. $\bar{X}$ for $\mu$ will cause the least squares function be minimized at this value.
parameter	Parameter to be estimated. Only estimation for $E(X)$ is currently implemented. Note that if $X \sim N(\mu, \sigma^2)$ then $E(X) = \mu$ .
est.lty	Line type to be used to indicate the least squares estimate.
est.col	Line color to be used to indicate the least squares estimate.
conv	Precision of LS function. Decreasing conv increases the smoothness and precision of the function.
anim	A logical command indicating whether animation should be used in plots.
plot.lsfunc	A logical command indicating whether the least-squares function should be plotted.
plot.res	A logical command indicating whether a plot of residuals should be created.
interval	Speed of animation (in frames per second). A smaller interval decreases speed. May not work in all systems; see <a href="#">Sys.sleep</a> .
xlab	X-axis label.
...	Additional arguments to <a href="#">plot</a>

**Value**

A plot of the least squares function is returned along with the least squares estimate for  $E(X)$  given a set of possibilities. The function `anm.ls.tck` provides a GUI to run the function.

**Author(s)**

Ken Aho

**See Also**

[loglik.plot](#)

**Examples**

```
## Not run: X<-c(11.2,10.8,9.0,12.4,12.1,10.3,10.4,10.6,9.3,11.8)
anm.ls(X)
## End(Not run)
```

---

anm.ls.reg                      *Animated plot of the least squares function.*

---

### Description

Depicts the process of least squares estimation of simple linear regression parameters by plotting the least squares function with respect to estimate possibilities for the intercept or slope.

### Usage

```
anm.ls.reg(X, Y, parameter="slope", nmax=50, interval = 0.1, col = "red",...)
anm.ls.reg.tck()
```

### Arguments

X	A numeric vector containing explanatory data.
Y	A numeric vector containing response data.
parameter	Parameter to be estimated. Either "slope" or "intercept".
nmax	The number of parameter estimates to be depicted. The true LS estimate will always be in the center of this sequence.
interval	Speed of animation (in frames per second). A smaller interval decreases speed. May not work in all systems; see <a href="#">Sys.sleep</a> .
col	Line color.
...	Additional arguments to <a href="#">plot</a>

### Value

An animated plot of the plot possible regression lines is created along with an animated plot of the residual sum of squares. The function `anm.ls.reg.tck` provides a GUI to run the function.

### Author(s)

Ken Aho

### See Also

[loglik.plot](#), [anm.ls](#)

### Examples

```
## Not run:
X<-c(11.2,10.8,9.0,12.4,12.1,10.3,10.4,10.6,9.3,11.8)
Y<-log(X)
anm.ls.reg(X, Y, parameter = "slope")
## End(Not run)
```

---

anm.LV                      *Animated depictions of Lotka-Volterra competition and exploitation models*

---

### Description

Creates animated plots of two famous abundance models from ecology; the Lotka-Volterra competition and exploitation models

### Usage

```
anm.LVcomp(n1, n2, r1, r2, K1, K2, a2.1, a1.2, time = seq(0, 200), ylab =
"Abundance", xlab = "Time", interval = 0.1, ...)
```

```
anm.LVexp(nh, np, rh, con, p, d.p, time = seq(0, 200), ylab = "Abundance",
xlab = "Time", interval = 0.1, circle = FALSE, ...)
```

```
anm.LVc.tck()
```

```
anm.LVe.tck()
```

### Arguments

n1	Initial abundance values for species one. To be used in the competition function <code>anm.LVcomp</code> , i.e., $N_1$ in the competition equations below.
n2	Initial abundance values for species two in the competition function, i.e., $N_2$ in the competition equations below.
r1	Maximum intrinsic rate of increase for species one, i.e., $r_{max1}$ .
r2	Maximum intrinsic rate of increase for species two in the competition model <code>anm.LVcomp</code> , i.e., $r_{max2}$ .
K1	Carrying capacity for species one, i.e., $K_1$ .
K2	Carrying capacity for species two, i.e., $K_2$ .
a2.1	The interspecific effect of species one on species two, i.e., the term $\alpha_{21}$ .
a1.2	The interspecific effect of species two on species one, i.e., the term $\alpha_{12}$ .
nh	Initial abundance values for the host (prey) species. To be used in the the exploitation model <code>anm.LVexp</code> , i.e., the term $N_h$ at $t = 1$ .
np	Initial abundance values for the predator species in the the exploitation model, i.e., the term $N_p$ at $t = 1$ .
rh	The intrinsic rate of increase for the host (prey) species, i.e., the term $r_h$ .
con	The conversion rate of prey to predator, i.e., the term $c$ .
p	The predation rate, i.e., the term $p$ .
d.p	The death rate of predators, i.e., the term $d_p$ .
time	A time sequence for which competition or exploitation is to be evaluated.



ylab	Y-axis label.
xlab	X-axis label.
interval	Animation speed per frame (in seconds).
circle	Logical, if TRUE a circular representation of the relation of prey and predator numbers is drawn.
...	Additional arguments from <a href="#">plot</a> .

### Details

The Lotka-Volterra competition and exploitation models require simultaneous solutions for two differential equations. These are solved using the function `rk4` from `odesolve`.

The interspecific competition model is based on:

$$\frac{dN_1}{dt} = r_{max1}N_1 \frac{K_1 - N_1 - \alpha_{12}}{K_1},$$

$$\frac{dN_2}{dt} = r_{max2}N_2 \frac{K_2 - N_2 - \alpha_{21}}{K_2},$$

where  $N_1$  is the number of individuals from species one,  $K_1$  is the carrying capacity for species one,  $r_{max1}$  is the maximum intrinsic rate of increase of species one, and  $\alpha_{12}$  is the interspecific competitive effect of species two on species one.

The exploitation model is based on:

$$\frac{dN_h}{dt} = r_h N_h - p N_h N_p,$$

$$\frac{dN_p}{dt} = cp N_h N_p - d_p N_p,$$

where  $N_h$  is the number of individuals from the host (prey) species,  $N_p$  is the number of individuals from the predator species,  $r_h$  is the intrinsic rate of increase for the host (prey) species,  $p$  is the rate of predation,  $c$  is a conversion factor which describes the rate at which prey are converted to new predators, and  $d_p$  is the death rate of the predators.

The term  $r_h N_h$  describes exponential growth for the host (prey) species. This will be opposed by deaths due to predation, i.e. the term  $p N_h N_p$ . The term  $cp N_h N_p$  is the rate at which predators destroy prey. This in turn will be opposed by  $d_p N_p$ , i.e. predator deaths. Loading package `tcltk` allows one to run the GUIs in `anm.LVc.tck` and `anm.LV.tck`.

### Value

The functions return descriptive animated plots

### Author(s)

Ken Aho, based on a concept elucidated by M. Crawley

## References

- Molles, M. C. (2010) *Ecology, Concepts and Applications, 5th edition*. McGraw Hill.  
 Crawley, M. J. (2007) *The R Book*. Wiley

## Examples

```
## Not run:

#----- Competition -----#
##Species 2 drives species 1 to extinction
anm.LVcomp(n1=150,n2=50,r1=.7,r2=.8,K1=200,K2=1000,a2.1=.5,a1.2=.7,time=seq(0,200))
##Species coexist with numbers below carrying capacities
anm.LVcomp(n1=150,n2=50,r1=.7,r2=.8,K1=750,K2=1000,a2.1=.5,a1.2=.7,time=seq(0,200))

#-----Exploitation-----#
#Fast cycles
anm.LVexp(nh=300,np=50,rh=.7,con=.4,p=.006,d.p=.2,time=seq(0,200))
## End(Not run)
```

---

anm.mc.bvn

*Animation of Markov Chain Monte Carlo walks in bivariate normal space*

---

## Description

The algorithm can use three different variants on MCMC random walks: Gibbs sampling, the Metropolis algorithm, and the Metropolis-Hastings algorithms to move through univariate `anm.mc.norm` and bivariate normal probability space. The jumping distribution is also bivariate normal with a mean vector at the current bivariate coordinates. The jumping kernel modifies the jumping distribution through multiplying the variance covariance of this distribution by the specified constant.

## Usage

```
anm.mc.bvn(start = c(-4, -4), mu = c(0, 0), sigma = matrix(2, 2, data = c(1, 0,
0, 1)), length = 1000, sim = "M", jump.kernel = 0.2, xlim = c(-4, 4),
ylim = c(-4, 4), interval = 0.01, show.leg = TRUE, cex.leg = 1, ...)
```

```
anm.mc.norm(start = -4, mu = 0, sigma = 1, length = 2000, sim = "M",
jump.kernel = 0.2, xlim = c(-4, 4), ylim = c(0, 0.4), interval = 0.01,
show.leg = TRUE, ...)
```

```
anm.mc.bvn.tck()
```

## Arguments

- `start` A two element vector specifying the bivariate starting coordinates.  
`mu` A two element vector specifying the mean vector for the proposal distribution.

sigma	A 2 x 2 matrix specifying the variance covariance matrix for the proposal distribution.
length	The length of the MCMC chain.
sim	Simulation method used. Must be one of "G" indicating Gibbs sampling, "M" indicating the Metropolis algorithm, or "MH" indicating the Metropolis-Hastings algorithm (Gibbs sampling is not implemented for anm.mc.norm).
jump.kernel	A number > 0 that will serve as a (squared) multiplier for the proposal variance covariance. The result of this multiplication will be used as the variance covariance matrix for the jumping distribution.
xlim	A two element vector describing the upper and lower limits of the x-axis.
ylim	A two element vector describing the upper and lower limits of the y-axis.
interval	Animation interval
show.leg	Logical. Indicating whether or not the chain length should be shown.
cex.leg	Character expansion for legend.
...	Additional arguments from <code>plot</code> .

**Value**

The function returns two plots. These are: 1) the proposal bivariate normal distribution in which darker shading indicates higher density, and 2) an animated plot showing the MCMC algorithm walking through the probability space.

**Author(s)**

Ken Aho

**References**

Gelman, A., Carlin, J. B., Stern, H. S., and D. B. Rubin (2003) *Bayesian Data Analysis, 2nd edition*. Chapman and Hall/CRC.

---

anm.samp.design

*Animated demonstration of randomized sampling designs*

---

**Description**

Animated Comparisons of outcomes from simple random sampling, stratified random sampling and cluster sampling.

**Usage**

```
anm.samp.design(n=20, interval = 0.5 ,iter = 30, main = "", lwd = 2, lcol = 2)
```

```
samp.design(n = 20, main = "", lwd = 2, lcol = 2)
```

```
anm.samp.design.tck()
```

**Arguments**

<code>n</code>	The number of samples to be randomly selected from a population of 400.
<code>interval</code>	Time length spent on each frame in animation (in seconds).
<code>iter</code>	Number of random iterations in animation.
<code>main</code>	Main heading.
<code>lwd</code>	Line width to distinguish strata in stratified and cluster designs.
<code>lcol</code>	Line width to distinguish strata in stratified and cluster designs.

**Details**

Returns a plot comparing outcomes of random sampling, stratified random sampling and cluster sampling from a population of size 400. For stratified random sampling the population is subdivided into four equally strata of size 100. and  $n/4$  samples are taken within each strata. For cluster sampling the population is subdivided into four equally sized clusters and a census is taken from two clusters (regardless of specification of  $n$ ). The function `anm.samp.design` depicts random sampling using animation

**Value**

A plot is returned with four subplots. (a) shows the population before sampling, (b) shows simple random sampling, (c) shows stratified random sampling, (d) shows cluster sampling. The function `anm.samp.design.tck` provides interaction with a **tcltk** GUI.

**Author(s)**

Ken Aho

**Examples**

```
samp.design(20)

#Animated demonstration
## Not run: anm.samp.design(20)
```

---

anolis

*Anolis lizard contingency table data*

---

**Description**

Schoener (1968) examined the resource partitioning of anolis lizards on the Caribbean island of South Bimini. He cross-classified lizard counts in habitats (branches in trees) with respect to three variables: lizard species *A. sargei* and *A. distichus*, branch height (high and low), and branch size (small and large).

**Usage**

```
data(anolis)
```

**Format**

A data frame with 8 observations on the following 4 variables.

height Brach height. A factor with levels H, L.

size Brach size. A factor with levels L, S.

species Anolis species. A factor with levels distichus, sagrei.

count Count at the cross classification.

**Source**

Schoener, T. W. (1968) The Anolis lizards of Bimini: resource partitioning in a complex fauna. *Ecology* 49(4): 704-726.

---

anscombe

*Anscombe's quartet*

---

**Description**

A set of four bivariate datasets with the same conditional means, conditional variances, linear regressions, and correlations, but with dramatically different forms of association.

**Usage**

```
data(anscombe)
```

**Format**

A data frame with 11 observations on the following 8 variables.

x1 The first conditional variable in the first bivariate dataset.

y1 The second conditional variable in the first bivariate dataset.

x2 The first conditional variable in the second bivariate dataset.

y2 The second conditional variable in the second bivariate dataset.

x3 The first conditional variable in the third bivariate dataset.

y3 The second conditional variable in the third bivariate dataset.

x4 The first conditional variable in the fourth bivariate dataset.

y4 The second conditional variable in the fourth bivariate dataset.

**Details**

Anscombe (1973) used these datasets to demonstrate that summary statistics are inadequate for describing association.

**Source**

Anscombe, F. J. (1973) Graphs in statistical analysis. *American Statistician* 27 (1): 17-21.

## References

Anscombe, F. J. (1973) Graphs in statistical analysis. *American Statistician* 27 (1): 17-21.

## Examples

```
# dev.new(height=3.5)
op <- par(mfrow=c(1,4),mar=c(0,0,2,3), oma = c(5, 4.2, 0, 0))
with(anscombe, plot(x1, y1, xlab = "", ylab = "", main = bquote(paste(italic(r),
" = ",.(round(cor(x1, y1),2)))))); abline(3,0.5)
with(anscombe, plot(x2, y2, xlab = "", ylab = "", main = bquote(paste(italic(r),
" = ",.(round(cor(x2, y2),2)))))); abline(3,0.5)
with(anscombe, plot(x3, y3, xlab = "", ylab = "", main = bquote(paste(italic(r),
" = ",.(round(cor(x3, y3),2)))))); abline(3,0.5)
with(anscombe, plot(x4, y4, xlab = "", ylab = "", main = bquote(paste(italic(r),
" = ",.(round(cor(x4, y4),2)))))); abline(3,0.5)
mtext(expression(italic(y[1])),side=1, outer = TRUE, line = 3)
mtext(expression(italic(y[2])),side=2, outer = TRUE, line = 2.6)
mtext("(a)",side=3, at = -42, line = .5)
mtext("(b)",side=3, at = -26, line = .5)
mtext("(c)",side=3, at = -10.3, line = .5)
mtext("(d)",side=3, at = 5.5, line = .5)
par(op)
```

---

ant.dew

*Ant honeydew data*

---

## Description

Wright et al. (2000) examined behavior of red wood ants (*Formica rufa*), a species that harvests honeydew in aphids. Worker ants traveled from their nests to nearby trees to forage honeydew from homopterans. Ants descending trees were laden with food and weighed more, given a particular ant head width, than unladen, ascending ants. The authors were interested in comparing regression parameters of the ascending and descending ants to create a predictive model of honeydew foraging load for a given ant size.

## Usage

```
data(ant.dew)
```

## Format

A data frame with 72 observations on the following 3 variables.

head.width Ant head width in mm

ant.mass Ant mass in mg

direction Direction of travel A = ascending, D = descending

**Details**

Data approximated from Fig. 1 in Wright et al. (2002)

**Source**

Wright, P. J., Bonser, R., and U. O. Chukwu (2000) The size-distance relationship in the wood ant *Formica rufa*. *Ecological Entomology* 25(2): 226-233.

---

 AP.test

 Agresti-Pendergrast test
 

---

**Description**

Provides a more powerful alternative to Friedman's test for blocked (dependent) data with a single replicate.

**Usage**

AP.test(Y)

**Arguments**

Y                    A matrix with treatments in columns and blocks (e.g. subjects) in rows.

**Details**

The Agresti-Pendergrast test is more powerful than Friedman's test, given normality, and remains powerful in heavier tailed distributions (Wilcox 2005).

**Value**

Returns a dataframe showing the numerator and denominator degrees of freedom,  $F$  test statistic, and  $p$ -value.

**Note**

code based on Wilcox (2005).

**Author(s)**

Ken Aho

**References**

Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

**See Also**

[friedman.test](#), [MS.test](#)

**Examples**

```
temp<-c(2.58,2.63,2.62,2.85,3.01,2.7,2.83,3.15,3.43,3.47,2.78,2.71,3.02,3.14,3.35,
2.36,2.49,2.58,2.86,3.1,2.67,2.96,3.08,3.32,3.41,2.43,2.5,2.85,3.06,3.07)
Y<- matrix(nrow=6,ncol=5,data=temp,byrow=TRUE)
AP.test(Y)
```

---

asthma

*Asthma repeated measures dataset from Littell et al. (2002)*

---

**Description**

This dataset was used by Littell (2002) to demonstrate repeated measures analyses. The effect of two asthma drugs and a placebo were measured on 24 asthmatic patients. Each patient was randomly given each drug using an approach to minimize carry-over effects. Forced expiratory volume (FEV1), the volume of air that can be expired after taking a deep breath in one second, was measured. FEV1 was measured hourly for eight hours following application of the drug. A baseline measure of FEV1 was also taken 11 hours before application of the treatment.

**Usage**

```
data(asthma)
```

**Format**

The dataframe has 11 columns:

PATIENT The subjects (there were 24 patients).

BASEFEV1 A numerical variable; the baseline forced expiratory volume.

FEV11H Forced expiratory volume at 11 hours.

FEV12H Forced expiratory volume at 12 hours.

FEV13H Forced expiratory volume at 13 hours.

FEV14H Forced expiratory volume at 14 hours.

FEV15H Forced expiratory volume at 15 hours.

FEV16H Forced expiratory volume at 16 hours.

FEV17H Forced expiratory volume at 17 hours.

FEV18H Forced expiratory volume at 18 hours.

DRUG A factor with three levels "a" = a standard drug treatment, "c" = the drug under development, and "p" = a placebo.

**Source**

Littell, R. C., Stroup, W. W., and R. J. Freund (2002) *SAS for Linear Models*. John Wiley and Associates.



---

auc	<i>Area under a receiver operating characteristic (ROC) curve</i>
-----	---

---

**Description**

A simple algorithm for calculating *AUC*.

**Usage**

```
auc(obs, fit, plot = FALSE)
```

**Arguments**

obs	Dichotomous 0, 1 outcomes (i.e., response values for binomial GLM).
fit	Fitted probabilities from some model.
plot	Logical, indicating whether or not ROC curve plot should be created.

**Author(s)**

Ken Aho

**References**

Agresti, A. (2012) *Categorical Data Analysis, 3rd edition*. New York. Wiley.

**Examples**

```
## Not run:  
obs <- rbinom(30, 1, 0.5)  
fit <- rbeta(30, 1, 2)  
auc(obs, fit)  
## End(Not run)
```

---

baby.walk	<i>Baby walking times experimental data</i>
-----------	---

---

**Description**

In general, mammals are able to walk within minutes or hours after birth. Human babies, however, generally don't begin to walk until they are between 10 and 18 months of age. This occurs because, although humans are born with rudimentary reflexes for walking, they are unused, and thus largely disappear by the age of eight weeks. As a result these movements must be relearned by an infant following significant passage of time, through a process of trial and error. Zelazo et al. (1972) performed a series of experiments to determine whether certain exercises could allow infants to maintain their walking reflexes, and allow them to walk at an earlier age. Study subjects were 24 white male infants from middle class families, and were assigned to one of four exercise treatments.

Active exercise (AE): Parents were taught and were told to apply exercises that would strengthen the walking reflexes of their infant. Passive exercise (PE): Parents were taught and told to apply exercises unrelated to walking. Test-only (TO): The investigators did not specify any exercise, but visited and tested the walking reflexes of infants in weeks 1 through 8. Passive and active exercise infants were also tested in this way. Control (C): No exercises were specified, and infants were only tested at weeks one and eight. This group was established to account for the potential effect of the walking reflex tests themselves.

### Usage

```
data(baby.walk)
```

### Format

A data frame with 22 observations on the following 2 variables.

```
date Age when baby first started walking (in months)
treatment A factor with levels AE C PE TO
```

### Source

Ott, R. L., and M. T. Longnecker 2004 *A First Course in Statistical Methods*. Thompson.

### References

Zelazo, P. R., Zelazo, N. A., and S. Kolb. 1972. Walking in the newborn. *Science* 176: 314-315.

---

bats

*Bat forearm length as a function of bat age*

---

### Description

Data from northern myotis bats (*Myotis septentrionalis*) captured in the field in Vermillion County Indiana in 2000.

### Usage

```
data(bats)
```

### Format

The dataframe has 2 columns:

```
days The age of the bats in days.
forearm.length The length of the forearm in millimeters.
```

### Source

Krochmal, A. R., and D. W. Sparks (2007) *Journal of Mammalogy*. 88(3): 649-656.

---

 Bayes.disc

*Bayesian graphical summaries for discrete or categorical data.*


---

**Description**

An simple function for for summarizing a Bayesian analysis given discrete or categorical variables and priors.

**Usage**

```
Bayes.disc(Likelihood, Prior, data.name = "data", plot = TRUE,
c.data = seq(1, length(Prior)), ...)
```

```
Bayes.disc.tck()
```

**Arguments**

Likelihood	A vector of sample distribution probabilities. This must be in the same order as Prior, i.e. if $\theta_1$ is the first element in Prior, then $data \theta_1$ must be the first element in Data.
Prior	A vector of prior probabilities, or weights.
data.name	A name for data in conditional statements.
plot	Logical, indicating whether a plot should be made.
c.data	A character string of names for discrete classes
...	Additional arguments to <code>plot</code> .

**Author(s)**

Ken Aho

---

 bayes.lm

*Bayesian linear models with uniform priors*


---

**Description**

Gelman et al. (2002) describe general methods for Bayesian implementation of simple linear models (e.g. simple and multiple regression and fixed effect one way ANOVA) with standard non-informative priors uniform on  $\alpha, \sigma^2$ . The function is not yet suited for multifactor or multivariate (random effect) ANOVAs.

**Usage**

```
bayes.lm(Y, X, model = "anova", length = 1000, cred = 0.95)
```

**Arguments**

Y	An $n \times 1$ column vector (a matrix with one column) containing the response variable.
X	The $n \times p$ design matrix
model	One of "anova" or "reg". Parameter output labels are changed depending on choice.
length	Number of draws for posterior.
cred	Level for credible interval.

**Value**

Provides the median and central credible intervals for model parameters.

**Author(s)**

Ken Aho

**References**

Gelman, A., Carlin, J. B., Stern, H. S., and D. B. Rubin (2003) *Bayesian Data Analysis, 2nd edition*. Chapman and Hall/CRC.

**See Also**

[mcmc.norm.hier](#)

**Examples**

```
## Not run:
data(Fbird)
X <- with(Fbird, cbind(rep(1, 18), vol))
Y <- Fbird$freq
bayes.lm(Y, X, model = "reg")

## End(Not run)
```

---

BCI.count

*Barro Colorado Island Tree Counts*

---

**Description**

This dataset, lifted from **vegan**, contains tree counts in 1-hectare plots in Barro Colorado Island, Panama.

**Usage**

```
data(BCI.count)
```

**Format**

A data frame with 50 plots (rows) of 1 hectare with counts of trees on each plot with total of 225 species (columns). Full Latin names are used for tree species.

**Details**

Data give the numbers of trees at least 10 cm in diameter at breast height (1.3 m above the ground) in each one hectare square of forest. Within each one hectare square, all individuals of all species were tallied and are recorded in this table.

The data frame contains only the Barro Colorado Island subset of the original data.

The quadrats are located in a regular grid. See examples for the coordinates.

**Source**

Condit et al. (2002). Data documentation here follows directly from **vegan**.

**References**

Condit, R, Pitman, N, Leigh, E.G., Chave, J., Terborgh, J., Foster, R.B., Nuñez, P., Aguilar, S., Valencia, R., Villa, G., Muller-Landau, H.C., Losos, E. & Hubbell, S.P. (2002). Beta-diversity in tropical forest trees. *Science* 295, 666–669.

---

 BCI.plant

*Tree presence/absence data from Barro Colorado island*


---

**Description**

The presence of the tropical trees *Alchornea costaricensis* and *Anacardium excelsum* with diameter at breast height equal or larger than 10 cm were recorded on along with environmental factors at Barro Colorado Island in Panama (Kindt and Coe 2005). These data were originally from (Pyke et al. 2001).

**Usage**

```
data(BCI.plant)
```

**Format**

A data frame with 43 observations on the following 9 variables.

site.no. A factor with levels C1 C2 C3 C4 p1 p10 p11 p12 p13 p14 p15 p16 p17 p18 p19 p2 p20 p21 p22 p23 p24 p25 p26 p27 p28 p29 p3 p30 p31 p32 p33 p34 p35 p36 p37 p38 p39 p4 p5 p6 p7 p8 p9

UTM.E UTM easting.

UTM.N UTM northing.

precip Precipitation in mm/year.

elev Elevation in m above sea level.

age A categorical vector describing age.

geology A factor describing geology with levels pT Tb Tbo Tc Tcm Tct Tgo Tl Tlc.

Alchornea.costaricensis Plant presence/absence.

Anacardium.excelsum Plant presence/absence.

### Source

Condit et al. (2002), Kindt et al. (2005).

### References

Condit, R, Pitman, N, Leigh, E.G., Chave, J., Terborgh, J., Foster, R.B., Nunez, P., Aguilar, S., Valencia, R., Villa, G., Muller-Landau, H.C., Losos, E. & Hubbell, S.P. (2002). Beta-diversity in tropical forest trees. *Science* 295, 666–669.

Kindt, R. & Coe, R. (2005) Tree diversity analysis: A manual and software for common statistical methods for ecological and biodiversity studies from the **BiodiversityR** package.

Pyke CR, Condit R, Aguilar S and Lao S. (2001). Floristic composition across a climatic gradient in a neotropical lowland forest. *Journal of Vegetation Science* 12: 553-566.

---

BDM.test

*Brunner-Dette-Munk test*

---

### Description

One and two way heteroscedastic rank-based permutation tests. Two way designs are assumed to be factorial, i.e., interactions are tested.

### Usage

BDM.test(Y, X)

BDM.2way(Y, X1, X2)

### Arguments

Y	Vector of response data. A quantitative vector
X	A vector of factor levels for a one-way analysis. To be used with BDM.test
X1	A vector of factor levels for the first factor in a two-way factorial design. To be used with BDM.2way.
X2	A vector of factor levels for the second factor in a two-way factorial design. To be used with BDM.2way.

## Details

A problem with the Kruskal-Wallis test is that, while it does not assume normality for groups, it still assumes homoscedasticity (i.e. the groups have the same distributional shape). As a solution Brunner et al. (1997) proposed a heteroscedastic version of the Kruskal-Wallis test which utilizes the  $F$ -distribution. Along with being robust to non-normality and heteroscedasticity, calculations of exact  $P$ -values using the Brunner-Dette-Munk method are not made more complex by tied values. This is another obvious advantage over the traditional Kruskal-Wallis approach.

## Value

Returns a list with two components

Q                      The "relative effects" for each group.

Table                 An ANOVA type table with hypothesis test results.

## Note

Code based on Wilcox (2005)

## Author(s)

Ken Aho

## References

Brunner, E., Dette, H., and A. Munk (1997) Box-type approximations in nonparametric factorial designs. *Journal of the American Statistical Association*. 92: 1494-1502.

Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

## See Also

[kruskal.test](#), [trim.test](#)

## Examples

```
rye<-c(50,49.8,52.3,44.5,62.3,74.8,72.5,80.2,47.6,39.5,47.7,50.7)
nutrient<-factor(c(rep(1,4),rep(2,4),rep(3,4)))
BDM.test(Y=rye,X=nutrient)
```

---

bear

*Grizzly bear litter sizes*

---

**Description**

Counts of grizzly bear (*Ursus arctos*) litter sizes from the Greater Yellowstone Ecosystem from 1973-2010.

**Usage**

data(bear)

**Format**

A data frame with 38 observations on the following 5 variables.

Year Year.

X1.cub The number of litters with one cub.

X2.cub The number of litters with two cubs.

X3.cub The number of litters with three cubs.

X4.cub The number of litters with four cubs.

**Source**

Haroldson, M. A (2010) Assessing trend and estimating population size from counts of unduplicated females. Pgs 10-15 in Schwartz, C. C., Haroldson, M. A., and K. West editors. *Yellowstone grizzly bear investigations: annual report of the Interagency grizzly bear study team, 2010*. U. S. Geological Survey, Bozeman, MT.

---

beetle

*Wood boring beetle data*

---

**Description**

Saint Germain et al. (2007) modeled the presence absence of a saprophytic wood boring beetle (*Anthophylax attenuatus*) as a function of the wood density of twenty-four decaying aspen trees (*Populus tremuloides*) in Western Quebec Canada.

**Usage**

data(beetle)



**Format**

A data frame with 24 observations on the following 4 variables.

Snag Snag identifier

Yrs.since.death The number of years since death, determined using dendrochronological methods.

Wood.density The density of the decaying wood (dry weight/volume) in units of g cm<sup>-3</sup>.

ANAT Beetle presence/absence (1/0)

**Source**

Saint-Germain, M., Drapeau, P., and C. Buddle (2007) Occurrence patterns of aspen-feeding wood-borers (Coleoptera: Cerambycidae) along the wood decay gradient: active selection for specific host types or neutral mechanisms? *Ecological Entomology* 32: 712-721.

---

best.agreement	<i>Determine agreement of two classifications</i>
----------------	---

---

**Description**

Distinct classifications will have class labels that may prevent straightforward comparisons. This algorithm considers all possible permutations of class labels to find a configuration that maximizes agreement on the diagonal of a contingency table comparing two classifications. Classifications need not have the same number of classes.

**Usage**

```
best.agreement(class1, class2, test = FALSE, rperm = 100)
```

**Arguments**

class1	A vector containing class assignments to observations, e.g., a result from <a href="#">cutree</a>
class2	A vector containing class assignments for a second classification
test	Logical. Indicates whether or not the null hypothesis, that agreement between class1 and class2 is no better than random, will be run.
rperm	If test = TRUE, the number of random permutations used in null hypothesis testing.

**Details**

Class assignments are fixed in class1, all possible permutations of class labels in class2 are considered to find a configuration that maximizes agreement in the two classifications. If test=TRUE, a permutation test is run for the null hypothesis that maximum agreement between classifications is no better than random. This is done by sampling without replacement rperm times from class2, finding maximum agreement between class1 and the randomly permuted classifications, and dividing one plus the number of times that maximum agreement between the random classifications

and `class1` was greater than the maximum agreement observed for `class1` and `class2`. Testing can be slow because it will be based on nested loops with  $pxc!$  steps, where  $p$  is `nperm` and  $c!$  is the number of combinatorial permutations possible for categories in `class2`.

### Value

A object of class `max_agree`.

<code>n.possible.perms</code>	Number of permutations considered
<code>n.max.solutions</code>	Number of configurations in which classification agreement is maximized. The first configuration identified is reported in <code>max.class.names1</code> and <code>max.class.names2</code> .
<code>max.agree</code>	Proportion of observations assigned to the same cluster
<code>max.class.names1</code>	Class labels in the first classification that allow maximum agreement.
<code>max.class.names2</code>	Class labels in the second classification that allow maximum agreement.
<code>test</code>	Whether or not test was run.
<code>p.val</code>	If <code>test = TRUE</code> , the $p$ -value for the null hypothesis test described in Details above.

### Author(s)

Ken Aho. The internal permutations algorithm for obtaining all possible permutations was provided by Benjamin Christoffersen on *stackoverflow*.

### See Also

[cutree](#), [hclust](#)

### Examples

```
# Example comparing a 4 cluster average-linkage solution
# and a 5 cluster Ward-linkage solution

avg <- hclust(dist(USArrests), "ave")
avg.4 <- as.matrix(cutree(avg, k = 4))
war <- hclust(dist(USArrests), "ward.D")
war.5 <- as.matrix(cutree(war, k = 5))

ba <- best.agreement(avg.4, war.5, test = TRUE)
ba
```

---

`bin2dec`*Conversion of binary digits to decimal numbers*

---

**Description**

Converts binary representations to digital numbers (e.g., 10101011 = 171). Fractions, (e.g., 0.11101) will be evaluated to the number of bits provided. The function will handle whole number and fractions, but not whole numbers with fractional parts, (e.g., 111.100110).

**Usage**

```
bin2dec(digits, round = 4)
```

**Arguments**

<code>digits</code>	A string of binary digits.
<code>round</code>	Rounding for fractional results, defaults to 4.

**Author(s)**

Ken Aho

**Examples**

```
bin2dec(1011001101) #=717
```

---

`bombus`*Bombus pollen data.*

---

**Description**

To investigate how pollen removal varied with reproductive caste in bumblebees (*Bombus* sp.) Harder and Thompson (1989) recorded the proportion of pollen removed by thirty five bumblebee queens and twelve worker bees.

**Usage**

```
data(bombus)
```

**Format**

This data frame contains the following columns:

`pollen` A numeric vector indicating the proportion of pollen removed.

`caste` A character string vector indicating whether a bee was a worker "W" or a queen "Q".

**Source**

Harder, L. D. and Thompson, J. D. 1989. Evolutionary options for maximizing pollen dispersal in animal pollinated plants. *American Naturalist* 133: 323-344.

---

 bone

*Bone development data*


---

**Description**

Neter et al. (1996) described an experiment in which researchers investigated the confounding effect of gender and bone development on growth hormone therapy for prepubescent children. Gender had two levels: "M" and "F". The bone development factor had three levels indicating the severity of growth impediment before therapy: 1 = severely depressed, 2 = moderately depressed, and 3 = mildly depressed. At the start of the experiment 3 children were assigned to each of the six treatment combinations. However 4 of the children were unable to complete the experiment, resulting in an unbalanced design.

**Usage**

```
data(bone)
```

**Format**

A data frame with 14 observations on the following 3 variables.

gender A factor with levels F M

devel A factor with levels 1 2 3

growth A numeric vector describing the growth difference before and after hormone therapy

**Source**

Neter, J., Kutner, M. H., Nachtsheim, C. J., and Wasserman, W (1996) *Applied Linear Statistical Models*. McGraw-Hill, Boston MA, USA.

---

 book.menu

*Pulldown menus for 'asbio' interactive graphical functions*


---

**Description**

Provides a pulldown GUI menus to allow access to **asbio** statistical and biological graphical demos, e.g. [anm.ci](#), [samp.dist](#), [anm.loglik](#), etc. The function demos is deprecated. The function book.menu currently provides links to over 100 distinct GUIs (many of these are slaves to other GUIs), which in turn provide distinct graphical demonstrations. The GUIs work best with an SDI R interface.

**Usage**

```
book.menu()
```

**Author(s)**

Ken Aho and Roy Hill (Roy created the book.menu GUI)

**See Also**

[anm.coin](#), [anm.ci](#), [anm.die](#), [anm.exp.growth](#), [anm.geo.growth](#), [anm.log.growth](#), [anm.loglik](#), [anm.LVcomp](#), [anm.LVexp](#), [anm.ls](#), [anm.ls.reg](#), [anm.transM](#), [see.lmu.tck](#), [samp.dist](#), [see.HW](#), [see.logic](#), [see.M](#), [see.move](#), [see.nlm](#), [see.norm.tck](#), [see.power](#), [see.regression.tck](#), [see.typeI\\_II](#), [selftest.se.tck1](#), [shade.norm](#), [Venn](#)

**Examples**

```
## Not run:  
book.menu()  
  
## End(Not run)
```

---

boot.ci.M

*Bootstrap CI of M-estimators differences of two samples*

---

**Description**

Creates a bootstrap confidence interval for location differences for two samples. The default location estimator is the Huber one-step estimator, although any estimator can be used. The function is based on a function written by Wilcox (2005). Note, importantly, that  $P$ -values may be in conflict with the confidence interval bounds.

**Usage**

```
boot.ci.M(X1, X2, alpha = 0.05, est = huber.one.step, R = 1000)
```

**Arguments**

X1	Sample from population one.
X2	Sample from population two.
alpha	Significance level.
est	Location estimator; default is the Huber one step estimator.
R	Number of bootstrap samples.

**Value**

Returns a list with one component, a dataframe containing summary information from the analysis:

<code>R.used</code>	The number of bootstrap samples used. This may not = <code>R</code> if NAs occur because $MAD = 0$ .
<code>ci.type</code>	The method used to construct the confidence interval.
<code>conf</code>	The level of confidence used.
<code>se</code>	The bootstrap distribution of differences standard error.
<code>original</code>	The original, observed difference.
<code>lower</code>	Lower confidence bound.
<code>upper</code>	Upper confidence bound.

**Author(s)**

Ken Aho and R. R. Wilcox from whom I stole liberally from code in the function `m2ci` on R-forge

**References**

Manly, B. F. J. (1997) *Randomization and Monte Carlo methods in Biology, 2nd edition*. Chapman and Hall, London.

Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, 2nd edition*. Elsevier, Burlington, MA.

**See Also**

[bootstrap](#), [ci.boot](#)

**Examples**

```
## Not run:
X1<-rnorm(100,2,2.5)
X2<-rnorm(100,3,3)
boot.ci.M(X1,X2)

## End(Not run)
```

---

bootstrap

*A simple function for bootstrapping*

---

**Description**

The function serves as a simplified alternative to the function [boot](#) from the library `boot`.

**Usage**

```
bootstrap(data, statistic, R = 1000, prob = NULL, matrix = FALSE)
```

**Arguments**

<code>data</code>	Raw data to be bootstrapped. A vector or quantitative data or a matrix if <code>matrix = TRUE</code> .
<code>statistic</code>	A function whose output is a statistic (e.g. a sample mean). The function must have only one argument, a call to <code>data</code> .
<code>R</code>	The number of bootstrap iterations.
<code>prob</code>	A vector of probability weights for parametric bootstrapping.
<code>matrix</code>	A logical statement. If <code>matrix = TRUE</code> then rows in the matrix are sampled as multivariate observations.

**Details**

With bootstrapping we sample with replacement from a dataset of size  $n$  with  $n$  samples  $R$  times. At each of the  $R$  iterations a statistical summary can be created resulting in a bootstrap distribution of statistics.

**Value**

Returns a list. The utility function `asbio:::print.bootstrap` returns summary output. Invisible items include the resampling distribution of the statistic, the data, the statistic, and the bootstrap samples.

**Author(s)**

Ken Aho

**References**

Manly, B. F. J. (1997) *Randomization and Monte Carlo Methods in Biology, 2nd edition*. Chapman and Hall, London.

**See Also**

[boot](#), [ci.boot](#)

**Examples**

```
data(vs)
# A partial set of observations from a single plot for a Scandinavian
# moss/vascular plant/lichen survey.
site18<-t(vs[1,])

#Shannon-Weiner diversity
SW<-function(data){
d<-data[data!=0]
p<-d/sum(d)
-1*sum(p*log(p))
}
```

```
bootstrap(site18[,1],SW,R=1000,matrix=FALSE)
```

---

bound.angle	<i>Angle of azimuth to a boundary.</i>
-------------	--

---

### Description

The function calculates the angle of azimuth from a Cartesian coordination given in  $X$  and  $Y$  to a nearest neighbor coordinate given by  $nX$  and  $nY$ . The nearest neighbor coordinates can be obtained using the function [near .bound](#).

### Usage

```
bound.angle(X, Y, nX, nY)
```

### Arguments

$X$	Cartesian $X$ coordinate of interest.
$Y$	Cartesian $Y$ coordinate of interest.
$nX$	Cartesian $X$ coordinate of nearest neighbor point on a boundary.
$nY$	Cartesian $Y$ coordinate of nearest neighbor point on a boundary.

### Details

The function returns the nearest neighbor angles (in degrees) with respect to a four coordinate system ala ARC-GIS Near(Analysis). Output angles range from  $-180^\circ$  to  $180^\circ$ :  $0^\circ$  to the East,  $90^\circ$  to the North,  $180^\circ$  (or  $-180^\circ$ ) to the West, and  $-90^\circ$  to the South.

### Value

Returns a vector of nearest neighbor angles.

### Author(s)

Ken Aho

### See Also

[near .bound](#), [prp](#)



**Examples**

```

bX<-seq(0,49)/46
bY<-c(4.89000,4.88200,4.87400,4.87300,4.88000,4.87900,4.87900,4.90100,4.90800,
4.91000,4.93300,4.94000,4.91100,4.90000,4.91700,4.93000,4.93500,4.93700,
4.93300,4.94500,4.95900,4.95400,4.95100,4.95800,4.95810,4.95811,4.95810,
4.96100,4.96200,4.96300,4.96500,4.96500,4.96600,4.96700,4.96540,4.96400,
4.97600,4.97900,4.98000,4.98000,4.98100,4.97900,4.98000,4.97800,4.97600,
4.97700,4.97400,4.97300,4.97100,4.97000)

X<-c(0.004166667,0.108333333,0.316666667,0.525000000,0.483333333,0.608333333,
0.662500000,0.683333333,0.900000000,1.070833333)
Y<-c(4.67,4.25,4.26,4.50,4.90,4.10,4.70,4.40,4.20,4.30)
nn<-near.bound(X,Y,bX,bY)

bound.angle(X,Y,nn[,1],nn[,2])

```

bplot

*Barplots with error bars (including interval plots)***Description**

Creates barplots for displaying statistical summaries by treatment (e.g. means, medians, *M*-estimates of location, standard deviation, variance, etc.) and their error estimates by treatment (i.e. standard errors, confidence intervals, *IQRs*, *IQR* confidence intervals, and *MAD* intervals). Custom intervals can also be created. The function can also be used to display letters indicating if comparisons of locations are significant after adjustment for simultaneous inference (see [pairw.anova](#), [pairw.kw](#), and/or [pairw.fried](#)).

**Usage**

```

bplot(y, x, bar.col = "gray", loc.meas = mean, sort = FALSE, order = NULL, int = "SE",
conf = 0.95, uiw = NULL, liw = NULL, sfrac = 0.1, slty = 1, scol = 1,
slwd = 1, exp.fact = 1.5, simlett = FALSE, lett.side = 3, lett = NULL,
cex.lett = 1, names.arg = NULL, ylim = NULL, horiz = FALSE, xpd = FALSE,
print.summary = TRUE, ...)

```

**Arguments**

y	A quantitative vector representing the response variable.
x	A categorical vector representing treatments (e.g. factor levels).
bar.col	Color of bar.
loc.meas	Measure of location or other summary statistic, e.g. mean, median, etc.
sort	Logical, if TRUE, then treatments are ordered by their location statistics.
order	A vector of length equal to the number of factor levels, specifying the order of bars with respect to the alphanumeric order of their names.

int	Type of error bar to be drawn, must be one of "SE", "CI", <a href="#">IQR</a> , "MAD", "IQR.CI" or "bootSE". IQR-derived confidence intervals are based on $\pm 1.58IQR/\sqrt{n}$ and provide an approximate 95% confidence interval for the difference in two medians. The measure can be attributed to Chambers et al. (1983, p. 62), given McGill et al. (1978, p. 16). It is based on asymptotic normality of the median and assumes roughly equal sample sizes for the two medians being compared. The interval is apparently insensitive to the underlying distributions of the samples. The specification "bootSE" gives bootstrap SEs for the location measure using the function <a href="#">bootstrap</a>
conf	Level of confidence, $1 - P(\text{type I error})$ .
uiw	Upper y-coordinate for the error bar, if NULL then this will be computed from int.
liw	Lower y-coordinate for the error bar, if NULL then this will be computed from int.
sfrac	Scaling factor for the size of the "serifs" (end bars) on the confidence bars, in x-axis units.
slty	Line type for error bars.
scol	Line color for error bars.
slwd	Line width for error bars.
exp.fact	A multiplication factor indicating how much extra room is made for drawing letters in top of graph. Only used if <code>simlett = TRUE</code> .
simlett	A logical statement indicating whether or not letters should be shown above bars indicating that populations means have been determined to be significantly different.
lett.side	Side that letters will be drawn on, 1 = bottom, 2 = left, 3 = top, 4 = right.
lett	A vector of letters or some other code to display multiple comparison results.
cex.lett	Character expansion for multiple comparison result letters.
names.arg	A vector of names to be plotted below each bar or error bar. If this argument is omitted, then the names are taken from the names attribute of y.
ylim	Upper and lower limits of the Y-axis
horiz	Logical value. If FALSE, then bars are drawn vertically with the first bar to the left. If TRUE, then bars are drawn horizontally with the first at the bottom.
xpd	Logical value. If FALSE, this overrides <a href="#">barplot</a> designation <code>xpd = TRUE</code> , which may cause bars to extend off the plot if <code>ylim</code> is modified.
print.summary	Logical value. If TRUE a summary of the location and dispersion measures used in the plot is printed.
...	Additional arguments from <a href="#">barplot</a> .

### Details

It is often desirable to display the results of a pairwise comparison procedure using sample measures of location and error bars. This functions allows these sorts of plots to be made. The function is essentially a wrapper for the function [barplot](#).

**Value**

A plot is returned. Bar centers (ala [barplot](#)) are returned invisibly.

**Author(s)**

Ken Aho

**References**

Chambers, J. M., Cleveland, W. S., Kleiner, B. and Tukey, P. A. (1983) *Graphical Methods for Data Analysis*. Wadsworth & Brooks/Cole.

McGill, R., Tukey, J. W. and Larsen, W. A. (1978) Variations of box plots. *The American Statistician* 32, 12-16.

**See Also**

[mad](#), [barplot](#), [pairw.anova](#), [pairw.kw](#), [pairw.fried](#)

**Examples**

```
eggs<-c(11,17,16,14,15,12,10,15,19,11,23,20,18,17,27,33,22,26,28)
trt<-c(1,1,1,1,1,2,2,2,2,2,3,3,3,3,4,4,4,4,4)
bplot(y=eggs, x=factor(trt),int="SE",xlab="Treatment",ylab="Mean number of eggs",
simlett=TRUE, lett=c("b","b","b","a"))
```

---

bromus

*Bromus tectorum dataset*


---

**Description**

Cheatgrass (*Bromus tectorum*) is an introduced annual graminoid that has invaded vast areas of sagebrush steppe in the intermountain west. Because it completes its vegetative growth stage relatively early in the summer, it leaves behind senescent biomass that burns easily. As a result areas with cheatgrass often experience a greater frequency of summer fires. A number of dominant shrub species in sagebrush steppe are poorly adapted to fire. As a result, frequent fires can change a community formerly dominated by shrubs to one dominated by cheatgrass. Nitrogen can also have a strong net positive effect on the cheatgrass biomass. A study was conducted at the Barton Road Long Term Experimental Research site (LTER) in Pocatello Idaho to simultaneously examine the effect of shrub removal and nitrogen addition on graminoid productivity.

**Usage**

```
data(bromus)
```

**Format**

The dataframe has 3 columns:

Plot Plot number.

Biomass Grass biomass in grams per meter squared.

Trt Treatment. C = Control, LN = Low nitrogen, HN = High Nitrogen, SR = Shrub removal.

---

 bv.boxplot

*Bivariate boxplots*


---

**Description**

Creates diagnostic bivariate quelplot ellipses (bivariate boxplots) using the method of Goldberg and Iglewicz (1992). The output can be used to check assumptions of bivariate normality and to identify multivariate outliers. The default robust=TRUE option relies on a biweight correlation estimator function written by Everitt (2006). Quelplots, are potentially asymmetric, although the method currently employed here uses a single "fence" definition and creates symmetric ellipses.

**Usage**

```
bv.boxplot(X, Y, robust = TRUE, D = 7, xlab = "X", ylab="Y", pch = 21,
pch.out = NULL, bg = "gray", bg.out = NULL, hinge.col = 1, fence.col = 1,
hinge.lty = 2, fence.lty = 3, xlim = NULL, ylim = NULL, names = 1:length(X),
ID.out = FALSE, cex.ID.out = 0.7, uni.CI = FALSE, uni.conf = 0.95,
uni.CI.col = 1, uni.CI.lty = 1, uni.CI.lwd = 2, show.points = TRUE, ...)
```

**Arguments**

X	First of two quantitative variables making up the bivariate distribution.
Y	Second of two quantitative variables making up the bivariate distribution.
robust	Logical. Robust estimators, i.e. robust = TRUE are recommended.
D	The default D = 7 lets the fence be equal to a 99 percent confidence interval for an individual observation.
xlab	Caption for X axis.
ylab	Caption for Y axis.
pch	Plotting character(s) for scatterplot.
pch.out	Plotting character for outliers.
hinge.col	Hinge color.
fence.col	Fence color.
hinge.lty	Hinge line type.
fence.lty	Fence line type.
xlim	A two element vector defining the X-limits of the plot.

ylim	The Y-limits of the plot.
bg	Background color for points in scatterplot, defaults to black if pch is not in the range 21:26.
bg.out	Background color for outlying points in scatterplot, defaults to black if pch is not in the range 21:26.
names	An optional vector of names for X, Y coordinates.
ID.out	Logical. Whether or not outlying points should be given labels (from argument name in plot).
cex.ID.out	Character expansion for outlying ID labels.
uni.CI	Logical. If true, univariate confidence intervals for the true median at confidence uni.CI are shown.
uni.conf	Univariate confidence, only used if CI.uni = TRUE.
uni.CI.col	Univariate confidence bound line color, only used if CI.uni = TRUE.
uni.CI.lty	Univariate confidence bound line type, only used if CI.uni = TRUE.
uni.CI.lwd	Univariate confidence bound line width, only used if CI.uni = TRUE.
show.points	Logical. Whether points should be shown in graph.
...	Additional arguments from <a href="#">points</a> .

### Details

Two ellipses are drawn. The inner is the "hinge" which contains 50 percent of the data. The outer is the "fence". Observations outside of the "fence" constitute possible troublesome outliers. The function `bivariate` from Everitt (2004) is used to calculate robust biweight measures of correlation, scale, and location if `robust = TRUE` (the default). We have the following form to the `quelp` model:

$$E_i = \sqrt{\frac{X_{si}^2 + Y_{si}^2 - 2R^* X_{si} Y_{si}}{1 - R^{*2}}}$$

where  $X_{si} = (X_i - T_X^*)/S_X^*$ , and  $Y_{si} = (Y_i - T_Y^*)/S_Y^*$  are standardized values for  $X_i$  and  $Y_i$ , respectively,  $T_X^*$  and  $T_Y^*$  are location estimators for  $X$  and  $Y$ ,  $S_X^*$  and  $S_Y^*$  are scale estimators for  $X$  and  $Y$ , and  $R^*$  is a correlation estimator for  $X$  and  $Y$ . We have:

$$E_m = \text{median}\{E_i : i = 1, 2, \dots, n\},$$

and

$$E_{max} = \text{max}\{E_i : E_i^2 < DE_m^2\}.$$

where  $D$  is a constant that regulates the distance of the "fence" and "hinge".

To draw the "hinge" we have:

$$R_1 = E_m \sqrt{\frac{1 + R^*}{2}},$$

$$R_2 = E_m \sqrt{\frac{1 - R^*}{2}}.$$

To draw the "fence" we have:

$$R_1 = E_{max} \sqrt{\frac{1 + R^*}{2}},$$

$$R_2 = E_{max} \sqrt{\frac{1 - R^*}{2}}.$$

For  $\theta = 0$  to 360, let:

$$\Theta_1 = R_1 \cos(\theta),$$

$$\Theta_2 = R_2 \sin(\theta).$$

The Cartesian coordinates of the "hinge" and "fence" are:

$$X = T_X^* = (\Theta_1 + \Theta_2) S_X^*,$$

$$Y = T_Y^* = (\Theta_1 - \Theta_2) S_Y^*.$$

Quelplots, are potentially asymmetric, although the current (and only) method used here defines a single value for  $E_{max}$  and hence creates symmetric ellipses. Under this implementation at least one point will define  $E_{max}$ , and lie on the "fence".

### Value

A diagnostic plot is returned. Invisible objects from the function include location, scale and correlation estimates for  $X$  and  $Y$ , estimates for  $E_m$  and  $E_{max}$ , and a list of outliers (that exceed  $E_{max}$ ).

### Author(s)

Ken Aho, the function relies on an Everitt (2006) function for robust  $M$ -estimation.

### References

- Everitt, B. (2006) *An R and S-plus Companion to Multivariate Analysis*. Springer.
- Goldberg, K. M., and B. Ingelwicz (1992) Bivariate extensions of the boxplot. *Technometrics* 34: 307-320.

### See Also

[boxplot](#)

**Examples**

```

Y1<-rnorm(100, 17, 3)
Y2<-rnorm(100, 13, 2)
bv.boxplot(Y1, Y2)

X <- c(-0.24, 2.53, -0.3, -0.26, 0.021, 0.81, -0.85, -0.95, 1.0, 0.89, 0.59,
0.61, -1.79, 0.60, -0.05, 0.39, -0.94, -0.89, -0.37, 0.18)
Y <- c(-0.83, -1.44, 0.33, -0.41, -1.0, 0.53, -0.72, 0.33, 0.27, -0.99, 0.15,
-1.17, -0.61, 0.37, -0.96, 0.21, -1.29, 1.40, -0.21, 0.39)
b <- bv.boxplot(X, Y, ID.out = TRUE, bg.out = "red")
b

```

bvn.plot

*Make plots of bivariate normal distributions***Description**

The function uses functions from **lattice** and **mvtnorm** to make wireframe plots of bivariate normal distributions. Remember that the covariance must be less than the product of the marginal standard deviations (square roots of the diagonal elements).

**Usage**

```

bvn.plot(mu = c(0, 0), cv = 0, vr = c(1, 1), res = 0.3, xlab = expression(y[1]),
ylab = expression(y[2]), zlab = expression(paste("f(", y[1], ", ", y[2], ")")), ...)

```

**Arguments**

mu	A vector containing the joint distribution means.
cv	A number, indicating the covariance of the two variables.
vr	The diagonal elements in the variance covariance matrix.
res	Plot resolution. Smaller values create a more detailed wireframe plot.
xlab	X-axis label.
ylab	Y-axis label.
zlab	Z-axis label.
...	Additional arguments from <a href="#">wireframe</a> .

**Author(s)**

Ken Aho

C.isotope

*Atmospheric carbon and D14C measurements***Description**

Atmospheric  $\delta^{14}\text{C}$  (per mille) and  $\text{CO}_2$  (ppm) measurements for La Jolla Pier, California. Latitude: 32.9 Degrees N, Longitude: 117.3 Degrees W, Elevation: 10m;  $\delta^{14}\text{C}$  derived from flask air samples

**Usage**

```
data(C.isotope)
```

**Format**

A data frame with 280 observations on the following 5 variables.

```
Date a factor with levels 01-Apr-96 01-Jul-92 01-Jul-93 02-Apr-01 02-Feb-96 02-Nov-94 02-Oct-92
03-Aug-06 03-Aug-92 03-Jan-95 03-Jan-97 03-Jul-95 03-Mar-93 03-May-05 03-May-96
03-Nov-05 04-Apr-94 04-Jun-01 04-Jun-03 04-Mar-03 04-May-01 04-May-07 04-Sep-96
05-Aug-96 05-Jul-05 05-Jun-00 05-Sep-00 06-Aug-02 06-Oct-06 06-Sep-01 06-Sep-07
07-Apr-05 07-Apr-95 07-Aug-07 07-Dec-07 07-Feb-01 07-Feb-03 07-Feb-05 07-Jun-07
07-Mar-01 07-Sep-05 08-Feb-94 08-Feb-95 08-Feb-99 08-Jan-01 08-Jun-95 08-Sep-99
09-Dec-01 09-Feb-93 09-Jan-02 09-Jun-04 09-Nov-00 09-Nov-02 09-Nov-06 09-Sep-02
09-Sep-03 09-Sep-92 10-Apr-03 10-Aug-01 10-Aug-97 10-Aug-99 10-Jan-98 10-Jun-02
10-Nov-95 10-Oct-00 10-Oct-04 10-Oct-97 11-Dec-92 11-Feb-00 11-Jan-07 11-Jan-93
11-Mar-94 11-Mar-96 11-Nov-93 11-Oct-02 12-Apr-93 12-Apr-99 12-Aug-93 12-Jul-02
12-Jun-06 12-Oct-07 13-Feb-98 13-Jan-98 13-Jun-01 13-Mar-95 13-May-02 13-Sep-06
14-Apr-00 14-Aug-00 14-Dec-98 14-Feb-03 14-Jul-00 14-Sep-04 15-Dec-93 15-Feb-06
15-Feb-95 15-May-95 15-Oct-99 16-Apr-96 16-Jul-01 16-Jun-00 16-Nov-03 16-Nov-99
16-Oct-95 17-Dec-02 17-Feb-02 17-Feb-97 17-Jul-06 17-Jul-07 17-Mar-06 17-May-94
17-Nov-99 18-Aug-00 18-Dec-92 18-Jul-97 18-Jun-05 18-Mar-03 18-May-93 18-Nov-94
19-Apr-05 20-Apr-04 20-Mar-00 21-Apr-06 21-Aug-95 21-Dec-04 21-Jan-00 21-Jul-99
21-Jun-02 21-Jun-93 22-Apr-97 22-Feb-00 22-Feb-96 22-Jan-96 22-Jun-94 22-Mar-02
22-May-06 22-May-98 23-Apr-98 23-Feb-07 23-Jul-92 23-Jun-97 23-Mar-01 23-Mar-05
24-Apr-03 24-Aug-94 24-Feb-93 24-Jul-01 24-Jul-02 24-Jun-03 24-Mar-04 25-Apr-02
25-Aug-98 25-Jan-06 25-Oct-96 26-Aug-04 26-Dec-03 26-Feb-04 26-Jan-05 26-Jan-99
26-Jun-96 26-Mar-04 26-May-00 26-May-04 26-Sep-95 27-Jul-04 27-Mar-07 27-Nov-96
27-Oct-05 28-Jul-04 28-Jul-05 29-Aug-03 29-Dec-02 29-Jul-98 29-Jun-98 29-Oct-92
29-Oct-98 30-Jun-97 30-Nov-93 31-Dec-99 31-Jan-04 31-Oct-01 31-Oct-03
```

Decimal.date A numeric vector

CO2 CO<sub>2</sub> concentration (in ppm)

D14C  $\delta^{14}\text{C}$  (in per mille)

D14C.uncertainty measurement uncertainty for D14C(in per mille)



**Source**

H. D. Graven, R. F. Keeling, A. F. Bollenbacher Scripps CO<sub>2</sub> Program Scripps Institution of Oceanography (SIO) University of California, La Jolla, California USA 92093-0244 and

T. P. Guilderson Center for Accelerator Mass Spectrometry (CAMS) Lawrence Livermore National Laboratory (LLNL) Livermore, California USA 94550

**References**

H. D. Graven, T. P. Guilderson and R. F. Keeling, Observations of radiocarbon in CO<sub>2</sub> at La Jolla, California, USA 1992-2007: Analysis of the long-term trend. *Journal of Geophysical Research*.

---

caribou

*Caribou count data*

---

**Description**

Stratified random sampling was used to estimate the size of the Nelchina herd of Alaskan caribou (*Rangifer tarandus*) in February 1962 (Siniff and Skoog 1964). The total population of sample units (for which responses would be counts of caribou) consisted of 699 four mile<sup>2</sup> areas. This population was divided into six strata, and each of these was randomly sampled.

**Usage**

```
data(caribou)
```

**Format**

A data frame with 6 observations on the following 5 variables.

stratum Strata; a factor with levels A B C D E F

N.h Strata population size

n.h Strata sample size

x.bar.h Strata means

var.h Strata variances

**Source**

Siniff, D. B., and R. O. Skoog (1964) Aerial censusing of caribou using stratified random sampling. *Journal of Wildlife Management* 28: 391-401.

---

case0902

*Dataset of mammal traits from Ramsey and Schaefer (1997)*

---

### **Description**

These data were used by Ramsey and Schaefer (1997) to demonstrate multiple regression. The dataset was originally collected by Sacher and Stafeldt (1974) and provided (for varying sample sizes) average values of brain weight, body weight, gestation period and litter size for 96 placental mammal species.

### **Usage**

```
data("case0902")
```

### **Format**

A data frame with 96 observations on the following 5 variables.

Xs A factor defining common names for mammal species under examination.

Y Brain weight (in grams).

Xb Body weight (in kilograms).

Xg Gestation period length (in days).

Xl Litter size.

### **Source**

Ramsey, F., and Schafer, D. (1997). *The statistical sleuth: a course in methods of data analysis*. Cengage Learning.

### **References**

Sacher, G. A., and Staffeldt, E. F. (1974). Relation of gestation time to brain weight for placental mammals: implications for the theory of vertebrate growth. *The American Naturalist*, 108(963), 593-615.

### **Examples**

```
data(case0902)
```

---

case1202	<i>Dataset of salary attributes for male and female workers from Ramsey and Schafer (1997)</i>
----------	--

---

### Description

Ramsey and Schafer (1997) used this dataset to illustrate considerations in model selection. The data describe attributes of 61 female and 32 male clerical employees hired between 1965 and 1975 by a bank sued for sexual harassment.

### Usage

```
data("case1202")
```

### Format

A data frame with 93 observations on the following 7 variables.

Yhire Annual salary upon hire (US dollars).

Y77 Annual salary in 1977 (US dollars).

Xsex Sex; a factor with the levels FEMALE and MALE.

Xsen Seniority (months since first hired).

Xage Age (in months).

Xed Education (in years).

Xexp Experience previous to being hired by the bank (in months).

### Source

Ramsey, F., and Schafer, D. (1997). *The statistical sleuth: a course in methods of data analysis*. Cengage Learning.

### Examples

```
data(case1202)
```

---

 chi.plot

*Chi plots for diagnosing multivariate independence.*


---

### Description

Chi-plots (Fisher and Switzer 1983, 2001) provide a method to diagnose multivariate non-independence among  $Y$  variables.

### Usage

```
chi.plot(Y1, Y2, ...)
```

### Arguments

Y1	A $Y$ variable of interest. Must be quantitative vector.
Y2	A second $Y$ variable of interest. Must also be a quantitative vector.
...	Additional arguments from <code>plot</code> .

### Details

The method relies on calculating all possible pairwise differences within  $\mathbf{y}_1$  and within  $\mathbf{y}_2$ . Let pairwise differences associated with the first observation in  $\mathbf{y}_1$  that are greater than zero be transformed to ones and all other differences be zeros. Take the sum of the transformed values, and let this sum divided by  $(1 - n)$  be the first element in the  $1 \times n$  vector  $\mathbf{z}$ . Find the rest of the elements  $(2, \dots, n)$  in  $\mathbf{z}$  using the same process.

Perform the same transformation for the pairwise differences associated with the first observation in  $\mathbf{y}_2$ . Let pairwise differences associated with the first observation in  $\mathbf{y}_2$  that are greater than zero be transformed to ones and all other differences be zeros. Take the sum of the transformed values, and let this sum divided by  $(1 - n)$  be the first element in the  $1 \times n$  vector  $\mathbf{g}$ . Find the rest of the elements  $(2, \dots, n)$  in  $\mathbf{g}$  using the same process.

Let pairwise differences associated with the first observation in  $\mathbf{y}_1$  and the first observation in  $\mathbf{y}_2$  that are both greater than zero be transformed to ones and all other differences be zeros. Take the sum of the transformed values, and let this sum divided by  $(1 - n)$  be the first element in the  $1 \times n$  vector  $\mathbf{h}$ . Find the rest of the elements  $(2, \dots, n)$  in  $\mathbf{h}$  using the same process. We let:

$$S = \text{sign}((\mathbf{z} - 0.5)(\mathbf{g} - 0.5))$$

$$\chi = (\mathbf{h} - \mathbf{z} \times \mathbf{g}) / \sqrt{\mathbf{z} \times (1 - \mathbf{z}) \times \mathbf{g} \times (1 - \mathbf{g})}$$

$$\lambda = 4 \times S \times \max[(\mathbf{z} - 0.5)^2, (\mathbf{g} - 0.5)^2]$$

We plot the resulting paired  $\chi$  and  $\lambda$  values for values of  $\lambda$  less than  $4(1/(n - 1) - 0.5)^2$ . Values outside of  $\frac{1.78}{\sqrt{n}}$  can be considered non-independent.

### Value

Returns a chi-plot.

**Author(s)**

Ken Aho and Tom Taverner (Tom provided modified original code to eliminate looping)

**References**

- Everitt, B. (2006) *R and S-plus Companion to Multivariate Analysis*. Springer.
- Fisher, N. I, and Switzer, P. (1985) Chi-plots for assessing dependence. *Biometrika*, 72: 253-265.
- Fisher, N. I., and Switzer, P. (2001) Graphical assessment of dependence: is a picture worth 100 tests? *The American Statistician*, 55: 233-239.

**See Also**

[bv.boxplot](#)

**Examples**

```
Y1<-rnorm(100, 15, 2)
Y2<-rnorm(100, 18, 3.2)
chi.plot(Y1, Y2)
```

---

chronic

*Chronic ailment counts for urban and rural women in Australia*

---

**Description**

Brown et al (1996) showed that Australian women who live in rural areas tended to have fewer visits with general practitioners. It was not clear from this data, however, whether this was because they were healthier or because of other factors (e.g. shortage of doctors, higher costs of visits, longer distances to travel for visits, etc.). To address this Dobson issue (2001) compiled data describing the number of chronic medical conditions for women visiting general practitioners in New South Wales. Women were divided into two groups; those from rural areas, and those from urban areas. All of the women were age 70-75, had the same socioeconomic status and reported to general practitioners three or fewer times in 1996. The question of central interest was: "do women who have the same level of general practitioner visits have the same medical need?"

**Usage**

```
data(chronic)
```

**Format**

A data frame with 49 observations on the following 4 variables.

- subject The subject number.
- count The number of chronic conditions in a subject.
- setting a factor with levels RURAL URBAN.

**Source**

Dobson, A. J. 2001. *An Introduction to Generalized Linear Models, 2nd edition*. Chapman and Hall, London.

**References**

Brown, W. J. Bryon, L., Byles, J., et al. (1996) Women's health in Australia: establishment of the Australian longitudinal study on women's health. *Journal of Women's Health*. 5: 467-472.

---

 ci.boot

---

*Bootstrap confidence intervals*


---

**Description**

Bootstrap confidence intervals for the output of function `bootstrap`. Up to five different interval estimation methods can be called simultaneously: the normal approximation, the basic bootstrap, the percentile method, the bias corrected and accelerated method (BCa), and the studentized bootstrap method.

**Usage**

```
ci.boot(x, method = "all", sigma.t = NULL, conf = 0.95)
```

**Arguments**

<code>x</code>	For <code>ci.boot</code> the list output from <code>bootstrap</code> .
<code>method</code>	CI interval method to be used. One of "all", "norm", "basic", "perc", "BCa", or "student". Partial matches are allowed.
<code>sigma.t</code>	Vector of standard errors in association with studentized intervals.
<code>conf</code>	Confidence level; $1 - P(\text{Type I error})$ .

**Author(s)**

Ken Aho

**References**

Manly, B. F. J. (1997) *Randomization and Monte Carlo Methods in Biology, 2nd edition*. Chapman and Hall, London.

**See Also**

[boot](#), [bootstrap](#),

**Examples**

```

data(vs)
# A partial set of observations from a single plot for a Scandinavian
# moss/vascular plant/lichen survey.
site18<-t(vs[1,])

#Shannon-Weiner diversity
SW<-function(data){
d<-data[data!=0]
p<-d/sum(d)
-1*sum(p*log(p))
}

b <- bootstrap(site18[,1],SW)
ci.boot(b)

```

---

ci.impt

*Confidence interval for the product of two proportions*


---

**Description**

Provides one and two-tailed confidence intervals for the true product of two proportions.

**Usage**

```

ci.impt(y1, n1, y2 = NULL, n2 = NULL, avail.known = FALSE, pi.2 = NULL,
conf = .95, x100 = TRUE, alternative = "two.sided", bonf = TRUE, wald = FALSE)

```

**Arguments**

y1	The number of successes associated with the first proportion.
n1	The number of trials associated with the first proportion.
y2	The number of successes associated with the second proportion. Not used if avail.known = TRUE.
n2	The number of trials associated with the first proportion. Not used if avail.known = TRUE.
avail.known	Logical. Are the proportions $\pi_{2i}$ known? If avail.known = TRUE these proportions should specified in the pi.2 argument.
pi.2	Proportions for $\pi_{2i}$ . Required if avail.known = TRUE.
conf	Confidence level, i.e., $1 - \alpha$ .
x100	Logical. If true, estimate is multiplied by 100.
alternative	One of "two.sided", "less", "greater". Allows lower, upper, and two-tailed confidence intervals. If alternative = "two.sided" (the default), then a conventional two-sided confidence interval is given. The specifications alternative = "less" and alternative = "greater" provide lower and upper tailed CIs, respectively.

bonf	Logical. If bonf = TRUE, and the number of requested intervals is greater than one, then Bonferroni-adjusted intervals are returned.
wald	Logical. If avail.known = TRUE one can apply one of two standard error estimators. The default is a delta-derived estimator. If wald = TRUE is specified a modified Wald standard error estimator is used.

### Details

Let  $Y_1$  and  $Y_2$  be multinomial random variables with parameters  $n_1, \pi_{1i}$  and  $n_2, \pi_{2i}$ , respectively; where  $i = 1, 2, \dots, r$ . Under delta derivation, the log of the products of  $\pi_{1i}$  and  $\pi_{2i}$  (or the log of a product of  $\pi_{1i}$  and  $\pi_{2i}$  and a constant) is asymptotically normal with mean  $\log(\pi_{1i} \times \pi_{2i})$  and variance  $(1 - \pi_{1i})/\pi_{1i}n_1 + (1 - \pi_{2i})/\pi_{2i}n_2$ . Thus, an asymptotic  $(1 - \alpha)100$  percent confidence interval for  $\pi_{1i} \times \pi_{2i}$  is given by:

$$\hat{\pi}_{1i} \times \hat{\pi}_{2i} \times \exp(\pm z_{1-(\alpha/2)} \hat{\sigma}_i)$$

where:  $\hat{\sigma}_i^2 = \frac{(1-\hat{\pi}_{1i})}{\hat{\pi}_{1i}n_1} + \frac{(1-\hat{\pi}_{2i})}{\hat{\pi}_{2i}n_2}$  and  $z_{1-(\alpha/2)}$  is the standard normal inverse CDF at probability  $1 - \alpha$ .

### Value

Returns a list of class = "ci". Printed results are the parameter estimate and confidence bounds.

### Note

Method will perform poorly given unbalanced sample sizes.

### Author(s)

Ken Aho

### References

Aho, K., and Bowyer, T. 2015. Confidence intervals for a product of proportions: Implications for importance values. *Ecosphere* 6(11): 1-7.

### See Also

[ci.prat](#), [ci.p](#)

### Examples

```
ci.impt(30,40, 25,40)
```



---

`ci.median`*Confidence interval for the median*

---

**Description**

Calculates the upper and lower confidence bounds for the true median, and calculates true coverage of the interval.

**Usage**

```
ci.median(x, conf = 0.95)
```

**Arguments**

<code>x</code>	A vector of quantitative data.
<code>conf</code>	The desired level of confidence $1 - P(\text{type I error})$ .

**Value**

Returns a list of class = "ci". Default printed results are the parameter estimate and confidence bounds. Other invisible objects include:

<code>coverage</code>	The true coverage of the interval.
-----------------------	------------------------------------

**Author(s)**

Ken Aho

**References**

Ott, R. L., and M. T. Longnecker (2004) *A First Course in Statistical Methods*. Thompson.

**See Also**

[median](#)

**Examples**

```
x<-rnorm(20)
ci.median(x)
```

---

ci.mu.oneside

*One sided confidence interval for mu.*


---

### Description

In some situations we may wish to quantify confidence in the region above or below a mean estimate. For instance, a biologist working with an endangered species may be interested in saying: "I am 95 percent confident that the true mean number of offspring is above a particular threshold." In a one-sided situation, we essentially let our confidence be  $1 - 2\alpha$  (instead of  $1 - \alpha$ ). Thus, if our significance level for a two-tailed test is  $\alpha$ , our one-tailed significance level will be  $2\alpha$ .

### Usage

```
ci.mu.oneside(data, conf = 0.95, n = NULL, Var = NULL, xbar = NULL,
summarized = FALSE, N = NULL, fpc = FALSE, tail = "upper", na.rm = FALSE)
```

### Arguments

data	A vector of quantitative data. Required if summarized=TRUE.
conf	Level of confidence; $1 - P(\text{type I error})$ .
n	Sample size. Required if summarized=TRUE.
Var	Sample variance. Required if summarized=TRUE.
xbar	Sample mean. Required if summarized=TRUE.
summarized	Logical. Indicates whether summary statistics instead of raw data should be used.
N	Population size. Required if summarized=TRUE.
fpc	Logical. Indicating whether finite population corrections should be made.
tail	Indicates what side the one sided confidence limit should be calculated for. Choices are "upper" or "lower".
na.rm	Logical, indicate whether NA values should be stripped before the computation proceeds.

### Value

Returns a list of class = "ci". Default output is a matrix with the sample mean and either the upper or lower confidence limit.

### Author(s)

Ken Aho

### References

Bain, L. J., and Engelhardt, M. (1992) *Introduction to Probability and Mathematical Statistics*. Duxbury press, Belmont, CA, USA.

**See Also**[ci.mu.t](#)**Examples**

```
ci.mu.oneside(rnorm(100))
```

---

 ci.mu.z

*Z and t confidence intervals for mu.*


---

**Description**

These functions calculate  $t$  and  $z$  confidence intervals for  $\mu$ .  $Z$  confidence intervals require specification (and thus knowledge) of  $\sigma$ . Both methods assume underlying normal distributions although this assumption becomes irrelevant for large sample sizes. Finite population corrections are provided if requested.

**Usage**

```
ci.mu.z(data, conf = 0.95, sigma = 1, summarized = FALSE, xbar = NULL,
fpc = FALSE, N = NULL, n = NULL, na.rm = FALSE)
```

```
ci.mu.t(data, conf = 0.95, summarized = FALSE, xbar = NULL, sd = NULL,
fpc = FALSE, N = NULL, n = NULL, na.rm = FALSE)
```

**Arguments**

data	A vector of quantitative data. Required if summarized = FALSE
conf	Confidence level; $1 - P(\text{type I error})$ .
sigma	The population standard deviation.
summarized	A logical statement specifying whether statistical summaries are to be used. If summarized = FALSE, then the sample mean and the sample standard deviation (t.conf only) are calculated from the vector provided in data. If summarized = TRUE then the sample mean xbar, the sample size n, and, in the case of ci.mu.t, the sample standard deviation st.dev, must be provided by the user.
xbar	The sample mean. Required if summarized = TRUE.
fpc	A logical statement specifying whether a finite population correction should be made. If fpc = TRUE the population size N must be specified.
N	The population size. Required if fpc=TRUE
sd	The sample standard deviation. Required if summarized=TRUE.
n	The sample size. Required if summarized = TRUE.
na.rm	Logical, indicate whether NA values should be stripped before the computation proceeds.

**Details**

ci.mu.z and ci.mu.t calculate confidence intervals for either summarized data or a dataset provided in data. Finite population corrections are made if a user specifies fpc=TRUE and provides some value for N.

**Value**

Returns a list of class = "ci". Default printed results are the parameter estimate and confidence bounds. Other invisible objects include:

Margin                    the confidence margin.

**Author(s)**

Ken Aho

**References**

Lohr, S. L. (1999) *Sampling: Design and Analysis*. Duxbury Press. Pacific Grove, USA.

**See Also**

[pnorm](#), [pt](#)

**Examples**

```
#With summarized=FALSE
x<-c(5,10,5,20,30,15,20,25,0,5,10,5,7,10,20,40,30,40,10,5,0,0,3,20,30)
ci.mu.z(x,conf=.95,sigma=4,summarized=FALSE)
ci.mu.t(x,conf=.95,summarized=FALSE)
#With summarized = TRUE
ci.mu.z(x,conf=.95,sigma=4,xbar=14.6,n=25,summarized=TRUE)
ci.mu.t(x,conf=.95,sd=4,xbar=14.6,n=25,summarized=TRUE)
#with finite population correction and summarized = TRUE
ci.mu.z(x,conf=.95,sigma=4,xbar=14.6,n=25,summarized=TRUE,fpc=TRUE,N=100)
ci.mu.t(x,conf=.95,sd=4,xbar=14.6,n=25,summarized=TRUE,fpc=TRUE,N=100)
```

---

ci.p

*Confidence interval estimation for the binomial parameter pi using five popular methods.*

---

**Description**

Confidence interval formulae for  $\mu$  are not appropriate for variables describing binary outcomes. The function p.conf calculates confidence intervals for the binomial parameter  $\pi$  (probability of success) using raw or summarized data. By default Agresti-Coull point estimators are used to estimate  $\pi$  and  $\sigma_{\hat{\pi}}$ . If raw data are to be used (the default) then successes should be indicated as ones and failures as zeros in the data vector. Finite population corrections can also be specified.

**Usage**

```
ci.p(data, conf = 0.95, summarized = FALSE, phat = NULL,
      fpc = FALSE, n = NULL, N = NULL, method="agresti.coull", plot = TRUE)
```

**Arguments**

data	A vector of binary data. Required if summarized = FALSE.
conf	Level of confidence 1 - P(type I error).
summarized	Logical; indicate whether raw data or summary stats are to be used.
phat	Estimate of $\pi$ . Required if summarized = TRUE.
fpc	Logical. Indicates whether finite population corrections should be used. If fpc = TRUE then N must be specified. Finite population corrections are not possible for method = "exact" or method = "score".
n	Sample size. Required if summarized = TRUE.
N	Population size. Required if fpc = TRUE.
method	Type of method to be used in confidence interval calculations, method = "agresti.coull" is the default. Other procedures include method = "asymptotic" which provides the conventional normal (Wald) approximation, method = "score", method = "LR", and method = "exact" (see <b>Details</b> below). Partial names can be used. The "exact" method cannot be implemented if summarized=TRUE.
plot	Logical. Should likelihood ratio plot be created with estimate from method = "LR".

**Details**

For the binomial distribution, the parameter of interest is the probability of success,  $\pi$ . ML estimators for the parameter,  $\pi$ , and its standard deviation,  $\sigma_\pi$  are:

$$\hat{\pi} = \frac{x}{n},$$

$$\hat{\sigma}_{\hat{\pi}} = \sqrt{\frac{\hat{\pi}(1 - \hat{\pi})}{n}}$$

where  $x$  is the number of successes and  $n$  is the number of observations.

Because the sampling distribution of any ML estimator is asymptotically normal, an "asymptotic" 100(1 -  $\alpha$ )% confidence interval for  $\pi$  is found using:

$$\hat{\pi} \pm z_{1-(\alpha/2)} \hat{\sigma}_{\hat{\pi}}.$$

This method has also been called the Wald confidence interval.

These estimators can create extremely inaccurate confidence intervals, particularly for small sample sizes or when  $\pi$  is near 0 or 1 (Agresti 2012). A better method is to invert the Wald binomial test statistic and vary values for  $\pi_0$  in the test statistic numerator and standard error. The interval consists of values of  $\pi_0$  in which result in a failure to reject null at  $\alpha$ . Bounds can be obtained by finding the roots of a quadratic expansion of the binomial likelihood function (See Agresti 2012). This has been called a "score" confidence interval (Agresti 2012). An simple approximation to this method

can be obtained by adding  $z_{1-(\alpha/2)}$  ( $\approx 2$  for  $\alpha = 0.05$ ) to the number of successes and failures (Agresti and Coull 1998). The resulting Agresti-Coull estimators for  $\pi$  and  $\sigma_{\hat{\pi}}$  are:

$$\hat{\pi} = \frac{x + z^2/2}{n + z^2},$$

$$\hat{\sigma}_{\hat{\pi}} = \sqrt{\frac{\hat{\pi}(1 - \hat{\pi})}{n + z^2}}.$$

where  $z$  is the standard normal inverse cdf at probability  $1 - \alpha/2$ .

As above, the  $100(1 - \alpha)\%$  confidence interval for the binomial parameter  $\pi$  is found using:

$$\hat{\pi} \pm z_{1-(\alpha/2)} \hat{\sigma}_{\hat{\pi}}.$$

The likelihood ratio method `method = "LR"` finds points in the binomial log-likelihood function where the difference between the maximum likelihood and likelihood function is closest to  $\chi_1^2(1 - \alpha)/2$  for support given in  $\pi_0$ . As support the function uses `seq(0.00001, 0.99999, by = 0.00001)`.

The "exact" method of Clopper and Pearson (1934) is bounded at the nominal limits, but actual coverage may be well below this level, particularly when  $n$  is small and  $\pi$  is near 0 or 1.

Agresti (2012) recommends the Agresti-Coull method over the normal approximation, the score method over the Agresti-Coull method, and the likelihood ratio method over all others. The Clopper Pearson has been repeatedly criticized as being too conservative (Agresti and Coull 2012).

## Value

Returns a list of `class = "ci"`.

<code>pi.hat</code>	Estimate for $\pi$ .
<code>S.p.hat</code>	Estimate for $\sigma_{\hat{\pi}}$ .
<code>margin</code>	Confidence margin.
<code>ci</code>	Confidence interval.

## Note

This function contains only a few of the many methods that have been proposed for confidence interval estimation for  $\pi$ .

## Author(s)

Ken Aho. thanks to Simon Thelwall for finding an error with summarized data under `fpc`.

## References

- Agresti, A. (2012) *Categorical Data Analysis, 3rd edition*. New York. Wiley.
- Agresti, A., and Coull, B. A. (1998) Approximate is better than 'exact' for interval estimation of binomial proportions. *The American Statistician*. 52: 119-126.
- Clopper, C. and Pearson, S. (1934) The use of confidence or fiducial limits illustrated in the case of the Binomial. *Biometrika* 26: 404-413.

Ott, R. L., and Longnecker, M. T. (2004) *A First Course in Statistical Methods*. Thompson.

Wilson, E. B.(1927) Probable inference, the law of succession, and statistical inference. *Journal of the American Statistical Association* 22: 209-212.

### See Also

[ci.mu.z](#)

### Examples

```
#In 2001, it was estimated that 56,200 Americans would be diagnosed with
# non-Hodgkin's lymphoma and that 26,300 would die from it (Cernan et al. 2002).
# Here we find the 95% confidence interval for the probability of diagnosis, pi.

ci.p(c(rep(0, 56200-26300),rep(1,26300))) # Agresti-Coull
ci.p(c(rep(0, 56200-26300),rep(1,26300)), method = "LR") # Likelihood Ratio

# summarized = TRUE
n = 56200
x = 26300
phat = x/n

ci.p(summarized = TRUE, phat = phat, n = n) # Agresti-Coull

# Use 2001 US population size as N
N <- 285 * 10^6
ci.p(c(rep(0, 56200-26300),rep(1,26300)), fpc = TRUE, N = N) # Agresti-Coull
ci.p(summarized = TRUE, phat = phat, n = n, N = N, fpc = TRUE) # Agresti-Coull
```

---

ci.prat

*Confidence intervals for the ratio of binomial and multinomial proportions*

---

### Description

A number of methods have been developed for obtaining confidence intervals for the ratio of two binomial proportions. These include the Wald/Katz-log method (Katz et al. 1978), adjusted-log (Walter 1975, Pettigrew et al. 1986), Koopman asymptotic score (Koopman 1984), Inverse hyperbolic sine transformation (Newman 2001), the Bailey method (Bailey (1987), and the Noether (1957) procedure. Koopman results are found iteratively for most intervals using root finding.

### Usage

```
ci.prat(y1, n1, y2, n2, conf = 0.95, method = "katz.log",
bonf = FALSE, tol = .Machine$double.eps^0.25, R = 1000, r = length(y1))
```

**Arguments**

y1	The ratio numerator number of successes. A scalar or vector.
n1	The ratio numerator number of trials. A scalar or vector of length(y1)
y2	The ratio denominator number of successes. A scalar or vector of length(y1)
n2	The ratio denominator number of trials. A scalar or vector of length(y1)
conf	The level of confidence, i.e. $1 - P(\text{type I error})$ .
method	Confidence interval method. One of "adj. log", "bailey", "boot", "katz.log", "koopman", "sinh-1" or "noether". Partial distinct names can be used.
bonf	Logical, indicating whether or not Bonferroni corrections should be applied for simultaneous inference if y1, y2, n1 and n2 are vectors.
tol	The desired accuracy (convergence tolerance) for the iterative root finding procedure when finding Koopman intervals. The default is taken to be the smallest positive floating-point number of the workstation implementing the function, raised to the 0.25 power, and will normally be approximately 0.0001.
R	If method "boot" is chosen, the number of bootstrap iterations.
r	The number of ratios to which family-wise inferences are being made. Assumed to be length(y1).

**Details**

Let  $Y_1$  and  $Y_2$  be multinomial random variables with parameters  $n_1, \pi_{1i}$ , and  $n_2, \pi_{2i}$ , respectively; where  $i = \{1, 2, 3, \dots, r\}$ . This encompasses the binomial case in which  $r = 1$ . We define the true selection ratio for the  $i$ th resource of  $r$  total resources to be:

$$\theta_i = \frac{\pi_{1i}}{\pi_{2i}}$$

where  $\pi_{1i}$  and  $\pi_{2i}$  represent the proportional use and availability of the  $i$ th resource, respectively. Note that if  $r = 1$  the selection ratio becomes relative risk. The maximum likelihood estimators for  $\pi_{1i}$  and  $\pi_{2i}$  are the sample proportions:

$$\hat{\pi}_{1i} = \frac{y_{1i}}{n_1},$$

and

$$\hat{\pi}_{2i} = \frac{y_{2i}}{n_2}$$

where  $y_{1i}$  and  $y_{2i}$  are the observed counts for use and availability for the  $i$ th resource. The estimator for  $\theta_i$  is:

$$\hat{\theta}_i = \frac{\hat{\pi}_{1i}}{\hat{\pi}_{2i}}.$$

Method	Algorithm
Katz-log	$\hat{\theta}_i \times \exp(\pm z_1 - \alpha/2\hat{\sigma}_W)$ ,



	where $\hat{\sigma}_W^2 = \frac{(1-\hat{\pi}_{1i})}{\hat{\pi}_{1i}n_1} + \frac{(1-\hat{\pi}_{2i})}{\hat{\pi}_{2i}n_2}$ .
Adjusted-log	$\hat{\theta}_{Ai} \times \exp(\pm z_1 - \alpha/2\hat{\sigma}_A)$ , where $\hat{\theta}_{Ai} = \frac{y_{1i}+0.5/n_1+0.5}{y_{2i}+0.5/n_2+0.5}$ , $\hat{\sigma}_A^2 = \frac{1}{y_1+0.5} - \frac{1}{n_1+0.5} + \frac{1}{y_2+0.5} - \frac{1}{n_2+0.5}$ .
Bailey	$\hat{\theta}_i \left[ \frac{1 \pm z_1 - (\alpha/2)(\hat{\pi}'_{1i}/y_{1i} + \hat{\pi}'_{2i}/y_{2i} - z_1 - (\alpha/2)^2 \hat{\pi}'_{1i} \hat{\pi}'_{2i} / 9y_{1i}y_{2i})^{1/2} / 3}{1 - z_1 - (\alpha/2)^2 \hat{\pi}'_{2i} / 9y_{2i}} \right]^3$ , where $\hat{\pi}'_{1i} = 1 - \hat{\pi}_{1i}$ , and $\hat{\pi}'_{2i} = 1 - \hat{\pi}_{2i}$ .
Inv. hyperbolic sine	$\ln(\hat{\theta}_i) \pm \left[ 2 \sinh^{-1} \left( \frac{z(1-\alpha/2)}{2} \sqrt{\frac{1}{y_{1i}} - \frac{1}{n_1} + \frac{1}{y_{2i}} - \frac{1}{n_2}} \right) \right]$ ,
Koopman	Find $X^2(\theta_0) = \chi_1^2(1 - \alpha)$ , where $\tilde{\pi}_{1i} = \frac{\theta_0(n_1+y_{2i})+y_{1i}+n_2 - \{[\theta_0(n_1+y_{2i})+y_{1i}+n_2]^2 - 4\theta_0(n_1+n_2)(y_{1i}+y_{2i})\}^{0.5}}{2(n_1+n_2)}$ , $\tilde{\pi}_{2i} = \frac{\tilde{\pi}_{1i}}{\theta_0}$ , and $X^2(\theta_0) = \frac{(y_{1i}-n_1\tilde{\pi}_{1i})^2}{n_1\tilde{\pi}_{1i}(1-\tilde{\pi}_{1i})} \left\{ 1 + \frac{n_1(\theta_0-\tilde{\pi}_{1i})}{n_2(1-\tilde{\pi}_{1i})} \right\}$ .
Noether	$\hat{\theta}_i \pm z_1 - \alpha/2\hat{\sigma}_N$ , where $\hat{\sigma}_N^2 = \hat{\theta}_i^2 \left( \frac{1}{y_{1i}} - \frac{1}{n_1} + \frac{1}{y_{2i}} - \frac{1}{n_2} \right)$ .

Exception handling strategies are generally necessary in the cases  $y_1 = 0$ ,  $n_1 = y_1$ ,  $y_2 = 0$ , and  $n_2 = y_2$  (see Aho and Bowyer 2015).

The bootstrap method currently employs percentile confidence intervals.

## Value

Returns a list of class = "ci". Default output is a matrix with the point and interval estimate.

## Author(s)

Ken Aho

## References

- Agresti, A., Min, Y. (2001) On small-sample confidence intervals for parameters in discrete distributions. *Biometrics* 57: 963-97.
- Aho, K., and Bowyer, T. 2015. Confidence intervals for ratios of proportions: implications for selection ratios. *Methods in Ecology and Evolution* 6: 121-132.
- Bailey, B.J.R. (1987) Confidence limits to the risk ratio. *Biometrics* 43(1): 201-205.
- Katz, D., Baptista, J., Azen, S. P., and Pike, M. C. (1978) Obtaining confidence intervals for the risk ratio in cohort studies. *Biometrics* 34: 469-474
- Koopman, P. A. R. (1984) Confidence intervals for the ratio of two binomial proportions. *Biometrics* 40:513-517.
- Manly, B. F., McDonald, L. L., Thomas, D. L., McDonald, T. L. and Erickson, W.P. (2002) *Resource Selection by Animals: Statistical Design and Analysis for Field Studies*. 2nd edn. Kluwer, New York, NY

Newcombe, R. G. (2001) Logit confidence intervals and the inverse sinh transformation. *The American Statistician* 55: 200-202.

Pettigrew H. M., Gart, J. J., Thomas, D. G. (1986) The bias and higher cumulants of the logarithm of a binomial variate. *Biometrika* 73(2): 425-435.

Walter, S. D. (1975) The distribution of Levins measure of attributable risk. *Biometrika* 62(2): 371-374.

### See Also

[ci.p](#), [ci.prat.ak](#)

### Examples

```
# From Koopman (1984)
ci.prat(y1 = 36, n1 = 40, y2 = 16, n2 = 80, method = "katz")
ci.prat(y1 = 36, n1 = 40, y2 = 16, n2 = 80, method = "koop")
```

---

ci.prat.ak	<i>Confidence intervals for ratios of proportions when the denominator is known</i>
------------	---

---

### Description

It is increasingly possible that resource availabilities on a landscape will be known. For instance, in remotely sensed imagery with sub-meter resolution, the areal coverage of resources can be quantified to a high degree of precision, at even large spatial scales. Included in this function are six methods for computation of confidence intervals for a true ratio of proportions when the denominator proportion is known. The first (adjusted-Wald) results from the variance of the estimator  $\hat{\sigma}_{\hat{\pi}}$  after multiplication by a constant. Similarly, the second method (Agresti-Coull-adjusted) adjusts the variance of the estimator  $\hat{\sigma}_{\hat{\pi}_{AC}}$ , where  $\hat{\pi}_{AC} = (y + 2)/(n + 4)$ . The third method (fixed-log) is based on delta derivations of the logged ratio. The fourth method is Bayesian and based on the beta posterior distribution derived from a binomial likelihood function and a beta prior distribution. The fifth procedure is an older method based on Noether (1959). Sixth, bootstrapping methods can also be implemented.

### Usage

```
ci.prat.ak(y1, n1, pi2 = NULL, method = "ac", conf = 0.95, bonf = FALSE,
bootCI.method = "perc", R = 1000, sigma.t = NULL, r = length(y1), gamma.hyper = 1,
beta.hyper = 1)
```

### Arguments

y1	The ratio numerator number of successes. A scalar or vector.
n1	The ratio numerator number of trials. A scalar or vector of length(y1)
pi2	The denominator proportion. A scalar or vector of length(y1)

method	One of "ac", "wald", "noether-fixed", "boot", "fixed-log" or "bayes" for the Agresti-Coull-adjusted, adjusted Wald, noether-fixed, bootstrapping, fixed-log and Bayes-beta, methods, respectively. Partial distinct names can be used.
conf	The level of confidence, i.e. $1 - P(\text{type I error})$ .
bonf	Logical, indicating whether or not Bonferroni corrections should be applied for simultaneous inference if $y_1$ , $y_2$ , $n_1$ and $n_2$ are vectors.
bootCI.method	If method = "boot" the type of bootstrap confidence interval to calculate. One of "norm", "basic", "perc", "BCa", or "student". See <a href="#">ci.boot</a> for more information.
R	If method = "boot" the number of bootstrap samples to take. See <a href="#">ci.boot</a> for more information.
sigma.t	If method = "boot" and bootCI.method = "student" a vector of standard errors in association with studentized intervals. See <a href="#">ci.boot</a> for more information.
r	The number of ratios to which family-wise inferences are being made. Assumed to be $\text{length}(y_1)$ .
gamma.hyper	If method = "bayes". A scalar or vector. Value(s) for the first hyperparameter for the beta prior distribution.
beta.hyper	If method = "bayes". A scalar or vector. Value(s) for the second hyperparameter for the beta prior distribution.

## Details

Koopman et al. (1984) suggested methods for handling extreme cases of  $y_1$ ,  $n_1$ ,  $y_2$ , and  $n_2$  (see below). These are applied through exception handling here (see Aho and Bowyer 2015).

Let  $Y_1$  and  $Y_2$  be multinomial random variables with parameters  $n_1, \pi_{1i}$ , and  $n_2, \pi_{2i}$ , respectively; where  $i = \{1, 2, 3, \dots, r\}$ . This encompasses the binomial case in which  $r = 1$ . We define the true selection ratio for the  $i$ th resource of  $r$  total resources to be:

$$\theta_i = \frac{\pi_{1i}}{\pi_{2i}}$$

where  $\pi_{1i}$  and  $\pi_{2i}$  represent the proportional use and availability of the  $i$ th resource, respectively. If  $r = 1$  the selection ratio becomes relative risk. The maximum likelihood estimators for  $\pi_{1i}$  and  $\pi_{2i}$  are the sample proportions:

$$\hat{\pi}_{1i} = \frac{y_{1i}}{n_1},$$

and

$$\hat{\pi}_{2i} = \frac{y_{2i}}{n_2}$$

where  $y_{1i}$  and  $y_{2i}$  are the observed counts for use and availability for the  $i$ th resource. If  $\pi_{2i}$ s are known, the estimator for  $\theta_i$  is:

$$\hat{\theta}_i = \frac{\hat{\pi}_{1i}}{\pi_{2i}}.$$

The function `ci.prat.ak` assumes that selection ratios are being specified (although other applications are certainly possible). Therefore it assume that  $y_{1i}$  must be greater than 0 if  $\pi_{2i} = 1$ , and assumes that  $y_{1i}$  must = 0 if  $\pi_{2i} = 0$ . Violation of these conditions will produce a warning message.

Method	Algorithm
Agresti Coull-Adjusted	$\hat{\theta}_{ACi} \pm z_{1-(\alpha/2)} \sqrt{\hat{\pi}_{AC1i}(1 - \hat{\pi}_{AC1i})/(n_1 + 4)\hat{\pi}_{AC1i}\pi_{2i}^2}$ , where $\hat{\pi}_{AC1i} = \frac{y_1 + z^2/2}{n_1 + z^2}$ , and $\hat{\theta}_{ACi} = \frac{\hat{\pi}_{AC1i}}{\pi_{2i}}$ , where $z$ is the standard normal inverse cdf at probability $1 - \alpha/2$ ( $\approx 2$ when $\alpha = 0.05$ ).
Bayes-beta	$(\frac{X_{\alpha/2}}{\pi_{2i}}, \frac{X_{1-(\alpha/2)}}{\pi_{2i}})$ , where $X \sim BETA(y_{1i} + \gamma_i, n_1 + \beta - y_{1i})$ .
Fixed-log	$\hat{\theta}_i \times \exp(\pm z_{1-\alpha/2} \hat{\sigma}_F)$ , where $\hat{\sigma}_F^2 = (1 - \hat{\pi}_{1i})/\hat{\pi}_{1i}n_1$ .
Noether-fixed	$\frac{\hat{\pi}_{1i}/\pi_2}{1 + z_{1-(\alpha/2)}^2} \pm \frac{z_{1-(\alpha/2)}^2}{2y_{1i}} \pm z_{1-(\alpha/2)}^2 \sqrt{\hat{\sigma}_{NF}^2 + \frac{z_{1-(\alpha/2)}^2}{4y_{1i}^2}}$ , where $\hat{\sigma}_{NF}^2 = \frac{1 - \hat{\pi}_{1i}}{n_1 \hat{\pi}_{1i}}$ .
Wald-adjusted	$\hat{\theta}_i \pm z_{1-(\alpha/2)} \sqrt{\hat{\pi}_{1i}(1 - \hat{\pi}_{1i})/n_1 \hat{\pi}_{1i} \pi_{2i}^2}$ .

### Value

Returns a list of `class = "ci"`. Default output is a matrix with the point and interval estimate.

### Author(s)

Ken Aho

### References

Aho, K., and Bowyer, T. 2015. Confidence intervals for ratios of proportions: implications for selection ratios. *Methods in Ecology and Evolution* 6: 121-132.

### See Also

[ci.prat](#), [ci.p](#)

### Examples

```
ci.prat.ak(3,4,.5)
```

---

ci.sigma	<i>Confidence interval for sigma squared.</i>
----------	---

---

**Description**

The function calculates confidence intervals for  $\sigma^2$ . We assume that the parent population is normal.

**Usage**

```
ci.sigma(data, conf = 0.95, S.sq = NULL, n = NULL, summarized = FALSE)
```

**Arguments**

data	A vector of quantitative data. Required if summarized=FALSE.
conf	Level of confidence. $1 - P(\text{type I error})$ .
S.sq	Sample variance, required if summarized=TRUE.
n	Sample size, required if summarized=TRUE.
summarized	Logical. If summarized=TRUE then the user must supply S.sq and n

**Value**

Returns a list of class = "ci". Default printed results are the point estimate and confidence bounds. Other objects are invisible.

**Author(s)**

Ken Aho

**References**

Bain, L. J., and M. Engelhardt. 1992. *Introduction to Probability and Mathematical Statistics*. Duxbury press. Belmont, CA, USA.

**See Also**

[ci.mu.z](#)

**Examples**

```
ci.sigma(rnorm(20))
```

---

ci.strat

*Confidence intervals for stratified random samples.*


---

### Description

A statistical estimate along with its associated confidence interval can be considered to be an inferential statement about the sampled population. However this statement will only be correct if the method of sampling is considered in the computations of standard errors. The function `ci.strat` provides appropriate computations given stratified random sampling.

### Usage

```
ci.strat(data, strat, N.h, conf = 0.95, summarized = FALSE, use.t = FALSE,
n.h = NULL, x.bar.h = NULL, var.h = NULL)
```

### Arguments

<code>data</code>	A vector of quantitative data. Required if <code>summarized=FALSE</code> .
<code>strat</code>	A vector describing strata.
<code>N.h</code>	A vector describing the number of experimental units for each of the $k$ strata.
<code>conf</code>	Level of confidence; $1 - P(\text{type I error})$ .
<code>summarized</code>	Logical. Indicates whether summarized data are to be used.
<code>use.t</code>	Logical. Indicates whether $t$ or $z$ confidence intervals should be built.
<code>n.h</code>	A vector indicating the number of experimental units sampled in each of the $k$ strata. Required if <code>summarized=TRUE</code> .
<code>x.bar.h</code>	A vector containing the sample means for each of the $k$ strata. Required if <code>summarized=TRUE</code> .
<code>var.h</code>	A vector containing the sample variances for each of the $k$ strata. Required if <code>summarized=TRUE</code> .

### Details

the conventional formula for the sample standard error assumes simple random sampling. There are two other general types of sampling designs: stratified random sampling and cluster sampling. Since cluster sampling is generally used for surveys involving human demographics we will only describe corrections for stratified random sampling here. For more information on sample standard error adjustments for cluster sampling see Lohr (1999).

For a stratified random sampling design let  $N$  be the known total number of units in the defined population of interest, and assume that the population can be logically divided into  $k$  strata;  $N = N_1 + N_2 + N_3 + \dots + N_k$  (i.e. we are assuming that we know both the total population size, and the population size of each stratum). We sample each of the  $k$  strata with  $n_h$  observations;  $h = 1, 2, \dots, k$ .

We estimate the variance in the  $h$ th stratum as:

$$S_h^2 = \frac{1}{n_h - 1} \sum_{i=1}^{n_h} (X_{hi} - \bar{X}_h)^2$$

where  $X_{hi}$  is the  $i$ th observation from the  $h$ th strata and  $\bar{X}_h$  is the  $h$ th sample mean. We estimate the true population total,  $T$ , with:

$$\hat{T} = \sum_{h=1}^k N_h \bar{X}_h$$

We estimate the population mean,  $\mu$ , with:

$$\bar{X}_{str} = \frac{\hat{T}}{N}$$

An unbiased estimator for the standard error of  $\bar{X}_{str}$  is:

$$S_{\bar{X}_{str}} = \sqrt{\sum_{h=1}^k \left(1 - \frac{n_h}{N}\right) \left(\frac{N_h}{N}\right)^2 \left(\frac{S_h^2}{n_h}\right)}$$

The standard error of  $\hat{T}$  is also of interest. Here is an unbiased estimator:

$$S_{\hat{T}} = \sqrt{\sum_{h=1}^k \left(1 - \frac{n_h}{N}\right) N_h^2 \left(\frac{S_h^2}{n_h}\right)}$$

Note that these standard errors have both a finite population correction and adjustments for stratification built into them. Assuming that sample sizes within each stratum are large or that the sampling design has a large number of strata, a  $100(1 - \alpha)$  percent confidence interval for  $\mu$  and  $T$  can be constructed using:

$$\begin{aligned} \bar{X}_{str} \pm z_{1-\alpha/2} S_{\bar{X}_{str}} \\ \hat{T} \pm z_{1-\alpha/2} S_{\hat{T}} \end{aligned}$$

In situations where sample sizes or the number of strata are small, a  $t(n - k)$  distribution can (and should) be used for calculation of confidence intervals, where  $n = n_1 + n_2 + \dots + n_k$ .

### Value

Returns a list with two items:

strat.summary    A matrix with columns: N.h, n.h, x.bar.h and var.h  
 CI                Confidence intervals for  $\mu$  and  $T$

### Author(s)

Ken Aho

## References

- Lohr, S. L. (1999) *Sampling: Design and Analysis*. Duxbury Press. Pacific Grove, USA.
- Siniff, D. B., and Skoog, R. O. (1964) Aerial censusing of caribou using stratified random sampling. *Journal of Wildlife Management* 28: 391-401.

## See Also

[ci.mu.z](#)

## Examples

```
#Data from Siniff and Skoog (1964)
Caribou<-data.frame(Stratum=c("A", "B", "C", "D", "E", "F"), N.h=c(400, 30, 61, 18, 70, 120),
n.h=c(98, 10, 37, 6, 39, 21), x.bar.h=c(24.1, 25.6, 267.6, 179, 293.7, 33.2),
var.h=c(5575, 4064, 347556, 22798, 123578, 9795))
attach(Caribou)
ci.strat(data, strat=Stratum, N.h=N.h, conf=.95, summarized=TRUE, use.t=FALSE, n.h=n.h,
x.bar.h=x.bar.h, var.h=var.h)
```

---

cliff.env

*Environmental data for the community dataset cliff.sp*

---

## Description

The data here are a subset of a dataset collected by Aho (2006) which describe the distribution of communities of lichens and vascular and avascular plant species on montane cliffs in Northeast Yellowstone National Park. Of particular interest was whether substrate (limestone or andesitic conglomerate) or water supply influenced community composition.

## Usage

```
data(cliff.env)
```

## Format

This data frame contains the following columns:

sub a factor with 2 levels "Andesite" and "Lime" describing substrate type.

water a factor with 3 levels "W" "I" "D" indicating wet, intermediate, or dry conditions.

## Details

Two categorical environmental variables are described for 54 sites. sub describes the substrate; there are two levels: "Andesite" and "Lime". water describes distance of samples from waterfalls which drain the cliff faces; there are three levels "W" indicating wet, "I" indicating intermediate, and "D" indicating dry.



**Source**

Aho, K.(2006) *Alpine Ecology and Subalpine Cliff Ecology in the Northern Rocky Mountains*. Doctoral dissertation, Montana State University, 458 pgs.

---

 cliff.sp

*Yellowstone NP cliff community data*


---

**Description**

A subset of a dataset collected by Aho (2006) which describes the distribution of communities of lichens and vascular and avascular plant species on montane cliffs in Northeast Yellowstone National Park. Of particular interest was whether substrate (limestone or andesitic conglomerate) or water supply influenced community composition.

**Usage**

```
data(cliff.sp)
```

**Details**

Responses are average counts from two 10 x 10 point frames at 54 sites. Abundance data are for eleven species, 9 lichens, 3 mosses, and 2 vascular plants. Data were gathered in the summer of 2004 on two andesitic/volcanic peaks (Barronette and Abiathar) with sedimentary layers at lower elevations.

**Source**

Aho, K.(2006) *Alpine Ecology and Subalpine Cliff Ecology in the Northern Rocky Mountains*. Doctoral dissertation, Montana State University, 458 pgs.

---

 concrete

*Concrete strength dataset for data mining*


---

**Description**

The actual concrete compressive strength (MPa) for a given mixture under a specific age (days) was determined from laboratory assays. Data are in raw form (not scaled).

**Usage**

```
data("concrete")
```

### Format

A data frame with 1030 observations on the following 9 variables.

X1 kg of cement in a m<sup>3</sup> mixture.

X2 kg of blast furnace slag in a m<sup>3</sup> mixture.

X3 kg of fly ash in a m<sup>3</sup> mixture.

X4 kg of water in a m<sup>3</sup> mixture.

X5 kg of superplasticizer in a m<sup>3</sup> mixture.

X6 kg of coarse aggregate in a m<sup>3</sup> mixture.

X7 kg of fine aggregate in a m<sup>3</sup> mixture.

X8 Age: day(1-365), a numeric vector

Y Concrete compressive strength in MPa, a numeric vector

### Details

The order of variables corresponds to the order in the original data.

### Source

Prof. I-Cheng Yeh Department of Information Management Chung-Hua University, Hsin Chu, Taiwan 30067, R.O.C. e-mail:icyeh@chu.edu.tw TEL:886-3-5186511

### References

Past Usage:

Primary

I-Cheng, Y. (1998) Modeling of strength of high performance concrete using artificial neural networks. *Cement and Concrete Research*, 28(12): 1797-1808 .

Others

I-Cheng, Y. (1998) Modeling concrete strength with augment-neuron networks. *J. of Materials in Civil Engineering, ASCE* 10(4): 263-268.

I-Cheng, Y. (1999) Design of high performance concrete mixture using neural networks. *J. of Computing in Civil Engineering, ASCE* 13 (1): 36-42.

I-Cheng, Y. (2003) Prediction of Strength of Fly Ash and Slag Concrete By The Use of Artificial Neural Networks. *Journal of the Chinese Institute of Civil and Hydraulic Engineering* Vol. 15, No. 4, pp. 659-663 (2003).

I-Cheng, Y. (2003) A mix Proportioning Methodology for Fly Ash and Slag Concrete Using artificial neural networks. *Chung Hua Journal of Science and Engineering* 1(1): 77-84.

I-Cheng, Y. (2006). Analysis of strength of concrete using design of experiments and neural networks. *Journal of Materials in Civil Engineering, ASCE* 18(4): 597-604.

Acknowledgements, Copyright Information, and Availability:

NOTE: Reuse of this database is unlimited with retention of copyright notice for Prof. I-Cheng Yeh.

---

`ConDis.matrix`*Calculation and display of concordant and discordant pairs*

---

**Description**

Calculates whether pairs of observations from two vectors are concordant discordant or neither. These are displayed in the lower diagonal of a symmetric output matrix as 1, -1 or 0.

**Usage**

```
ConDis.matrix(Y1, Y2)
```

**Arguments**

Y1	A vector of quantitative data.
Y2	A vector of quantitative data. Observations are assumed to be paired with respective observations from Y1.

**Details**

Consider all possible combinations of  $(Y_{1i}, Y_{1j})$  and  $(Y_{2i}, Y_{2j})$  where  $1 \leq i < j \leq n$ . A pair is concordant if  $Y_{1i} > Y_{1j}$  and  $Y_{2i} > Y_{2j}$  or if  $Y_{1i} < Y_{1j}$  and  $Y_{2i} < Y_{2j}$ . Conversely, a pair is discordant if  $Y_{1i} < Y_{1j}$  and  $Y_{2i} > Y_{2j}$  or if  $Y_{1i} > Y_{1j}$  and  $Y_{2i} < Y_{2j}$ . This information has a number of important uses including calculation of Kendall's  $\tau$ .

**Value**

A matrix is returned. Elements in the lower triangle indicate whether observations are concordant (element = 1), discordant (element = -1) or neither (element = 0).

**Author(s)**

Ken Aho

**References**

- Hollander, M., and Wolfe, D. A. (1999) *Nonparametric statistical methods*. New York: John Wiley & Sons.
- Liebetrau, A. M. (1983) *Measures of association*. Sage Publications, Newbury Park, CA.
- Sokal, R. R., and Rohlf, F. J. (1995) *Biometry*. W. H. Freeman and Co., New York.

**See Also**

[cor](#)

**Examples**

```
#Crab data from Sokal and Rohlf (1998)
crab<-data.frame(gill.wt=c(159,179,100,45,384,230,100,320,80,220,320,210),
body.wt=c(14.4,15.2,11.3,2.5,22.7,14.9,1.41,15.81,4.19,15.39,17.25,9.52))
attach(crab)
crabm<-ConDis.matrix(gill.wt,body.wt)
crabm
```

---

 corn

*Corn yield data*


---

**Description**

Hoshmand (2006) described a split plot design to test grain yield of corn with respect to corn hybrids (split plots) and nitrogen (in whole plots). The experiment was replicated at two blocks.

**Usage**

```
data(corn)
```

**Format**

A data frame with 40 observations on the following 4 variables.

yield Corn yield in bushels per acre.

hybrid Type of hybrid, P = pioneer, levels were: A632xLH38 LH74xLH51 Mo17xA634 P3732 P3747.

N Nitrogen addition in lbs/acre 0 70 140 210.

block A blocking factor with levels 1 2.

**Source**

Hoshmand, A. R. (2006) *Design of Experiments for Agriculture and the Natural Sciences 2nd Edition*. Chapman and Hall.

---

 crab.weight

*crab gill and body weight data*


---

**Description**

Gill weight and body weight data for 12 striped shore crabs (*Pachygrapsus crassipes*).

**Usage**

```
data(crab.weight)
```

**Format**

A data frame with 12 observations on the following 2 variables.

gill.wt Gill weight in mg

body.wt Body weight in grams

**Source**

Sokal, R. R., and F. J. Rohlf (2012) *Biometry, 4th edition*. W. H. Freeman and Co., New York.

---

crabs	<i>Agresti crabs dataset</i>
-------	------------------------------

---

**Description**

Horseshoe crab satellite counts as a function of crab phenotype.

**Usage**

```
data(crabs)
```

**Format**

A data frame with 173 observations on the following 5 variables.

color A factor with levels 1 = light medium, 2 = medium, 3 = dark medium, 4 = dark.

spine A factor with levels 1 = both good, 2 = one worn or broken, 3 = both worn or broken.

width Crab carapace width in cm.

satell Number of satellites.

weight Crab weight in in kg.

**Source**

Agresti, A. (2012) *An Introduction to Categorical Data Analysis, 3rd edition*. Wiley, New Jersey.

**References**

Brockman, H. J. (1996) Satellite male groups in horseshoe crabs, *Limulus polyphemus*. *Ethology* 102(1) 1-21.

cuckoo

*Tippett cuckoo egg data*

---

**Description**

Part of a dataset detailing cuckoo egg lengths found in other birds nests. Units are millimeters

**Usage**

```
data(cuckoo)
```

**Format**

A data frame with 16 observations on the following 3 variables.

TP Tree pipit

HS Hedge sparrow

RB Robin

**Source**

Tippett, L. H. C. (1952) *The Methods of Statistics, 4th Edition*. Wiley.

---

D.sq

*Mahalanobis distance for two sites using a pooled covariance matrix*

---

**Description**

Allows much easier multivariate comparisons of groups of sites than provided by the function `mahalanobis` in the base library.

**Usage**

```
D.sq(g1, g2)
```

**Arguments**

g1                   Community vector for site 1

g2                   Community vector for site 2

**Author(s)**

Ken Aho

## References

Legendre, P, and L. Legendre (1998) *Numerical Ecology, 2nd English Edition*. Elsevier, Amsterdam, The Netherlands.

## See Also

[mahalanobis](#)

## Examples

```
g1<-matrix(ncol=3,nrow=3,data=c(1,0,3,2,1,3,4,0,2))
g2<-matrix(ncol=3,nrow=3,data=c(1,2,4,5,2,3,4,3,1))
D.sq(g1,g2)$D.sq
```

---

death.penalty

*Florida state death penalty data*

---

## Description

Dataset detailing death penalty 674 homicide trials in the state of Florida from 1976-1987 with respect to verdict, and victim and defendant race. The data were previously used (Agesti 2012) to demonstrate Simpson's Paradox.

## Usage

```
data(death.penalty)
```

## Format

A data frame with 8 observations on the following 4 variables.

count Counts from cross classifications.

verdict Death penalty verdict No Yes.

d.race Defendant's race Black White.

v.race Victims' race Black White.

## Details

A reversal of associations or comparisons may occur as a result of lurking variables or aggregating groups. This is called Simpson's Paradox.

**Source**

Agresti, A. (2012) *Categorical Data Analysis, 3rd edition*. New York. Wiley.

Radelet, M. L., and G. L. Pierce (1991) Choosing those who will die: race and the death penalty in Florida. *Florida Law Review* 43(1):1-34.

Simpson, E. H. (1951) The Interpretation of interaction in contingency tables. *Journal of the Royal Statistical Society Ser. B* 13: 238-241.

---

 deer

---

*Maternal deer data*


---

**Description**

Monteith et al. (2009) examined the maternal life history characteristics of white-tailed deer (*Odocoileus virginianus*) originating from the Black Hills in southwestern South Dakota and from eastern South Dakota. Because litter size and dam size affects offspring weight the investigators used proportional birth mass (dam mass/total litter mass) as a measure of reproductive investment by deer.

**Usage**

`data(deer)`

**Format**

The dataframe contains 6 columns

`Birth.Yr` Year of birth.

`Litter.size` Number of offspring.

`Region` Categorical variable with two factor levels. BH = Black Hills, ER = Eastern Region.

`Dam.weight` Dam weight in kg.

`Total.birth.mass` Mass of litter in kg.

`Prop.mass` Total birth mass divided by dam weight.

**Source**

Monteith, K. L., Schmitz, L. E., Jenks, J. A., Delger, J. A., and R. T. Bowyer. 2009. Growth of male white tailed deer: consequences of maternal effects. *Journal of Mammalogy* 90(3): 651-660.



---

 deer . 296

*Mule deer telemetry data*


---

### Description

Telemetry data for mule deer #296 from the Starkey Experimental Forest in Northeastern Oregon. Data are high resolution (10 minute) radio collar readings from 8/20/2008 to 11/6/2008. Also included are data for nearest neighbor locations of forest/grassland boundaries.

### Usage

```
data(deer . 296)
```

### Format

A data frame with 5423 observations on the following 7 variables.

Time Unit of time measurement used at the Starkey Experimental Forest

X Mule Deer X-coordinate, UTM Easting

Y Mule Deer Y-coordinate, UTM Northing

NEAR\_X Nearest boundary location X coordinate

NEAR\_Y Nearest boundary location Y coordinate

Hab\_Type Type of habitat

NEAR\_ANGLE A numeric vector containing the angle of azimuth to the nearest point on the boundary with respect to a four quadrant system. NE =  $0^\circ$  to  $90^\circ$ , NW is  $> 90^\circ$  and  $\leq 180^\circ$ , SE is  $< 0^\circ$  and  $\leq -90^\circ$  is  $> -90^\circ$  and  $\leq -180^\circ$ .

---

 depression

*Hamilton depression scores before and after drug treatment*


---

### Description

Hollander and Wolfe (1999) presented Hamilton depression scale factor measurements for 9 patients with mixed anxiety and depression. Measurements were taken at a time preceding administration of tranquilizer, and a time after tranquilizer administration.

### Usage

```
data(depression)
```

**Format**

A data frame with 18 observations on the following 3 variables.

subject Experimental subject.

scale Hamilton depression scale score. 0-7 is considered to be normal. Scores of 20 or higher indicate moderate to very severe depression

time A factor with levels post pre indicating before and after tranquilizer treatment.

**Source**

Hollander, M., and D. A. Wolfe. 1999. *Nonparametric Statistical Methods*. New York: John Wiley & Sons.

---

DH.test

*Doornik-Hansen test for multivariate normality.*

---

**Description**

The Doornik-Hansen test for multivariate normality is a powerful alternative to the Shapiro-Wilk test.

**Usage**

```
DH.test(Y, Y.names = NULL)
```

**Arguments**

Y An  $n \times p$  dataframe of dependent variables.

Y.names Names of Y variables; should be a  $1 \times p$  character string.

**Details**

An assumption of multivariate normality is exceedingly difficult to verify. Hypothesis tests tend to be too stringent, and multivariate diagnostic plots only allow viewing of two variables at a time. Univariate normality of course can be verified using normal probability plots. However while marginal non-normality indicates multivariate non-normality, marginal normality does not insure that  $Y$  variables collectively follow a multivariate normal distribution.

The Doornik-Hansen test for multivariate normality (Doornik and Hansen 2008) is based on the skewness and kurtosis of multivariate data that is transformed to insure independence. The DH test is more powerful than the Shapiro-Wilk test for most tested multivariate distributions (Doornik and Hansen 2008). The function `DH.test` also runs the Doornik-Hansen test for both multivariate and univariate normality. The later test follows directly from the work of Bowman and Shenton (1975), Shenton and Bowman (1977) and D'Agostino (1970).

**Value**

Returns a list with two objects.

multi	A dataframe containing multivariate results, i.e. the test statistic, $E$ , the degrees of freedom and the $p$ -value.
comp2	A dataframe with $p$ rows detailing univariate tests. Columns in the dataframe contain the test statistics, degrees of freedom and $P$ -values.

**Note**

As with all inferential normality tests our null hypothesis is that the underlying population is normal, in this case multivariate normal.

**Author(s)**

Ken Aho

**References**

D'Agostino, R. B. (1970). Transformation to normality of the null distribution of  $g_1$ , *Biometrika* 57: 679-681.

Doornik, J.A. and Hansen, H. (2008). An Omnibus test for univariate and multivariate normality. *Oxford Bulletin of Economics and Statistics* 70, 927-939.

Shenton, L. R. and Bowman, K. O. (1977). A bivariate model for the distribution of  $b_1$  and  $b_2$ , *Journal of the American Statistical Association* 72: 206.211.

**See Also**

[shapiro.test](#), [bv.boxplot](#)

**Examples**

```
data(iris)#The ubiquitous multivariate iris data.
DH.test(iris[,1:4],Y.names=names(iris[,1:4]))
```

---

d02

*Dissolved levels in locations above and below a town*

---

**Description**

Dissolved O<sub>2</sub> readings in ppm for 15 random locations above and below a riverside community.

**Usage**

```
data(d02)
```

**Format**

A data frame with 30 observations on the following 2 variables.

o2 Dissolved O<sub>2</sub> levels in ppm.

location River flow location with respect to town. Levels are Above Below.

**Source**

Ott, R. L., and M. T. Longnecker (2004) *A First Course in Statistical Methods*. Thompson.

---

drugs	<i>Contingency data for high school marijuana, alcohol, and cigarette use</i>
-------	---

---

**Description**

Agresti (2012) included a three way contingency table describing cigarette, alcohol, and marijuana use of high school students in Dayton Ohio.

**Usage**

```
data(drugs)
```

**Format**

A data frame with 8 observations on the following 4 variables.

alc Alcohol use. A factor with levels N Y.

cig Cigarette use. A factor with levels N Y.

mari Marijuana use. A factor with levels N Y

count Counts for the cross-classification.

**Source**

Agresti, A. 2012. *Categorical Data Analysis, 3rd edition*. New York. Wiley.

---

e.cancer	<i>Esophageal cancer data modified slightly to create a balanced three-way factorial design</i>
----------	---

---

### Description

Breslow and Day (1980) studied the effect of age, tobacco, and alcohol on esophageal cancer rates at Ile-et-Vilaine, France. Data are altered slightly to make the design balanced, and to allow enough degrees of freedom to perform a fully factorial three way ANOVA.

### Usage

```
data(e.cancer)
```

### Format

The dataset contains four variables:

**age grp.** age group, a factor with four levels: "25-34", "35-44", "45-54", "55-64", and "65-74".

**alcohol** alcohol consumed (g/day).

**tobacco** tobacco consumed (g/day).

**cases** number of esophageal cancer cases.

### Source

Breslow, N. E. and N. E. Day (1980) *Statistical Methods in Cancer Research. 1: The Analysis of Case-Control Studies*. IARC Lyon / Oxford University Press.

---

eff.rbd	<i>Efficiency of a randomized block design compared to a CRD</i>
---------	--

---

### Description

Calculates the RCBD efficiency ratio for a linear model with one main factor and one blocking factor. Values greater than 1 indicate that the RCBD has greater efficiency compared to a CRD.

### Usage

```
eff.rbd(lm)
```

### Arguments

**lm** An object of class `lm`. The blocking factor must be called "block".

**Author(s)**

Ken Aho

**References**

Kutner, M. H., C. J. Nachtsheim, J. Neter, and W. Li (2005) *Applied Linear Statistical Models*. McGraw-Hill Irwin.

---

enzyme

*Enzymatic rate data for the phospholipase protein ExoU*

---

**Description**

The bacterium *Pseudomonas aeruginosa* causes disease in human hosts leading to sepsis and even death in part by secreting lipases (proteins that break down lipids) into cellular environments. The protein ExoU is a phospholipase produce by particularly virulent strains of *P. aeruginosa*. Benson et al. (2009) measured of ExoU enzymatic activity under varying levels of the fluorescent phospholipase substrate PED6.

**Usage**

data(enzyme)

**Format**

A data frame with 10 observations on the following 3 variables.

substrate PED6 concentration (in micromoles).

rate enzymatic rate (nmol of cleaved of PED6 per mg ExoU).

sd standard deviation of rate for each level of substrate.

**Source**

Benson, M. A., Schmalzer, K. M., and D. W. Frank (2009) A sensitive fluorescence-based assay for the detection of ExoU mediated PLA2 activity. *Clin Chim Acta* 411(3-4): 190-197.

---

 ES.May

*May's effective specialization index*


---

### Description

May and Beverton (1990) created the effective specialization index to quantify the degree of specialization of insects with potential host plants.

### Usage

```
ES.May(mat, digs = 3)
```

### Arguments

mat	A symmetric matrix with potential specialist hosts in rows and the number of species specializing on each of the host species in columns (see details below).
digs	The number of significant digits in output.

### Details

The structure of the object `mat` is nonintuitive. In the rows of the matrix are species which can be selected by potential specialists (i.e. hosts). May and Beverton (1990) used four oak species. The columns indicate the degree of specialization of potential specialists. May and Beverton (1990) were interested in the specialization of beetles. The first element (row 1, column 1) in their 4 x 4 matrix contained only beetle species found on host 1. The second element (row 1, column 2) contained the number of beetle species found on host 1 and one other host. The third element (row 1, column 3) contained the number of beetle species found on host 1 and two other hosts. The fourth element (row 1, column 4) contained the number of beetle species occurring on all four hosts.

### Value

Output is a list

`E.S_coefficients`

<code>Nk</code>	The number of distinct specialists.
<code>Pki.matrix</code>	The proportion of potential specialists on the $k$ th host
<code>N.matrix</code>	The raw data.
<code>fk.matrix</code>	
<code>fk.vector</code>	For the $k$ th host, the proportion of species which are effectively specialized.
<code>Nk.vector</code>	The number of species which are effectively specialized on the $k$ th host.

### Author(s)

Ken Aho and Jessica Fultz

## References

May, R. M. and Beverton, R. J. H. (1990) How many species [and discussion]. *Philosophical Transactions: Biological Sciences*. 330 (1257) 293-304.

## Examples

```
#data from May and Beverton (1990)
beetle<-matrix(ncol=4,nrow=4,data=c(5,8,7,8,20,10,9,8,14,15,11,8,15,15,12,8),
byrow=TRUE)
ES.May(beetle)
```

---

exercise.repeated      *Repeated measures data for an exercise experiment.*

---

## Description

Freund et al. (1986) listed data for a longitudinal study of exercise therapies. The data were analyzed using AR1 covariance matrices in mixed models by Fitzmaurice et al. (2004). In the study 37 patients were randomly assigned to one of two weightlifting programs. In the first program (TRT 1), repetitions with weights were increased as subjects became stronger. In the second program (TRT 2), the number of repetitions was fixed but weights were increased as subjects became stronger. An index measuring strength was created and recorded at day 0, 2, 4, 6, 8, 10, and 12.

## Usage

```
data(exercise.repeated)
```

## Format

The dataframe contains a repeated measures dataset describing the strength of 37 subjects with respect to two weightlifting programs. There are four columns:

**ID** Subject ID.

**TRT** The type of weightlifting treatment (a factor with two levels, 1 and 2).

**strength** A strength index.

**day** The day that strength was measured on a subject, measured from the start of the experiment.

## Source

Fitzmaurice, G. M., Laird, N. M, and Waird, J. H. (2004) *Applied Longitudinal Analysis*. Wiley.



---

facebook

*Facebook performance metrics for data mining and machine learning*

---

### **Description**

These data concern posts published during the year 2014 on the Facebook page of a popular cosmetics brand. The data here are 500 of the 790 rows and part of the features analyzed by Moro et al. (2016). The remaining data points were omitted due to confidentiality issues.

### **Usage**

`data(facebook)`

### **Format**

A data frame with 500 observations on the following 19 variables.

- X1 Total number of likes of the page containing a post.
- X2 Type of content; a factor with levels Link, Photo, Status, and Video.
- X3 Manual content category; a factor with levels: action (special offers and contests), product (direct advertisement, explicit brand content), and inspiration (non-explicit brand related content).
- X4 Month the post was posted.
- X5 Weekday the post was published.
- X6 Hour the post was posted
- X7 An binary variable indicating if the company paid to Facebook for advertising.
- Y1 Lifetime post total reach: the number of people who saw a page post.
- Y2 Lifetime number of total impressions: the number of times a post from a page is displayed, whether the post is clicked or not.
- Y3 Lifetime engaged users: the total number of people who clicked anywhere in a post (unique users).
- Y4 Lifetime number of post consumers: the number of people who clicked anywhere in a post after purchasing something on the page.
- Y5 Lifetime number of post consumptions: the number of clicks anywhere in a post by people after purchasing something on the page.
- Y6 Lifetime number of post impressions by people who have liked the page.
- Y7 Lifetime post reach by people who like the page.
- Y8 Lifetime number of people who have liked the page and engaged with the post.
- Y9 Number of "comments" on the post.
- Y10 Number of "likes" on the post.
- Y11 Number of times the post was "shared."
- Y12 Total interactions: the sum of "likes," "comments," and "shares" of the post.

## References

This dataset is publicly available for research. The details are described in (Moro et al., 2016). Please include this citation if you plan to use this data:

S. Moro, P. Rita, Vala, B. (2016) Predicting social media performance metrics and evaluation of the impact on brand building: A data mining approach. *Journal of Business Research* 69(9): 3341-3351.

---

Fbird

*Frigatebird drumming frequency data*

---

## Description

Male magnificent frigatebirds (*Fregata magnificens*) have an enlarged red throat pouch that has probably evolved as the result of sexual selection. During courtship displays males attract females by displaying this pouch and using it to make a drumming sound. Madsen et al. (2004) noted that conditions (e.g. oblique viewing angles) often limit females' ability to appraise pouch size exactly. Since females choose mates based on pouch size, a question of interest is whether females could use the pitch of the pouch drumming as an indicator of pouch size. Madsen et al. (2004) estimated the pouch volume and fundamental drumming frequency for forty males at Isla Isabel in Nayarit Mexico. Eighteen of these observations are in this dataset.

## Usage

```
data(Fbird)
```

## Format

The dataframe contains two variables:

vol Pouch volume (in cm<sup>3</sup>).

freq Frequency of drumming (in Hz)

## Source

Madsen, V., Balsby, T.J.S., Dabelsteen, T., and J.L. Osorno (2004) Bimodal signaling of a sexually selected trait: gular pouch drumming in the magnificent frigatebird. *Condor* 106: 156-160.

---

fire	<i>Fire data from Yellowstone National Park</i>
------	---

---

**Description**

Fires from 1988 constituted the largest conflagration in the history of Yellowstone National Park. This dataframe lists burned areas for ten Yellowstone stream catchments (Robinson et al. 1994).

**Usage**

```
data(fire)
```

**Format**

A data frame with 10 observations on the following 2 variables.

fire Burn area in, in hectares<sup>2</sup>.

stream A factor with levels Blacktail Cache EF.Blacktail Fairy Hellroaring Iron.Springs  
Pebble Rose SF.Cache Twin

**Source**

Robinson, C. T., Minshall, G. W., and S. R. Rushforth (1994) The effects of the 1988 wildfires on diatom assemblages in the streams of Yellowstone National Park. Technical Report NPS/NRYELL/NRTR-93/XX.

---

fly.sex	<i>Fly sex and longevity</i>
---------	------------------------------

---

**Description**

Partridge and Farquar (1981) studied the effect of the number of mating partners on the longevity of fruit flies. Five different mating treatments were applied to single male fruit flies. As a concomitant variable thorax length was measured.

**Usage**

```
data(fly.sex)
```

**Format**

A data frame with 125 observations on the following 3 variables.

treatment a factor with levels 1 = One virgin female per day, 2 = eight virgin females per day, 3 = a control group with one newly inseminated female per day, 4 = a control group with eight newly inseminated females per day, and 5 a control group with no added females.

longevity Age in days.

thorax Thorax length in mm.

**Source**

Quinn, G. P., and M. J. Keough. 2002. *Experimental Design and Data Analysis for Biologists*. Cambridge University Press.

**References**

Partridge, L., and Farquhar, M. (1981), Sexual activity and the lifespan of male fruit flies, *Nature* 294, 580-581.

---

 frog

---

*Australian frog calls following fire*


---

**Description**

Driscoll and Roberts (1997) examined the impact of fire on the Walpole frog (*Geocrinia lutea*) in catchments in Western Australia by counting the number of calling males in six paired burn and control sites for three years following spring burning in 1991.

**Usage**

```
data(frog)
```

**Format**

A data frame with 18 observations on the following 3 variables.

catchment A factor with levels angove logging newpipe newquinE newquinW oldquinE.

frogs The difference in the number of male frog calls for control - burned sites.

year Year.

**Source**

Quinn, G. P., and M. J. Keough (2002) *Experimental Design and Data Analysis for Biologists*. Cambridge University Press.

**References**

Driscoll, D. A., and J. D. Roberts. 1997. Impact of fuel-reduction burning on the frog *Geocrinia lutea* in southwest Western Australia. *Australian Journal of Ecology* 22:334-339.

---

fruit	<i>Fruit weight data from Littell et al. (2002)</i>
-------	---

---

**Description**

Valencia orange tree fruit weights are measured at harvest with respect to five irrigation treatment applied in eight blocks in a RCBD.

**Usage**

```
data(fruit)
```

**Format**

A data frame with 40 observations on the following 3 variables.

block a factor describing eight blocks

irrig a factor with levels basin flood spray sprinkler trickle

fruitwt a numeric vector

**Source**

Littell, R. C., Stroup, W. W., and R. J. Freund (2002) *SAS for linear models*. John Wiley and Associates.

---

G.mean	<i>Geometric mean</i>
--------	-----------------------

---

**Description**

Calculates the geometric mean.

**Usage**

```
G.mean(x)
```

**Arguments**

x A vector of quantitative data.

**Value**

Returns the geometric mean.

**Author(s)**

Ken Aho

**See Also**

[H.mean](#), [HL.mean](#)

**Examples**

```
x<-c(2,1,4,5,6,2.4,7,2.2,.002,15,17,.001)
G.mean(x)
```

---

g.test

*Likelihood ratio test for tabular data*

---

**Description**

Provides likelihood ratio tests for one way and multiway tables.

**Usage**

```
g.test(y, correct = FALSE, pi.null = NULL)
```

**Arguments**

y	A vector of at least 2 elements, or a matrix. Must contain only non-negative integers.
correct	Logical. Indicating whether Yates correction for continuity should be used.
pi.null	Optional vector or matrix of null proportions. Must sum to one.

**Author(s)**

Ken Aho

**Examples**

```
obs <- c(6022, 2001)
g.test(obs, pi.null = c(0.75, 0.25))
```

---

garments

*Garment Latin square data from Littell et al. (2002)*

---

**Description**

Four materials (A, B, C, D) used in permanent press garments were subjected to a test for shrinkage. The four materials were placed in a heat chamber with with four settings (pos). The test was then conducted in four runs (run).

**Usage**

```
data(garments)
```

**Format**

A data frame with 16 observations on the following 4 variables.

run Test run, a factor with levels 1 2 3 4

pos Heat position, a factor with levels 1 2 3 4

mat Fabric materials, a factor with levels A B C D

shrink Shrinkage measure, a numeric vector

**Source**

Littell, R. C., Stroup, W. W., and R. J. Freund (2002) *SAS for Linear Models*. John Wiley and Associates.

---

Glucose2

*Glucose Levels Following Alcohol Ingestion*

---

**Description**

The Glucose2 data frame has 196 rows and 4 columns.

**Format**

This data frame contains the following columns:

Subject a factor with levels 1 to 7 identifying the subject whose glucose level is measured.

Date a factor with levels 1 2 indicating the occasion in which the experiment was conducted.

Time a numeric vector giving the time since alcohol ingestion (in min/10).

glucose a numeric vector giving the blood glucose level (in mg/dl).

**Details**

Hand and Crowder (Table A.14, pp. 180-181, 1996) describe data on the blood glucose levels measured at 14 time points over 5 hours for 7 volunteers who took alcohol at time 0. The same experiment was repeated on a second date with the same subjects but with a dietary additive used for all subjects.

**Note**

Descriptions and details are from the library `nlme`.

**Source**

Pinheiro, J. C. and Bates, D. M. (2000), *Mixed-Effects Models in S and S-PLUS*, Springer, New York. (Appendix A.10)

Hand, D. and Crowder, M. (1996), *Practical Longitudinal Data Analysis*, Chapman and Hall, London.

---

goats

*Mountain goat data from Yellowstone National Park*

---

**Description**

Mount goat (*Oreamnos americanus*) feces data and soil nutrient data for eight different mountains in the Northern Absarokas in Yellowstone National Park.

**Usage**

```
data(goats)
```

**Format**

The dataframe has 3 columns:

feces feces concentration (Percent occurrence per 0.1, m<sup>2</sup> plot).

N03 Nitrate concentration in ppm.

organic.matter Organic matter concentration (LOI) as a percentage.

**Source**

Aho, K. (2012) *Management of introduced mountain goats in Yellowstone National Park (vegetation analysis along a mountain goat gradient)*. PMIS: 105289. Report prepared for USDA National Park Service. 150 pp.



---

grass

*Agricultural factorial design*

---

### Description

Littell et al. (2006) describe an experiment to distinguish the effects of three seed growing methods on the yield of five turf grass varieties. The seed growing methods were applied to seed from each grass variety. Six pots were planted with each variety  $\times$  method combination. The pots were placed in a growth chamber with uniform conditions and dry matter (in grams) was weighed from above ground clips after four weeks.

### Usage

```
data(grass)
```

### Format

The dataframe has three columns:

yield Refers to grass yield.

method Seed growing method. A factor with three levels: a, b, c.

variety Grass variety. A factor with five levels: 1, 2, 3, 4, 5.

### Source

Littell, R. C., Milliken, G. A., Stroup, W. W., Wolfinger, R. D., and O. Schabenberger (2006) *SAS for mixed models 2nd ed.* SAS press.

---

H.mean

*Harmonic mean*

---

### Description

Calculates the harmonic mean.

### Usage

```
H.mean(x)
```

### Arguments

x                      Vector of quantitative data.

### Value

Returns the harmonic mean.

**Author(s)**

Ken Aho

**See Also**[G.mean](#), [HL.mean](#)**Examples**

```
x<-c(2,1,4,5,6,2.4,7,2.2,.002,15,17,.001)
H.mean(x)
```

heart

*Heart rate data from Milliken and Johnson (2009)***Description**

A repeated measures demonstration dataset from Milliken and Johnson (1999). Heart rate was measured for twenty four subject at four time periods following administration of a treatment. The treatment types were two active heart drugs and a control. One treatment was assigned to each subject. Thus each drug was administered to eight subjects.

**Usage**

```
data(heart)
```

**Format**

A data frame with 96 observations on the following 4 variables.

rate A numeric vector describing heart rate (bpm).

time A factor with levels t1 t2 t3 t4

drug A factor with levels AX23 BWW9 Ctr1

subject A factor describing which subject (in drug) that measurements were made on.

**Source**

Milliken, G. A., and D. E. Johnson (2008) *Analysis of Messy Data: Vol. I. Designed Experiments, 2nd edition*. CRC.

**Examples**

```
## Not run:
#data(heart)
#aov(rate ~ drug * time + Error(subject%in%drug), data = heart)

## End(Not run)
```

---

`HL.mean`*Hodges-Lehman estimator of location*

---

**Description**

Calculates the Hodges-Lehman estimate of location –which is consistent for the true pseudomedian– using Walsh averages (Hollander and Wolfe 1999, pgs. 51-55). If requested, the function also provides confidence intervals for the true pseudomedian. In a symmetric distribution the mean, median, and pseudomedian will be identical.

**Usage**

```
HL.mean(x, conf = NULL, method = "exact")
```

**Arguments**

<code>x</code>	A vector of quantitative data.
<code>conf</code>	A proportion specifying $1 - P(\text{type I error})$ .
<code>method</code>	method for confidence interval calculation. One of "approx", which uses a normal approximation, or "exact", which uses the Wilcoxon sign-rank quantile function (see Hollander and Wolfe 1999).

**Author(s)**

Ken Aho

**References**

Hollander, M., and Wolfe, D. A (1999) *Nonparametric Statistical Methods*. New York: John Wiley & Sons.

**See Also**

[H.mean](#), [G.mean](#)

**Examples**

```
# Hamilton depression scale (Hollander and Wolfe 1999)
x<-c( -0.952, 0.147, -1.022, -0.430, -0.620, -0.590, -0.490, 0.080, -0.010)
HL.mean(x, conf = .96)
```

---

`huber.mu`*Huber M-estimator of location*

---

**Description**

The Huber  $M$ -estimator is a robust high efficiency estimator of location that has probably been under-utilized by biologists. It is based on maximizing the likelihood of a weighting function. This is accomplished using an iterative least squares process. The Newton Raphson algorithm is used here. The function usually converges fairly quickly (< 10 iterations). The function uses the Median Absolute Deviation function, `mad`. Note that if  $MAD = 0$ , then NA is returned.

**Usage**

```
huber.mu(x, c = 1.28, iter = 20, conv = 1e-07)
```

**Arguments**

<code>x</code>	A vector of quantitative data.
<code>c</code>	Stop criterion. The value $c = 1.28$ gives 95% efficiency of the mean given normality.
<code>iter</code>	Maximum number of iterations.
<code>conv</code>	Convergence criterion.

**Value**

Returns Huber's  $M$ -estimator of location.

**Author(s)**

Ken Aho

**References**

Huber, P. J. (2004) *Robust Statistics*. Wiley.

Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

**See Also**

[huber.one.step](#), [huber.NR](#), [mad](#)

**Examples**

```
x <- rnorm(100)
huber.mu(x)
```

---

`huber.NR`*Huber M-estimator iterative least squares algorithm*

---

**Description**

Algorithm for calculating fully iterated or one step Huber  $M$ -estimators of location.

**Usage**

```
huber.NR(x, c = 1.28, iter = 20)
```

**Arguments**

<code>x</code>	A vector of quantitative data
<code>c</code>	Bend criterion. The value $c = 1.28$ gives 95% efficiency of the mean given normality.
<code>iter</code>	Maximum number of iterations

**Details**

The Huber  $M$ -estimator is a robust high efficiency estimator of location that has probably been under-utilized by biologists. It is based on maximizing the likelihood of a weighting function. This is accomplished using an iterative least squares process. The Newton Raphson algorithm is used here. The function usually converges fairly quickly  $< 10$  iterations. The function uses the Median Absolute Deviation function, `mad`. Note that if  $MAD = 0$ , then NA is returned.

**Value**

Returns iterative least squares iterations which converge to Huber's  $M$ -estimator. The first element in the vector is the sample median. The second element is the Huber one-step estimate.

**Author(s)**

Ken Aho

**References**

Huber, P. J. (2004) *Robust Statistics*. Wiley.

Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

**See Also**

[huber.one.step](#), [huber.mu](#), [mad](#)

**Examples**

```
x<-rnorm(100)
huber.NR(x)
```

---

huber.one.step	<i>Huber one step M-estimator</i>
----------------	-----------------------------------

---

**Description**

Returns the first Raphson-Newton iteration of the function `Huber.NR`.

**Usage**

```
huber.one.step(x, c = 1.28)
```

**Arguments**

x	Vector of quantitative data
c	Bend criterion. The value $c = 1.28$ gives 95% efficiency of the mean given normality.

**Details**

The Huber  $M$ -estimator function usually converges fairly quickly, hence the justification of the Huber one step estimator. The function uses the Median Absolute Deviation function, [mad](#). If  $MAD = 0$ , then NA is returned.

**Value**

Returns the Huber one step estimator.

**Author(s)**

Ken Aho

**References**

Huber, P. J. (2004) *Robust Statistics*. Wiley.  
Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

**See Also**

[huber.mu](#), [huber.NR](#), [mad](#)

**Examples**

```
x<-rnorm(100)
huber.one.step(x)
```

---

`illusions`*Visual illusions illustrating human perception errors.*

---

**Description**

In development, currently displays three illusions. Illusion 3 is from Yihui Xie's package **animation**.

**Usage**

```
illusions(ill.no = 1)
```

**Arguments**

`ill.no` Integer in 1:3 describing which illusion number to view.

**Author(s)**

Ken Aho. Illusion 3 uses code from Yihui Xie's package animation.

**Examples**

```
illusions(1)
illusions(2)
illusions(3)
```

---

`ipomopsis`*Ipomopsis fruit yield data*

---

**Description**

The following question is based on data from Crawley (2007). We are interested in the effect of grazing on seed production in the plant scarlet gilia *Ipomopsis aggregata*. Forty plants were allocated to two treatments, grazed and ungrazed. Grazed plants were exposed to rabbits during the first two weeks of stem elongation. They were then protected from subsequent grazing by the erection of a fence and allowed to continue growth. Because initial plant size may influence subsequent fruit production, the diameter of the top of the rootstock was measured before the experiment began. At the end of the experiment, fruit production (dry weight in milligrams) was recorded for each of the forty plants.

**Usage**

```
data(ipomopsis)
```

**Format**

A data frame with 40 observations on the following 3 variables.

root Rootstock diameter in mm

fruit Fruit dry weight in mg

grazing a factor with levels Grazed Ungrazed

**Source**

Website associated with – Crawley, M. J. 2007. *The R book*. Wiley.

---

joint.ci.bonf	<i>Calculates joint confidence intervals for parameters in linear models using a Bonferroni procedure.</i>
---------------	--

---

**Description**

Creates widened confidence intervals to allow joint consideration of parameter confidence intervals.

**Usage**

```
joint.ci.bonf(model, conf = 0.95)
```

**Arguments**

model	A linear model created by <code>lm</code>
conf	level of confidence 1 - $P$ (type I error)

**Details**

As with all Bonferroni-based methods for joint confidence the resulting intervals are exceedingly conservative and thus are prone to type II error.

**Value**

Returns a dataframe with the upper and lower confidence bounds for each parameter in a linear model.

**Author(s)**

Ken Aho

**References**

Kutner, M. H., Nachtsheim, C. J., Neter, J., and W. Li. (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.



**See Also**

[confint](#), [p.adjust](#)

**Examples**

```
Soil.C<-c(13,20,10,11,2,25,30,25,23)
Soil.N<-c(1.2,2,1.5,1,0.3,2,3,2.7,2.5)
Slope<-c(15,14,16,12,10,18,25,24,20)
Aspect<-c(45,120,100,56,5,20,5,15,15)
Y<-as.vector(c(20,30,10,15,5,45,60,55,45))
model<-lm(Y~Soil.C+Soil.N+Slope+Aspect)
joint.ci.bonf(model)
```

---

K

*Soil potassium analyses from 8 laboratories*

---

**Description**

Jacobsen et al. (2002) sent nine "identical" soil samples to eight soil testing laboratories in the Great Plains region of the Central United States over a three year period of time. Among other characteristics the labs were paid to measure soil potassium. A question of interest was whether the labs would produce identical analytical results.

**Usage**

```
data(K)
```

**Format**

A data frame with 72 observations on the following 2 variables.

K Soil K in mg/kg

lab Laboratories, a factor with levels B D E F G H I J

**Source**

Jacobsen, J. S., Lorber, S. H., Schaff, B. E., and C. A. Jones (2002) Variation in soil fertility test results from selected Northern Great Plains laboratories. *Commun. Soil Sci. plant Anal.*, 33(3&4): 303-319.

---

 Kappa

*Calculates kappa statistic and other classification error statistics*


---

**Description**

The kappa statistic, along with user and producer error rates are conventionally used in the remote sensing to describe the effectiveness of ground cover classifications. Since it simultaneously considers both errors of commission and omission, kappa can be considered a more conservative measure of classification accuracy than the percentage of correctly classified items.

**Usage**

```
Kappa(class1, reference)
```

**Arguments**

class1	A vector describing a classification of experimental units.
reference	A vector describing the "correct" classification of the experimental units in class1

**Value**

Returns a list with 4 items

t1_agreement	The percentage of correctly classified items.
user_accuracy	The user accuracy for each category of the classification.
producer_accuracy	The producer accuracy for each category of the classification.
kappa	The kappa statistic.
table	A two way contingency table comparing the user supplied classification to the reference classification.

**Author(s)**

Ken Aho

**References**

Jensen, J. R. (1996) *Introductory digital imagery processing 2nd edition*. Prentice-Hall.

**Examples**

```
reference<-c("hi", "low", "low", "hi", "low", "med", "med")
class1<-c("hi", "hi", "low", "hi", "med", "med", "med")
Kappa(class1, reference)
```

---

km *Kaplan-Meier survivorship.*

---

### Description

Calculates survivorship for individuals in a population over time based on the method of Kaplan-Meier; cf. Pollock et al. (1989).

### Usage

```
km(r, d, var = "0", conf = 0.95, age.seq=seq(1,length(r)),
  ylab = "Survivorship", xlab = "Age class", type = "b",
  plot.km = TRUE, plot.CI = TRUE, ...)
```

### Arguments

r	Numbers of individuals at risk in each age or time class.
d	Vector of the number of deaths in each age or time class.
var	Type of procedure used to calculate variance in confidence intervals "0" = Oakes, "G" = Greenwood.
conf	Level of confidence for confidence interval calculations; 1 - $P(\text{type I error})$
age.seq	A sequence of numbers indicating the age classes used.
ylab	Y-axis label.
xlab	X-axis label.
type	type argument from <a href="#">plot</a> .
plot.km	Logical. Should plot be created?
plot.CI	Logical. Should confidence interval be overlaid on plot?
...	Additional arguments from <a href="#">plot</a> .

### Details

Details for this index are given in Pollock et al. (1989).

### Value

Returns a list with the following components

s.hat	A vector of estimated survivorship probabilities from the 1st age class onward.
Greenwood.Var	The estimated Greenwood variance for each age class.
Oakes.Var	The estimated Oakes variance for each age class.
CI	Upper and lower confidence bound to the true survivorship.

### Author(s)

Ken Aho

**References**

Pollock, K. H., Winterstein, S. R., and Curtis, P. D. (1989) Survival analysis in telemetry studies: the staggered entry design. *Journal of Wildlife Management*. 53(1):7-1.

**Examples**

```
##Example from Pollock (1989)
r<-c(18,18,18,16,16,16,15,15,13,10,8,8,7)
d<-c(0,0,2,0,0,1,0,1,1,1,0,0,0)

km(r,d)
```

---

 Kullback

---

*Kullback test for equal covariance matrices.*


---

**Description**

Provides Kullback's (1959) test for multivariate homoscedasticity.

**Usage**

```
Kullback(Y, X)
```

**Arguments**

Y	An $n \times p$ matrix of quantitative variables
X	An $n \times 1$ vector of categorical assignments (e.g. factor levels)

**Details**

Multivariate general linear models assume equal covariance matrices for all factor levels or factor level combinations. Legendre and Legendre (1998) recommend this test for verifying homoscedasticity.  $P$ -values concern a null hypothesis of equal population covariance matrices.  $P$ -values from the test are conservative with respect to type I error.

**Value**

Returns a dataframe with the test statistic (which follows a chi-square distribution if  $H_0$  is true), the chi-square degrees of freedom, and the calculated  $p$ -value. Invisible objects include the within group dispersion matrix.

**Author(s)**

Pierre Legendre is the author of the most recent version of this function asbio ver  $\geq 1.0$ . Stephen Ousley discovered an error in the original code. Ken Aho was the author of the original function

## References

- Kullback, S. (1959) *Information Theory and Statistics*. John Wiley and Sons.
- Legendre, P, and Legendre, L. (1998) *Numerical Ecology, 2nd English edition*. Elsevier, Amsterdam, The Netherlands.

## Examples

```
Y1<-rnorm(100,10,2)
Y2<-rnorm(100,15,2)
Y3<-rnorm(100,20,2)
Y<-cbind(Y1,Y2,Y3)
X<-factor(c(rep(1,50),rep(2,50)))
Kullback(Y,X)
```

---

larrea	<i>Creosote bush counts</i>
--------	-----------------------------

---

## Description

Phillips and MacMahon (1981) conducted an extensive study of *Larrea tridentata* (creosote bush) distributions in the Mojave and Sonoran deserts from several life stage classes based areal coverage: Life stage 1 (102 -103 cm<sup>2</sup>) Life stage 2 (103 -104 cm<sup>2</sup>), and Life stage 3 (104 -105 cm<sup>2</sup>). Data were generated (using variance and mean values, and the function `rpois` to approximate the results of the authors.

## Usage

```
data(larrea)
```

## Format

A data frame with 25 observations on the following 3 variables.

class1 Counts from life stage 1

class2 Counts from life stage 2

class3 Counts from life stage 3

## References

- Phillips, D. L., and J. A. MacMahon (1981) Competition and spacing patterns in desert shrubs. *Journal of Ecology* 69(1): 97-115.

---

`life.exp`*Mouse life expectancy data*

---

**Description**

Weindruch et al. (1986) compared life expectancy of field mice given different diets. To accomplish this, the authors randomly assigned 244 mice to one of four diet treatments.

**Usage**

```
data(life.exp)
```

**Format**

A data frame with 244 observations on the following 2 variables.

`lifespan` Lifespan in weeks

`treatment` a factor with levels N/N85: Mice were fed normally both before and after weaning (the slash distinguishes pre and post weaning). After weaning the diet consisted of 85kcal/week, a conventional total for mice rearing, N/R40: Mice were fed normally before weaning, but were given a severely restricted diet of 40 kcal per week after feeding, N/R50: Mice were restricted to 50kcal per week before and after weaning, R/R50: Mice were fed normally before weaning, but their diet was restricted to 50 kcal per week after weaning.

**Source**

Ramsey, F. L., and D. W. Schafer (1997) *The Statistical Sleuth: A Course in Methods of Data Analysis*. Duxbury Press, Belmont, CA.

**References**

Weindruch, R., Walford, R. L., Fligiel, S., and D. Guthrie (1986) The retardation of aging in mice by dietary restriction: longevity, cancer, immunity and lifetime energy intake. *The Journal of Nutrition* 116 (4): 641-54.

**Examples**

```
data(life.exp)
## maybe str(life.exp) ; plot(life.exp) ...
```

---

lm.select	<i>AIC, AICc, BIC, Mallow's Cp, and PRESS evaluation of linear models</i>
-----------	---

---

### Description

The function provide model selection summaries using *AIC*, *AICc*, *BIC*, Mallow's  $C_p$ , and *PRESS* for a list of objects of class `lm`

### Usage

```
lm.select(lms, deltaAIC = FALSE)
```

### Arguments

<code>lms</code>	A list containing linear models.
<code>deltaAIC</code>	Logical; Should a $\Delta AIC$ summary be given with relative likelihoods and Akaike weights?

### Note

Mallow's  $C_p$  assumes that all models are nested within the first model in the argument `lms`. Non-nesting will produce a warning message.

### Author(s)

Ken Aho

### See Also

[AIC](#), [press](#)

### Examples

```
Y <- rnorm(100)
X1 <- rnorm(100)
X2 <- rnorm(100)

lms <- list(lm(Y ~ X1), lm(Y ~ X1 + X2))
lm.select(lms)
```

---

 magnets

*Magnet pain relief data*


---

### Description

Magnets have long been used as an alternative medicine, particularly in the Far East, for speeding the recovery of broken bones and to aid in pain relief. Vallbona et al. (1997) tested whether chronic pain experienced by post-polio patients could be treated with magnetic fields applied directly to pain trigger points. The investigators identified fifty subjects who not only had post-polio syndrome, but who also experienced muscular or arthritic pain. Magnets were applied to pain trigger points in 29 randomly selected subjects, and in the other 21 a placebo was applied. The patients were asked to subjectively rate pain on a scale from one to ten before and after application of the magnet or placebo.

### Usage

```
data(magnets)
```

### Format

The dataframe contains 4 columns

Score\_1 Reported pain level before application of treatment.

Score\_2 Reported pain level after application of treatment.

Active Categorical variable indicating whether the device applied was active (magnet) or inactive (placebo).

### Source

Vallbona, C. et al (1997) Response of pain to static magnetic fields in post-polio patients, a double blind pilot study. *Archives of Physical Medicine and Rehabilitation*. 78: 1200-1203.

---

 MC

*Simple functions for MCMC demonstrations*


---

### Description

Function MC creates random Markov Chain from a transitions matrix. Function Rf presents proportional summaries of discrete states from MC. Function mat.pow finds the exponential expansion of a matrix. Required for finding the expectations of a transition matrix.

### Usage

```
MC(T, start, length)
```

```
Rf(res)
```

```
mat.pow(mat, pow)
```



**Arguments**

T	A symmetric transition matrix.
start	Starting state
length	Length of the chain to be created
res	Results from MC.
mat	A symmetric matrix.
pow	Power the matrix is to be raised to.

**Author(s)**

Ken Aho

**Examples**

```
A <- matrix(nrow = 4, ncol = 4, c(0.5, 0.5, 0, 0, 0.25, 0.5, 0.25, 0, 0, 0.25, 0.5, 0.25,
0, 0, 0.5, 0.5), byrow = TRUE)
pi.0 <- c(1, 0, 0, 0)
Tp10 <- mat.pow(A, 10)
chain <- MC(A, 1, 100)
Rf(chain)
```

---

MC.test

*Monte Carlo hypothesis testing for two samples.*

---

**Description**

MC.test calculates a permutation distribution of test statistics from a Welch *t*-test. It compares this distribution to an initial test statistic calculated using non-permuted data, to derive an empirical *P*-value.

**Usage**

```
MC.test(Y,X, perm = 1000, alternative = "not.equal", paired = FALSE, print = TRUE)
```

**Arguments**

Y	Response data.
X	Categorical explanatory variable.
perm	Number of iterations.
paired	Logical: Are sample paired?
alternative	Alternative hypothesis. One of three options: "less", "greater", or "not.equal". These provide lower-tail, upper-tail, and two-tailed tests.
print	Logical: automatically print a pretty summary of results (default).

**Details**

The method follows the description of Manly (1998) for a two-sample test. Upper and lower tailed tests are performed by finding the portion of the distribution greater than or equal to the observed  $t$  test statistic (upper-tailed) or less than or equal to the observed test statistic (lower-tailed). A two tailed test is performed by multiplying the portion of the null distribution greater than or equal to the absolute value of the observed test statistic and less than or equal to the absolute value of the observed test statistic times minus one. Results from the test will be similar to `oneway_test` from the library `coin` because it is based on an equivalent test statistic. As with `t.test`, pairing is assumed to occur within levels of  $X$ . That is, the responses  $Y = 11$  and  $Y = 2$  occur in the same pair (block) below.

```
Y <- c(11,12,13,2,3,4)
```

```
X <- c(1,1,1,2,2,2)
```

**Value**

Returns a list with the following items:

<code>observed.test.statistic</code>	$t$ -statistic calculated from non-permuted (original) data.
<code>no_of_permutations_exceeding_observed_value</code>	The number of times a Monte Carlo derived test statistic was more extreme than the initial observed test statistic.
<code>p.value</code>	Empirical $P$ -value
<code>alternative</code>	The alternative hypothesis

**Author(s)**

Ken Aho, thanks to Vince Buonaccorsi who found an error under `paired = TRUE`.

**References**

Manly, B. F. J. (1997) *Randomization and Monte Carlo Methods in Biology*, 2nd edition. Chapman and Hall, London.

**See Also**

[t.test](#)

**Examples**

```
Y<-c(runif(100,1,3),runif(100,1.2,3.2))
X<-factor(c(rep(1,100),rep(2,100)))
MC.test(Y,X,alternative="less")
```

---

mcmc.norm.hier                    *Gibbs sampling of normal hierarchical models*


---

### Description

These functions are designed for Gibbs sampling comparison of groups with normal hierarchical models (see Gelman 2003), and for providing appropriate summaries.

### Usage

```
mcmc.norm.hier(data, length = 1000, n.chains = 5)

norm.hier.summary(M, burn.in = 0.5, cred = 0.95, conv.log = TRUE)
```

### Arguments

data	A numerical matrix with groups in columns and observations in rows.
length	An integer specifying the length of MCMC chains.
n.chains	The number of chains to be computed for each parameter
M	An output array from <code>mcmc.norm.hier</code> .
burn.in	The burn in period for the chains. The default value, 0.5, indicates that only the latter half of chains should be used for calculating summaries.
cred	Credibility interval width.
conv.log	A logical argument indicating whether convergence for $\sigma$ and $\tau$ should be considered on a log scale.

### Details

An important Bayesian application is the comparison of groups within a normal hierarchical model. We assume that the data from each group are independent and from normal populations with means  $\theta[j]$ ,  $j = (1, \dots, J)$ , and a common variance,  $\sigma^2$ . We also assume that group means, are normally distributed with an unknown mean,  $\mu$ , and an unknown variance,  $\tau^2$ . A uniform prior distribution is assumed for  $\mu$ ,  $\log\sigma$  and  $\tau$ ;  $\sigma$  is logged to facilitate conjugacy. The function `mcmc.norm.hier` provides posterior distributions of  $\theta[j]$ 's,  $\mu$ ,  $\sigma$  and  $\tau$ . The distributions are derived from univariate conditional distributions from the multivariate likelihood function. These conditional distributions provide a situation conducive to MCMC Gibbs sampling. Gelman et al. (2003) provide excellent summaries of these sorts of models.

The function `mcmc.summary` provides statistical summaries for the output array from `mcmc.norm.hier` including credible intervals (empirically derived directly from chains) and the Gelman/Rubin convergence criterion,  $\hat{R}$ .

### Value

The function `mcmc.norm.hier` returns a three dimensional (step x variable x chain) array. The function `mcmc.summary` returns a summary table containing credible intervals and the Gelman/Rubin convergence criterion,  $\hat{R}$ .

**Author(s)**

Ken Aho

**References**

Gelman, A., Carlin, J. B., Stern, H. S., and D. B. Rubin (2003) *Bayesian Data Analysis, 2nd edition*. Chapman and Hall/CRC.

**See Also**[R.hat](#)**Examples**

```
## Not run:
data(cuckoo)
mcmc.norm.hier(cuckoo,10,2)

## End(Not run)
```

ML.k

---

*Maximum likelihood algorithm for determining the binomial dispersal coefficient*

---

**Description**

The function uses the maximum likelihood method described by Bliss and R. A. Fisher (1953) to determine maximum likelihood estimates for the binomial parameters  $m$  (the mean) and  $k$  (a parameter describing aggregation/dispersion).

**Usage**

```
ML.k(f, x, res = 1e-06)
```

**Arguments**

f	A vector of frequencies for objects in x (must be integers).
x	A vector of counts, must be sequential integers.
res	Resolution for the ML estimator.

**Value**

Returns a list with two items

k	The negative binomial dispersion parameter, $k$
m	The negative binomial distribution mean, $m$

**Note**

The program is slow at the current resolution. Later iterations will use linear interpolation, or Fortran loops, or both.

**Author(s)**

Ken Aho

**References**

Bliss, C. I., and R. A. Fisher (1953) Fitting the negative binomial distribution to biological data. *Biometrics* 9: 176-200.

**See Also**

[dnbinom](#)

**Examples**

```
mites <- seq(0, 8)
freq <- c(70, 38, 17, 10, 9, 3, 2, 1, 0)
ML.k(freq, mites)
```

---

Mode

*Sample mode*

---

**Description**

Calculates the sample mode; i.e. the most frequent outcome in a dataset. Non-existence of the mode will return a message. Several errors in earlier versions were corrected in *asbio* 0.4.

**Usage**

```
Mode(x)
```

**Arguments**

x                    A vector of quantitative data.

**Value**

Returns the sample mode or an error message if the mode does not exist.

**Author(s)**

Ken Aho

**References**

Bain, L. J., and M. Engelhardt (1992) *Introduction to Probability and Mathematical Statistics*. Duxbury press. Belmont, CA, USA.

**See Also**

[H.mean](#), [HL.mean](#), [mean](#), [median](#), [huber.mu](#)

**Examples**

```
x<-round(rnorm(100000,mean=10,sd=2),0)
Mode(x)
```

---

modlevene.test	<i>Modified Levene's test</i>
----------------	-------------------------------

---

**Description**

Conducts the modified Levene's test for homoscedastic populations.

**Usage**

```
modlevene.test(y, x)
```

**Arguments**

y	Vector of quantitative responses, e.g., residuals from a linear model.
x	Vector of factor levels.

**Details**

The modified Levene's test is a test for homoscedasticity that (unlike the classic  $F$ -test) is robust to violations of normality (Conover et al. 1981). In a Modified Levene's test we calculate  $d_{ij} = |e_{ij} - \tilde{e}_i|$  where  $\tilde{e}_i$  is the  $i$ th factor level residual median. We then run an ANOVA on the  $d_{ij}$ 's. If the  $p$ -value is  $< \alpha$ , we reject the null and conclude that the population error variances are not equal.

**Value**

An ANOVA table is returned with the modified Levene's test results.

**Author(s)**

Ken Aho

**References**

Kutner, M. H., Nachtsheim, C. J., Neter, J., and W. Li. (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.

**See Also**

[fligner.test](#)

**Examples**

```
eggs<-c(11,17,16,14,15,12,10,15,19,11,23,20,18,17,27,33,22,26,28)
trt<-as.factor(c(1,1,1,1,1,2,2,2,2,3,3,3,3,4,4,4,4,4))
lm1<-lm(eggs~trt)
modlevene.test(residuals(lm1),trt)
```

---

montane.island

*Mountain island biogeographic data*

---

**Description**

Lomolino et al. (1989) investigated the relationship between the area of montane forest patches (islands) and the richness of mammal fauna in the Southwestern United States. This dataset contains richness and area information for 27 montane islands.

**Usage**

```
data(montane.island)
```

**Format**

A data frame with 27 observations on the following 3 variables.

Island.name a factor with levels Abajos Animas Blacks Capitans Catalinas Chirucahuas Chuskas Guadalupe Huachucas Hualapais Lasals Magdalenas Manzanos Mogollon Mt. Taylor N. Rincon N. Uncompaghre Navajo Organs Pinalenos Prescotts S. Kabib Sacramentos San Mateos Sandias Santa Ritas Zunis.

Richness A numeric vector; the number of species.

Area A numeric vector; area in km<sup>2</sup>.

**Source**

Lomolino, M. V., Brown, J. H., and R. Davis (1989) Island biogeography of montane forest mammals in the American Southwest. *Ecology* 70: 180-194.

---

`moose.sel`*Datasets for resource use and availability*

---

**Description**

A collection of datasets which can be used to calculate and compare selection ratios. Datasets are: `goat.sel`, `mule.sel`, `quail.sel`, `elk.sel`, `bighorn.sel`, `bighornAZ.sel`, `juniper.sel` and are described (briefly) in Manly et al. (2002) and Aho and Bowyer (2015).

**Usage**

```
data(moose.sel)
data(goat.sel)
data(quail.sel)
data(elk.sel)
data(bighorn.sel)
data(bighornAZ.sel)
data(juniper.sel)
```

**Format**

Dataframes with observations on the following variables.

`resources` A factor listing resource types.

`avail` Proportional availability (for datasets without `n2` and `y2`).

`y1` A numeric vector: number of times the resource was used.

`y2` A numeric vector: number of time the resource was observed.

`n1` A numeric vector: number of times that all resources were used.

`n2` A numeric vector: number of times that all resources were observed.

**Source**

Manly BF, McDonald LL, Thomas DL, McDonald TL, Erickson WP (2002) *Resource Selection by Animals: Statistical Design and Analysis for Field Studies*. 2nd edn. Kluwer, New York

**References**

Aho, K., and Bowyer, T. 2015. Confidence intervals for ratios of proportions: implications for selection ratios. *Methods in Ecology and Evolution* 6: 121-132.



---

mosquito	<i>Mosquito wing length data</i>
----------	----------------------------------

---

**Description**

Sokal and Rohlf (2012) describe an experiment to gauge the variability in wing length in female mosquitos (*Aedes intrudens*). Four females were randomly selected from three cages and two measurements were made on the left wing of each female. Both cage and female (in cage) can be seen as random effects.

**Usage**

```
data(mosquito)
```

**Format**

A data frame with 24 observations on the following 4 variables.

length Wing length in micrometers

cage Cage number.

female Female (in cage) number

measures Measurement (in female in cage) number, i.e. pseudoreplicates in female.

**Source**

Sokal, R. R., and F. J. Rohlf (2012) *Biometry, 4th edition*. W. H. Freeman and Co., New York.

---

MS.test	<i>Mack-Skillings test</i>
---------	----------------------------

---

**Description**

Runs a Mack-Skillings test for situations applicable to rank-based permutation procedures with blocking and more than one replicate for treatments in a block.

**Usage**

```
MS.test(Y, X, reps)
```

**Arguments**

Y A matrix of response data. The MS.test function requires that response data are organized in columns (see example below).

X A vector of treatments. The length of the vector should be equal to the number of rows in the response matrix.

reps The number of replicates in each treatment (unbalanced designs cannot be analyzed).

**Details**

When we have more than one replication within a block, and the number of replications is equal for all treatments, we can use the Mack-Skillings test (Mack and Skillings 1980) as a rank based permutation procedure to test for main effect differences. If ties occur the value of the significance level is only approximate. Hollander and Wolfe (1996) provide a method for finding exact  $P$ -values by deriving a test statistic distribution allowing ties.

**Value**

Returns a dataframe summarizing the degrees of freedom, test statistic and  $p$ -value.

**Author(s)**

Ken Aho

**References**

- Campbell, J. A., and O. Pelletier (1962) Determination of niacin (niacinamide) in cereal products. *J. Assoc. Offic. Anal. Chem.* 45: 449-453.
- Hollander, M., and D. A. Wolfe (1999) *Nonparametric Statistical Methods*. New York: John Wiley & Sons.
- Mack, G. A., and J. H. Skillings (1980) A Friedman-type rank test for main effects in a two-factor ANOVA. *Journal of the American Statistical Association.* 75: 947-951.

**See Also**

[friedman.test](#)

**Examples**

```
#data from Campbell and Pelletier (1962)
Niacin0<-c(7.58,7.87,7.71,8.00,8.27,8,7.6,7.3,7.82,8.03,7.35,7.66)
Niacin4<-c(11.63,11.87,11.40,12.20,11.70,11.80,11.04,11.50,11.49,11.50,10.10,11.70)
Niacin8<-c(15.00,15.92,15.58,16.60,16.40,15.90,15.87,15.91,16.28,15.10,14.80,15.70)
Niacin<-cbind(Niacin0,Niacin4,Niacin8)
lab<-c(rep(1,3),rep(2,3),rep(3,3),rep(4,3))
MS.test(Niacin, lab, reps=3)
```

---

myeloma

*Patient responses to myeloma drug treatments*

---

**Description**

Murakami et al. (1997) studied the effect of drugs treatments on levels of serum beta-2 microglobulin in patients with multiple myeloma. Serum beta-2 microglobulin is produced in the body as a result of myelomas, and thus can be used as an indicator of the severity of disease

**Usage**

```
data(myeloma)
```

**Format**

A data frame with 20 observations on the following 2 variables.

mglobulin Levels of serum beta-2 microglobulin in mg/l

drug Drug treatment strategy. Control = sumerifon alone, Trt = malphalan and sumerifon.

**Source**

Ott, R. L., and M. T. Longnecker (2004) *A First Course in Statistical Methods*. Thompson.

**References**

Murakami, H., Ogawara, H., Morita, K., Saitoh, T., Matsushima, T., Tamura, J., Sawamura, M., Karasawa, M., Miyawaki, M., Schimano, S., Satoh, S., and J Tsuchiy (1997) Serum beta-2-microglobulin in patients with multiple myeloma treated with alpha interferon. *Journal of Medicine* 28(5-6):311-8.

---

near.bound

*Nearest neighbor boundary coordinates*

---

**Description**

Finds nearest neighbor boundary Cartesian coordinates for use as arguments in function [prp](#).

**Usage**

```
near.bound(X, Y, bX, bY)
```

**Arguments**

X A vector of Cartesian X-coordinates (e.g. UTM) describing an animal's locations (e.g. telemetry data).

Y A vector of Cartesian Y coordinates (e.g. UTM) describing an animal's locations (e.g. telemetry data).

bX A vector of boundary X-coordinates.

bY A vector of boundary Y-coordinates.

**Value**

Returns Cartesian X,Y coordinates of nearest neighbor locations on a boundary.

**Author(s)**

Ken Aho

**See Also**[prp](#), [bound.angle](#)**Examples**

```

bX<-seq(0,49)/46
bY<-c(4.89000,4.88200,4.87400,4.87300,4.88000,4.87900,4.87900,4.90100,4.90800,
4.91000,4.93300,4.94000,4.91100,4.90000,4.91700,4.93000,4.93500,4.93700,
4.93300,4.94500,4.95900,4.95400,4.95100,4.95800,4.95810,4.95811,4.95810,
4.96100,4.96200,4.96300,4.96500,4.96500,4.96600,4.96700,4.96540,4.96400,
4.97600,4.97900,4.98000,4.98000,4.98100,4.97900,4.98000,4.97800,4.97600,
4.97700,4.97400,4.97300,4.97100,4.97000)

X<-c(0.004166667,0.108333333,0.316666667,0.525000000,0.483333333,0.608333333,
0.662500000,0.683333333,0.900000000,1.070833333)
Y<-c(4.67,4.25,4.26,4.50,4.90,4.10,4.70,4.40,4.20,4.30)
near.bound(X,Y,bX,bY)

```

one.sample.t

*One sample t-test***Description**

Provides a one-sample hypothesis test. The test assumes that the underlying population is normal.

**Usage**

```

one.sample.t(data = NULL, null.mu = 0, xbar = NULL, sd = NULL, n = NULL,
alternative = "two.sided", conf = 0.95, na.rm = FALSE, fpc = FALSE, N = NULL)

```

**Arguments**

<code>data</code>	A vector of quantitative data. Not required if <code>xbar</code> and <code>n</code> are supplied by the user.
<code>null.mu</code>	The expectation for the null distribution.
<code>xbar</code>	Sample mean. Not required if <code>is.null(data)==FALSE</code>
<code>sd</code>	The sample standard deviation. Not required if <code>is.null(data)==FALSE</code>
<code>n</code>	The sample size. Not required if <code>is.null(data)==FALSE</code>
<code>alternative</code>	Type of test. One of three must be specified "two.sided", "less", or "greater"
<code>conf</code>	Confidence level.
<code>na.rm</code>	Logical, indicate whether NA values should be stripped before the computation proceeds.

fpc	A logical statement specifying whether a finite population correction should be made. If fpc = TRUE the population size N must be specified.
N	The population size. Required if fpc=TRUE

**Details**

The function can use either raw data `is.null(data)==FALSE` or summarized data if `is.null(data)==TRUE`. With the later `xbar`, and `n` must be specified by the user.

**Value**

Returns a test statistic and a  $p$ -value.

**Author(s)**

Ken Aho. Thanks to Samuel Hale for identifying a function bug.

**See Also**

[pt](#)

**Examples**

```
one.sample.t(null.mu = 131, xbar = 126, sd = 12, n = 85,
alternative = "two.sided")
```

---

one.sample.z	<i>One sample z-test</i>
--------------	--------------------------

---

**Description**

Provides a one-sample hypothesis test. The test assumes that the underlying population is normal and furthermore that  $\sigma$  is known.

**Usage**

```
one.sample.z(data = NULL, null.mu = 0, xbar = NULL, sigma, n = NULL,
alternative = "two.sided", conf = 0.95, na.rm = FALSE, fpc = FALSE, N = NULL)
```

**Arguments**

data	A vector of quantitative data. Not required if <code>xbar</code> and <code>n</code> are supplied by the user.
null.mu	The expectation for the null distribution.
xbar	Sample mean. Not required if <code>is.null(data)==FALSE</code>
sigma	The null distribution standard deviation
n	The sample size. Not required if <code>is.null(data)==FALSE</code>

alternative	Type of test. One of three must be specified "two.sided", "less", or "greater"
conf	Confidence level.
na.rm	Logical, indicate whether NA values should be stripped before the computation proceeds.
fpc	A logical statement specifying whether a finite population correction should be made. If fpc = TRUE the population size N must be specified.
N	The population size. Required if fpc=TRUE

### Details

The function can use either raw data `is.null(data)==FALSE` or summarized data if `is.null(data)==TRUE`. With the later `xbar` and `n` must be specified by the user.

### Value

Returns a test statistic and a  $p$ -value.

### Author(s)

Ken Aho. Thanks to Anderson Canteli for identifying a bug in the function for **asbio** versions < 1.9-6.

### See Also

[pnorm](#)

### Examples

```
one.sample.z(null.mu = 131, xbar = 126, sigma = 12, n = 85, alternative = "two.sided")
```

---

paik

*Paik diagrams*

---

### Description

Paik diagrams for the representation of Simpsons Paradox in three way tables.

### Usage

```
paik(formula, counts, resp.lvl = 2, data, circle.mult = 0.4, xlab = NULL,
      ylab = NULL, leg.title = NULL, leg.loc = NULL, show.mname = FALSE,...)
```

**Arguments**

formula	A two sided formula, e.g. $Y \sim X1 + X2$ , with cross-classified categorical variables. The second explanatory variable, i.e. $X2$ , is used as the trace variable whose levels are distinguished in the graph with different colors. Interactions and nested terms are not allowed.
counts	A vector of counts for the associated categorical variables in formula.
resp.lvl	The level in $Y$ of primary interest. See example below.
data	Dataframe containing variables in formula.
circle.mult	Multiplier for circle radii in the diagram.
xlab	X-axis label. By default this is defined as the categories in the first explanatory variable, $X1$ .
ylab	Y-axis label. By default these will be proportions with respect to the specified level of interest in the response.
leg.title	Legend title. By default the conditioning variable name.
leg.loc	Legend location. A legend location keyword; "bottomright", "bottom", "bottomleft", "left", "topleft", "top", "topright", "right" or "center".
show.mname	Logical, indicating whether or not the words "Marginal prop" should printed in the graph above the dotted line indicating marginal proportions.
...	Additional arguments from <a href="#">plot</a> .

**Author(s)**

Ken Aho

**References**

- Agresti, A. (2012) *Categorical Data Analysis, 3rd edition*. New York. Wiley.
- Paik M. (1985) A graphical representation of a three-way contingency table: Simpson's paradox and correlation. *American Statistician* 39:53-54.

**Examples**

```
require(tcltk)

data(death.penalty)# from Agresti 2012

op <- par(mfrow=c(1,2), mar=c(4,4,0,0))
paik(verdict ~ d.race + v.race, counts = count, data = death.penalty,
leg.title = "Victims race", xlab = "Defendants race",
ylab = "Proportion receiving death penalty")
par(mar=c(4,2,0,2))
paik(verdict ~ v.race + d.race, counts = count, data = death.penalty,
xlab = "Victims race", leg.title = "Defendants race",leg.loc="topleft",
ylab = "", yaxt = "n")
par(op)
```

```

if(interactive()){
  if(any(names(sessionInfo())$otherPkgs=="asbio")) vignette(package = "asbio", "simpson")
}

```

---

pairw.anova	<i>Conducts pairwise post hoc and planned comparisons associated with an ANOVA</i>
-------------	--

---

## Description

The function `pairw.anova` replaces the defunct `Pairw.test`. Conducts all possible pairwise tests with adjustments to  $P$ -values using one of five methods: Least Significant difference (LSD), Bonferroni, Tukey-Kramer honest significantly difference (HSD), Scheffe's method, or Dunnett's method. Dunnett's method requires specification of a control group, and does not return adjusted  $P$ -values. The functions `scheffe.cont` and `bonf.cont` allow Bonferroni and Scheffe's family-wise adjustment of individual planned pairwise contrasts.

## Usage

```

pairw.anova(y, x, conf.level = 0.95, method = "tukey",
MSE = NULL, df.err = NULL, control = NULL)

lsdCI(y, x, conf.level = 0.95, MSE = NULL, df.err = NULL)

bonfCI(y, x, conf.level = 0.95, MSE = NULL, df.err = NULL)

tukeyCI(y, x, conf.level = 0.95, MSE = NULL, df.err = NULL)

scheffeCI(y, x, conf.level = 0.95, MSE = NULL, df.err = NULL)

dunnettCI(y, x, conf.level = 0.95, control = NULL)

scheffe.cont(y, x, lvl = c("x1", "x2"), conf.level = 0.95,
MSE = NULL, df.err = NULL)

bonf.cont(y, x, lvl = c("x1", "x2"), conf.level = 0.95,
MSE = NULL, df.err = NULL, comps = 1)

```

## Arguments

<code>y</code>	A quantitative vector containing the response variable
<code>x</code>	A categorical vector containing the groups (e.g. factor levels or treatments)
<code>conf.level</code>	1 - $P$ (type I error)
<code>method</code>	One of five possible choices: "lsd", "bonf", "tukey", "scheffe", "dunnett"
<code>MSE</code>	Value of MSE from the ANOVA model. Default = NULL



df.err	Degrees of freedom error from the omnibus ANOVA. Default = NULL
control	Control group for Dunnett's test.
lvl	A two element vector defining two factor levels to be compared using Scheffe's and the Bonferroni method.
comps	The number of comparisons to be made in the Bonferroni method.

### Details

Adjustment of comparison type I error for simultaneous inference is a contentious subject and will not be discussed here. For description of methods go to Kutner et al. (2005). For models where the number of factors is  $\geq 2$ , MSE and the residual degrees of freedom (used in the computation of confidence intervals for all pairwise methods used here) will vary depending on the experimental design and the number of factors. Thus, for multifactor designs the user should specify the residual degrees of freedom and MSE from the overall ANOVA. This will be unnecessary for one-way ANOVAs.

### Value

The function `pairw.anova` and the confidence interval functions it calls return a list of class = "pairw". For all but the LSD test (which also returns LSD) and Dunnett's test (which does not return adjusted *P*-values), the utility function `print.pairw` returns a descriptive head and a six column summary dataframe containing:

- 1) the type of contrast (names are taken from levels in *x*),
- 2) the mean difference,
- 3) the lower confidence bound of the true mean difference,
- 4) the upper confidence bound of the true mean difference,
- 5) the hypothesis decision, given the prescribed significance level, and
- 6) the adjusted *P*-value.

Other invisible objects include:

cont	a vector of contrasts.
conf	The confidence level.
band	A two column matrix containing the lower and upper confidence bounds.

The `pairw` class also has a utility function `plot.pairw` which provides either a barplot of location measures with errors and letters indicating whether true effects are significant and the defined significance level (argument `type = 1`) or confidence intervals for the true difference of each comparison (argument `type = 2`). See code below and `plot.pairw` for examples.

### Note

Different forms of these functions have existed for years without implementation into libraries. My version here, based on the function `outer` is unique.

### Author(s)

Ken Aho

## References

Kutner, M. H., Nachtsheim, C. J., Neter, J., and Li., W (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.

## See Also

`plot.pairw`. Functions from library **mult.comp** provide more sophisticated comparisons including customized contrasts and one tailed tests.

## Examples

```
eggs<-c(11,17,16,14,15,12,10,15,19,11,23,20,18,17,27,33,22,26,28)
trt<-as.factor(c(1,1,1,1,1,2,2,2,2,3,3,3,3,4,4,4,4,4))

pairw.anova(y = eggs, x = trt, method = "lsd")##LSD method
pairw.anova(y = eggs, x = trt, method = "bonf")##Bonferroni
pairw.anova(y = eggs, x = trt, method = "scheffe")##Sheffe
tukey <- pairw.anova(y = eggs, x = trt, method = "tukey")##Tukey HSD

plot(tukey)
# you can also try plot(tukey, type = 2)

blood.count <- data.frame(bc=c(7.4,8.5,7.2,8.24,9.84,8.32,9.76,8.8,
7.68,9.36,12.8,9.68,12.16,9.2,10.55), trt=c(rep("C",6),rep("A",4),rep("B",5)))
with(blood.count,pairw.anova(y=bc,x=trt,control="C",method="dunnett"))## Dunnett

scheffe.cont(y = eggs, x = trt, lvl = c(1, 3))
scheffe.cont(y = eggs, x = trt, lvl = c(1,2))

bonf.cont(y = eggs, x = trt, lvl = c(1,3), comps = 2)
bonf.cont(y = eggs, x=trt, lvl = c(1,2), comps = 2)
```

---

pairw.fried

*Multiple pairwise comparison procedure to accompany a Friedman test.*

---

## Description

Replaces now defunct `FR.multi.comp`. As with ANOVA we can examine multiple pairwise comparisons from a Friedman test after we have rejected the overall null hypothesis. However we will need to account for family-wise type I error in these comparisons which will be non-orthogonal. A conservative multiple comparison method used here is based on the Bonferroni procedure.

## Usage

```
pairw.fried(y, x, blocks, nblocks, conf = 0.95)
```

**Arguments**

y	A vector of responses, i.e. quantitative data.
x	A categorical vector of factor levels.
blocks	A categorical vector of blocks.
nblocks	The number of blocks.
conf	The level of confidence. $1 - P(\text{type I error})$ .

**Value**

Returns a list of class = "pairw". The utility print function returns a descriptive head and a six column summary dataframe containing:

- 1) the type of contrast (names are taken from levels in x),
- 2) the mean rank difference,
- 3) the lower confidence bound of the true mean rank difference,
- 4) the upper confidence bound of the true mean rank difference,
- 5) the hypothesis decision given the prescribed significance level, and
- 6) the adjusted  $P$ -value.

**Author(s)**

Ken Aho

**References**

Fox, J. R., and Randall, J. E. (1970) Relationship between forearm tremor and the biceps electromyogram. *Journal of Applied Physiology* 29: 103-108.

Kutner, M. H., Nachtsheim, C. J., Neter, J., and W. Li (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.

**See Also**

[friedman.test](#), [plot.pairw](#)

**Examples**

```
#Data from Fox and Randall (1970)
tremors <- data.frame(freq = c(2.58, 2.63, 2.62, 2.85, 3.01, 2.7, 2.83, 3.15,
3.43, 3.47, 2.78, 2.71, 3.02, 3.14, 3.35, 2.36, 2.49, 2.58, 2.86, 3.1, 2.67,
2.96, 3.08, 3.32, 3.41, 2.43, 2.5, 2.85, 3.06, 3.07), weights =
factor(rep(c(7.5, 5, 2.5, 1.25, 0), 6)), block = factor(rep(1 : 6, each = 5)))

fr <- with(tremors, pairw.fried(y = freq, x = weights, blocks = block, nblocks = 6, conf = .95))
fr
plot(fr, loc.meas = median, int = "IQR")
# you can also try: plot(fr, type = 2, las = 2)
```

---

pairw.kw	<i>Multiple pairwise comparison procedure to accompany a Kruskal-Wallis test</i>
----------	--

---

### Description

Replaces the defunct `KW.multi.comp`. As with ANOVA we can examine multiple pairwise comparisons from a Kruskal-Wallis test after we have rejected our omnibus null hypothesis. However we will need to account for the fact that these comparisons will be non-orthogonal. A conservative multiple comparison method used here is based on the Bonferroni inequality.

### Usage

```
pairw.kw(y, x, conf)
```

### Arguments

y	The response variable. A vector of quantitative responses.
x	An explanatory variable. A vector of factor levels.
conf	The level of desired confidence, $1 - P(\text{type I error})$ .

### Value

Returns a list of class = "pairw". The utility print function returns a descriptive head and a six column summary dataframe containing:

- 1) the type of contrast (names are taken from levels in x),
- 2) the mean rank difference,
- 3) the lower confidence bound of the true mean rank difference,
- 4) the upper confidence bound of the true mean rank difference,
- 5) the hypothesis decision given the prescribed significance level,
- 6) the adjusted  $P$ -value.

### Author(s)

Ken Aho and Richard Boyce. Richard provided an adjustment for ties. Thanks to Paule Bodson-Clermont for pointing out issues with the default behaviour of `rank`, leading to incorrect answers from `pair.kw` given missing values.

### References

Kutner, M. H., Nachtsheim, C. J., Neter, J., and W. Li (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.

### See Also

[pairw.anova](#), [pairw.fried](#), [plot.pairw](#)

**Examples**

```
rye.data <- data.frame(rye = c(50, 49.8, 52.3, 44.5, 62.3, 74.8, 72.5, 80.2,
47.6, 39.5, 47.7, 50.7), nutrient = factor(c(rep(1, 4), rep(2, 4), rep(3, 4))))
kw <- with(rye.data, pairw.kw(y = rye, x = nutrient, conf = .95))
kw
plot(kw, loc.meas = median, int = "IQR")
# you can also try: plot(kw, type = 2)
```

pairw.oneway

*Welch tests controlled for simultaneous inference***Description**

Conducts all possible pairwise Welch tests with adjustments to  $P$ -values using methods from [p.adjust](#)

**Usage**

```
pairw.oneway(y, x, conf = 0.95, digits = 5, method = "holm")
```

**Arguments**

y	Response variable
x	Explanatory variable
conf	Confidence level
digits	Number of digits in results
method	Generalized method for controlling family wise type one error. These must be methods from <a href="#">p.adjust</a> , i.e., "holm", "hochberg", "hommel", "bonferroni", "BH", "BY", "fdr", "none". Names can be abbreviated.

**Value**

The function `pairw.oneway` and the confidence interval functions it calls return a list of class = "pairw".

- 1) the type of contrast (names are taken from levels in x),
- 2) the mean difference,
- 3) the lower confidence bound of the true mean difference,
- 4) the upper confidence bound of the true mean difference,
- 5) the hypothesis decision, given the prescribed significance level, and
- 6) the adjusted  $P$ -value.

Other invisible objects include:

cont	a vector of contrasts.
conf	The confidence level.
band	A two column matrix containing the lower and upper confidence bounds.

**Note**

Note that while  $P$ -values will be adjusted for simultaneous inference (unless `method = "none"`), confidence interval width are generally *not adjusted*. In particular, CI widths correspond to Welch SEs and Satterthwaite  $t$  degrees of freedoms Thus they control for heteroscedasticity, however they do not control for family-wise levels of  $\alpha$  unless `method = "bonferroni"`, under which the restrictive confidence level  $1 - (\alpha/2r)$  is used, where  $r$  is the number of comparisons.

**Author(s)**

Ken Aho and Peter Eckert

**References**

Kutner, M. H., Nachtsheim, C. J., Neter, J., and Li., W (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.

**See Also**

[p.adjust](#), [pairw.anova](#)

**Examples**

```
y <- rnorm(30)
x <- as.factor(c(rep(1,10), rep(2,10), rep(3, 10)))
p <- pairw.oneway(y,x)
p
plot(p)
```

---

panel.cor.res

*Functions for customizing correlation matrices*

---

**Description**

The functions here can be used to customize upper and lower triangles in correlation matrices. In particular `panel.cor.res` provides correlation coefficients (any alternative from `cor` can be used) and  $p$ -values for correlation tests. The function `panel.lm` puts linear fitted lines from simple linear regression in scatterplots. Note that the function `panel.smooth` provides a smoother fit.

**Usage**

```
panel.cor.res(x, y, digits = 2, meth = "pearson", cex.cor=1)
panel.lm(x, y, col = par("col"), bg = NA, pch = par("pch"), cex = 1,
col.line = 2,lty = par("lty"))
```

**Arguments**

x	variable 1 in correlation
y	variable 2 in correlation
digits	number of digits in text for panel.cor.res
meth	type of correlation coefficient from panel.cor.res, one of "pearson", "spearman", "kendall"
cex.cor	size of text in panel.lm
col	color of points in panel.lm
bg	background color of points in panel.lm
pch	type of symbols for points in panel.lm
cex	symbol size in panel.lm
lty	line type in panel.lm
col.line	color of lines in panel.lm

**Author(s)**

Ken Aho

**See Also**

[cor](#), [cor.test](#), [panel.smooth](#)

**Examples**

```
data(asthma)

pairs(asthma, cex.labels=1, cex=.95, gap=.1, lower.panel = panel.cor.res,
upper.panel = panel.lm)
```

---

partial.R2

*Partial correlations of determination in multiple regression*

---

**Description**

Calculates the partial correlation of determination for a variable of interest in a multiple regression.

**Usage**

```
partial.R2(nested.lm, ref.lm)
```

**Arguments**

nested.lm	A linear model without the variable of interest.
ref.lm	A linear model with the variable of interest.

**Details**

Coefficients of partial determination measure the proportional reduction in sums of squares after a variable of interest,  $X$ , is introduced into a model. We can see how this would be of interest in a multiple regression.

**Value**

The partial  $R^2$  is returned.

**Author(s)**

Ken Aho

**References**

Kutner, M. H., Nachtsheim, C. J., Neter, J., and W. Li. (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.

**See Also**

[cor](#), [partial.resid.plot](#)

**Examples**

```
Soil.C<-c(13,20,10,11,2,25,30,25,23)
Soil.N<-c(1.2,2,1.5,1,0.3,2,3,2.7,2.5)
Slope<-c(15,14,16,12,10,18,25,24,20)
Aspect<-c(45,120,100,56,5,20,5,15,15)
Y<-as.vector(c(20,30,10,15,5,45,60,55,45))

lm.with<-lm(Y~Soil.C+Soil.N+Slope+Aspect)
lm.without<-update(lm.with, ~. - Soil.N)

partial.R2(lm.without,lm.with)
```

---

partial.resid.plot      *Partial residual plots for interpretation of multiple regression.*

---

**Description**

The function creates partial residual plots which help a user graphically determine the effect of a single predictor with respect to all other predictors in a multiple regression model.

**Usage**

```
partial.resid.plot(x, smooth.span = 0.8, lf.col = 2, sm.col = 4, ...)
```



**Arguments**

<code>x</code>	A output object of class <code>lm</code> or class <code>glm</code>
<code>smooth.span</code>	Degree of smoothing for smoothing line.
<code>lf.col</code>	Color for linear fit.
<code>sm.col</code>	Color for smoother fit.
<code>...</code>	Additional arguments from <a href="#">plot</a> .

**Details**

Creates partial residual plots (see Kutner et al. 2002). Smoother lines from [lowess](#) and linear fits from `lm` are imposed over plots to help an investigator determine the effect of a particular  $X$  variable on  $Y$  with all other variables in the model. The function automatically inserts explanatory variable names on axes.

**Value**

Returns  $p$  partial residual plots, where  $p$  = the number of explanatory variables.

**Author(s)**

Ken Aho

**References**

Kutner, M. H., Nachtsheim, C. J., Neter, J., and W. Li. (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.

**See Also**

[partial.R2](#)

**Examples**

```
if(interactive()){
  Soil.C<-c(13,20,10,11,2,25,30,25,23)
  Soil.N<-c(1.2,2,1.5,1,0.3,2,3,2.7,2.5)
  Slope<-c(15,14,16,12,10,18,25,24,20)
  Aspect<-c(45,120,100,56,5,20,5,15,15)
  Y<-c(20,30,10,15,5,45,60,55,45)
  x <- lm(Y ~ Soil.N + Soil.C + Slope + Aspect)
  op <- par(mfrow=c(2,2),mar=c(5,4,1,1.5))
  partial.resid.plot(x)
  par(op)
}
```

PCB

*PCBs and herring egg thickness***Description**

Thirteen sites in the Great Lakes were selected for a study to quantify PCB concentrations in 1982 and 1996 (Hughes et al. 1998). At each site 9-13 American herring gull (*Larus smithsonianus*) eggs were randomly collected and tested for PCB content.

**Usage**

```
data(PCB)
```

**Format**

A data frame with 26 observations on the following 3 variables.

nest Nest number

level PCB levels microgram/gram of dry weight

year a numeric vector

**Source**

Ott, R. L., and M. T. Longnecker (2004) *A First Course in Statistical Methods*. Thompson.

**References**

Hughes, K. D., Weseloh, D. V., and B. M. Braune (1998) The ratio of DDE to PCB concentrations in Great Lakes herring gull eggs and its use in interpreting contaminants data. *Journal of Great Lakes Research* 24(1): 12-31.

perm.fact.test

*Permutation test for two and three way factorial designs***Description**

Provides permutation tests for two and three way designs, using permutations of of the response vector with respect to factor levels. One way permutation tests are provided by [MC.test](#), and the function `oneway_test` in `coin`.

**Usage**

```
perm.fact.test(Y, X1, X2, X3 = NA, perm = 100, method = "a")
```

**Arguments**

Y	A vector of response data. A quantitative vector.
X1	A vector of factor levels describing factor one.
X2	A vector of factor levels describing factor two.
X3	If necessary, a vector of factor levels describing factor three.
perm	Number of permutations.
method	Either "a" or "b", see below.

**Details**

Manly (1997) describes five factorial permutation methods which allow testing of interactions. None of these should be considered to be extensively tested or strongly supported by the statistical literature. (a) In the first method observations are randomly allocated to factorial treatments preserving the sample size for each treatment. Permutation distributions of the  $F$  statistics for A, B, and AB are used for statistical tests. (b) In the second method observations are randomized as above but permutation distributions of MSA, MSB and MSAB are obtained. (c) Edgington (1995) recommended a restricted randomization procedure where observations within a main effect are randomized while holding other effects constant. Either mean squares or  $F$  statistics can be used to create permutation distributions. Edgington emphasized that testing interactions with this method are not possible, but that by randomizing over all AB combinations (as in alternative "a" above) provides a test statistic sensitive to interactions. (d) Still and White (1981) recommended a restricted testing procedure (as in (c) above) but recommended testing interactions after "subtracting" main effects. (e) Ter Braak (1992) recommended replacing observations by their residuals from the initial linear model. These are then permuted, assuming that sample sizes were equal to original sample sizes across interactions of treatments. Permutation distributions of the  $F$  statistics for A, B, and AB are then used for statistical tests. Manly (1997) recommends methods a, b, d, or e. Methods a and b are currently implemented.

**Value**

A dataframe is returned describing initial  $F$  test statistics for main effects and interactions, degrees of freedom, and permutation  $P$ -values.

**Author(s)**

Ken Aho

**References**

- Edgington, E. S. (1995) *Randomization Tests, 3rd edition*. Marcel Dekker, New York.
- Manly, B. F. J. (1997) *Randomization and Monte Carlo Methods in Biology, 2nd edition*. Chapman and Hall, London.
- Still, A. W., and A. P. White (1981) The approximate randomization test as an alternative to the  $F$  test in analysis of variance. *British Journal of Mathematics and Statistical Psychology*. 34: 243-252.
- Ter Braak, C. F. J. (1992) Permutation versus bootstrap significance tests in multiple regression and ANOVA. In Jockel, K. J. (ed). *Bootstrapping and Related Techniques*. Springer-Verlag, Berlin.

**See Also**

[MC.test](#)

**Examples**

```
lizard<-data.frame(ants=c(13,242,105,8,59,20,515,488,88,18,44,21,182,21,7,24,312,68,
460,1223,990,140,40,27),size=factor(c(rep(1,12),rep(2,12))),
month=factor(rep(rep(c(1,2,3,4),each=3),2)))
attach(lizard)
perm.fact.test(ants,month,size,perm=100, method = "b")
```

---

pika

*Nitrogen content of soils under pika haypiles*

---

**Description**

Aho (1998) hypothesized that pikas worked as ecosystem engineers by building relatively rich soils (via decomposing haypiles and fecal accumulations) in otherwise barren scree. Soils from twenty one paired on-haypile and off-haypile sites were gathered from Rendezvous Peak Grand Teton National Park to determine if the habitats differed in total soil nitrogen.

**Usage**

```
data(pika)
```

**Format**

A data frame with 22 observations on the following 2 variables.

Haypile a numeric vector

On.Off..N a numeric vector

**References**

Aho, K., Huntly N., Moen J., and T. Oksanen (1998) Pikas (*Ochotona princeps*: Lagomorpha) as allogenic engineers in an alpine ecosystem. *Oecologia*. 114 (3): 405-409.

---

 plantTraits

*Plant traits for 136 species*


---

### Description

This dataset, from the library **cluster**, describes 136 plant species according to biological attributes (morphological or reproductive).

### Usage

```
data(plantTraits)
```

### Format

A data frame with 136 observations on the following 31 variables.

`pdias` Diaspore mass (mg).

`longindex` Seed bank longevity.

`durflow` Flowering duration.

**height** Plant height, an ordered factor with levels '1' < '2' < ... < '8'.

`begflow` Time of first flowering, an ordered factor with levels '1' < '2' < '3' < '4' < '5' < '6' < '7' < '8' < '9'.

`mycor` Mycorrhizae, an ordered factor with levels '0'never < '1' sometimes < '2'always.

`vegaer` Aerial vegetative propagation, an ordered factor with levels '0'never < '1' present but limited < '2'important.

`vegsout` Underground vegetative propagation, an ordered factor with 3 levels identical to 'vegaer' above.

`autopoll` Selfing pollination, an ordered factor with levels '0'never < '1'rare < '2' often < the rule '3'.

`insects` Insect pollination, an ordered factor with 5 levels '0' < ... < '4'.

`wind` Wind pollination, an ordered factor with 5 levels '0' < ... < '4'.

`lign` A binary factor with levels '0':1', indicating if plant is woody.

`piq` A binary factor indicating if plant is thorny.

`ros` A binary factor indicating if plant is rosette.

`semiros` Semi-rosette plant, a binary factor ('0': no; '1': yes).

`leafy` Leafy plant, a binary factor.

`suman` Summer annual, a binary factor.

`winan` Winter annual, a binary factor.

`monocarp` Monocarpic perennial, a binary factor.

`polycarp` Polycarpic perennial, a binary factor.

`seasaes` Seasonal aestival leaves, a binary factor.

seashiv Seasonal hibernal leaves, a binary factor.  
 seasver Seasonal vernal leaves, a binary factor.  
 everalw Leaves always evergreen, a binary factor.  
 everparti Leaves partially evergreen, a binary factor.  
 elaio Fruits with an elaiosome (dispersed by ants), a binary factor.  
 endozoo Endozoochorous fruits, a binary factor.  
 epizoo Epizoochorous fruits, a binary factor.  
 aquat Aquatic dispersal fruits, a binary factor.  
 windgl wind dispersed fruits, a binary factor.  
 unsp Unspecialized mechanism of seed dispersal, a binary factor.

### Details

Most of factor attributes are not disjunctive. For example, a plant can be usually pollinated by insects but sometimes self-pollination can occur.

### Note

The description here follows directly from that in **cluster**.

### Source

Vallet, Jeanne (2005) *Structuration de communautés végétales et analyse comparative de traits biologiques le long d'un gradient d'urbanisation*. Memoire de Master 2 'Ecologie-Biodiversité-Evolution'; Université Paris Sud XI, 30p.+ annexes (in french).

Maechler, M., Rousseeuw, P., Struyf, A., Hubert, M. (2005). *Cluster Analysis Basics and Extensions*; unpublished.

---

plot.pairw

*Plots confidence intervals and/or bars with letters indicating significant differences for objects from class pairw*

---

### Description

Provides a utility confidence interval plotting function for objects of class = "pairw", e.g., objects from pairw.anova, pair.fried, and pairw.kw.

### Usage

```
## S3 method for class 'pairw'
plot(x, type = 1, lcol = 1, lty = NULL, lwd = NULL,
     cap.length = 0.1, xlab = "", main = NULL, explanation = TRUE,...)
```

**Arguments**

x	An object of class pairw.
type	Two types of plots can be made. Type 1 is a barplot with identical letters over bars if the differences are not significant after adjustment for simultaneous inference. Type 1 plots can be modified using <a href="#">bplot</a> arguments. A type 2 plot shows confidence intervals for true differences.
lcol	Confidence bar line color for a type 2 plot, see <a href="#">par</a> .
lty	Confidence bar line type, see <a href="#">par</a> .
lwd	Confidence bar line width, see <a href="#">par</a> .
cap.length	Widths for caps on interval bars (in inches).
xlab	X-axis label.
main	Main caption. Defaults to a descriptive head.
explanation	Logical. If TRUE (default) provides plot explanation with text.
...	Additional arguments from <a href="#">bplot</a> or <a href="#">barplot</a> for type 1 and 2 graphs, respectively.

**Author(s)**

Ken Aho. Letters for type 1 graphs obtained using the function [multcompLetters](#) from package **multcompView** which uses the algorithm of Peipho (2004).

**References**

Piepho, H-P (2004) An algorithm for a letter-based representation of all-pairwise comparisons. *Journal of Computational and Graphical Statistics* 13(2): 456-466.

**See Also**

[pairw.anova](#), [pairw.fried](#), [pairw.kw](#), [barplot](#), [bplot](#), [multcompLetters](#)

**Examples**

```
eggs<-c(11,17,16,14,15,12,10,15,19,11,23,20,18,17,27,33,22,26,28)
trt<-as.factor(c(1,1,1,1,1,2,2,2,2,3,3,3,3,4,4,4,4,4))

# Type 1 plot
plot(pairw.anova(y = eggs, x = trt, method = "scheffe", conf = .8), int = "CI",
conf = .8)
# Type 2 plot
plot(pairw.anova(y = eggs, x = trt, method = "scheffe", conf = .8), type = 2)

# Data from Fox and Randall (1970)
tremors <- data.frame(freq = c(2.58, 2.63, 2.62, 2.85, 3.01, 2.7, 2.83, 3.15,
3.43, 3.47, 2.78, 2.71, 3.02, 3.14, 3.35, 2.36, 2.49, 2.58, 2.86, 3.1, 2.67,
2.96, 3.08, 3.32, 3.41, 2.43, 2.5, 2.85, 3.06, 3.07), weights =
factor(rep(c(7.5, 5, 2.5, 1.25, 0), 6)), block = factor(rep(1 : 6, each = 5)))
```

```

plot(with(tremors, pairw.fried(y = freq, x = weights, blocks = block, nblocks =
6, conf = .95)), loc.meas = median, int = "IQR", bar.col = "lightgreen",
lett.side = 4, density = 3, horiz = TRUE) # Note how blocking increases power

rye.data <- data.frame(rye = c(50, 49.8, 52.3, 44.5, 62.3, 74.8, 72.5, 80.2,
47.6, 39.5, 47.7,50.7), nutrient = factor(c(rep(1, 4), rep(2, 4), rep(3, 4))))

plot(with(rye.data, pairw.kw(y = rye, x = nutrient, conf = .95)), type = 2)

```

---

plotAncova

*Creates plots for one way ANCOVAs*


---

### Description

ANCOVA plots are created, potentially with distinct line types and/or symbols and colors for treatments. A legend relating ciphers to treatments is also included.

### Usage

```

plotAncova(model, pch = NULL, lty = NULL, col = NULL, leg.loc = "topright",
leg.cex = 1, leg.bty = "o", leg.bg = par("bg"), legend.title = NULL,...)

```

### Arguments

model	Result from <a href="#">lm</a> . An additive model results in a common slope plot. An interaction model results in distinct slopes for treatments
pch	A scalar, or a vector of length <i>n</i> defining symbols for treatments.
lty	A scalar, or a vector of length <i>n</i> defining line types for treatments.
col	A scalar, or a vector of length <i>n</i> defining color for symbols and lines.
leg.loc	Location of the legend. "n" suppresses the legend.
leg.cex	Character expansion from <a href="#">legend</a> .
leg.bty	Box type from <a href="#">legend</a> .
leg.bg	Background color from <a href="#">legend</a> .
legend.title	Legend title from <a href="#">legend</a> .
...	Additional arguments from <a href="#">plot</a>

### Value

Returns an ANCOVA plot and model coefficients.

### Author(s)

Ken Aho



**See Also**[lm](#)**Examples**

```
x <- rnorm(20)
y <- 3 * x + rnorm(20)
cat <- c(rep("A",5),rep("B",5),rep("C",5),rep("D",5))
l <- lm(y ~ x * cat)
plotAncova(l, leg.loc = "bottomright")
```

---

plotCI.reg	<i>Plots a simple linear regression along with confidence and prediction intervals.</i>
------------	---

---

**Description**

Plots the fitted line from a simple linear regression ( $y \sim x$ ) and (if requested) confidence and prediction intervals.

**Usage**

```
plotCI.reg(x, y, conf = 0.95, CI = TRUE, PI = TRUE, resid = FALSE, reg.col = 1,
CI.col = 2, PI.col = 4, reg.lty = 1, CI.lty = 2, PI.lty = 3, reg.lwd = 1,
CI.lwd = 1, resid.lty = 3, resid.col = 4,...)
```

**Arguments**

x	The explanatory variable, a numeric vector.
y	The response variable, a numeric vector
conf	The level of confidence; $1 - P(\text{type I error})$
CI	Logical; should the confidence interval be plotted?
PI	Logical; should the prediction interval be plotted?
resid	Logical; should residuals be plotted?
reg.col	Color of the fitted regression line.
CI.col	Color of the confidence interval lines.
PI.col	Color of the prediction interval lines.
reg.lty	Line type for the fitted regression line.
CI.lty	Line type for the confidence interval.
PI.lty	Line type for the confidence interval.
reg.lwd	Line width for the regression line.
CI.lwd	Line widths for the confidence and prediction intervals.
resid.lty	Line width for the regression line.
resid.col	Line color for residual lines.
...	Additional arguments from <a href="#">plot</a>

**Value**

Returns a plot with a regression line and (if requested) confidence and prediction intervals

**Author(s)**

Ken Aho

**See Also**

[plot](#), [predict](#)

**Examples**

```
y<-c(1,2,1,3,4,2,3,4,3,5,6)
x<-c(2,3,1,4,5,4,5,6,7,6,8)
plotCI.reg(x,y)
```

PM2.5

*PM 2.5 pollutant data from Pocatello Idaho*

**Description**

PM 2.5 pollutants (those less than 2.5 microns in diameter) can be directly emitted from sources such as forest fires, or can form when gases discharged from power plants, industries and automobiles react in the air. Once inhaled, these particles can affect the heart and lungs and cause serious health problems. The DEQ began monitoring PM 2.5 pollutants in Pocatello Idaho in November 1998.

**Usage**

```
data(PM2.5)
```

**Format**

A data frame with 65 observations on the following 2 variables.

```
Yr.mos Year and month. A factor with levels 1998 11 1998 12 1999 1 1999 10 1999 11 1999 12
1999 2 1999 3 1999 4 1999 5 1999 6 1999 7 1999 8 1999 9 2000 1 2000 10 2000 11 2000 12
2000 2 2000 3 2000 4 2000 5 2000 6 2000 7 2000 8 2000 9 2001 1 2001 10 2001 11 2001 12
2001 2 2001 3 2001 4 2001 5 2001 6 2001 7 2001 8 2001 9 2002 1 2002 10 2002 11 2002 12
2002 2 2002 3 2002 4 2002 5 2002 6 2002 7 2002 8 2002 9 2003 1 2003 10 2003 11 2003 12
2003 2 2003 3 2003 4 2003 5 2003 6 2003 7 2003 8 2003 9 2004 1 2004 2 2004 3
```

PM2.5 A numeric vector describing PM 2.5 pollutant levels in  $\mu\text{g}/\text{m}^2$ .

**Source**

Idaho department of Environmental Quality

---

polyamine

*Polyamine data from Hollander and Wolfe (1999)*

---

### Description

Polyamines are a class of organic compounds having two or more primary amino groups. They appear to have a number of important functions including regulation of cell proliferation, cell differentiation, and cell death. Polyamine plasma levels taken for healthy children of different ages were summarized by Hollander and Wolfe (1999).

### Usage

```
data(polyamine)
```

### Format

A data frame with 25 observations on the following 2 variables.

age Child age in years (0 indicates newborn)

p.amine Polyamine level in blood

### Source

Hollander, M., and D. A. Wolfe (1999) *Nonparametric Statistical Methods*. New York: John Wiley & Sons.

---

portneuf

*Portneuf River longitudinal N and P data*

---

### Description

Portneuf River data from the Siphon Road site near Pocatello Idaho, downstream from an elemental P refinery.

### Usage

```
data(portneuf)
```

### Format

A data frame with 176 observations on the following 3 variables.

date Dates from 1998-01-15 to 2011-08-16

TKN Total Kjeldahl nitrogen (measured as a percentage)

total.P Total phosphorous (mg/L)

**Source**

Idaho State Department of Environmental Quality

---

potash

*Potash/cotton strength data*

---

**Description**

An oft-cited RCBD example is an agricultural experiment which evaluates the effect of levels of soil  $K_2O$  (potash) on the breaking strength of cotton fibers (Cochran and Cox 1957). Five levels of  $K_2O$  were used in the soil subplots ( 36, 54, 72, 108, and 144 lbs per acre) and a single sample of cotton was taken from each of five subplot. The experiment had three blocks, and each of the  $K_2O$  treatments was randomly assigned to the five subplots within each block.

**Usage**

data(potash)

**Format**

A data frame with 15 observations on the following 3 variables.

treatment a factor with levels 36 54 72 108 144

block a factor with levels 1 2 3

strength a numeric vector

**Source**

Cochran, W. G. and G. M. Cox (1957) *Experimental Designs (Second Edition)*. New York: John Wiley & Sons.

---

potato

*Fisher's Rothamsted potato data*

---

**Description**

In his "Statistical Methods for Research Workers" Fisher (1925) introduced the world to ANOVA using data from the Rothamsted Agricultural Experimental Station. In one example, Fisher compared potato yield (per plant) for twelve potato varieties and three fertilizer treatments (a basal manure application, along with sulfur and chloride addition). Three replicates were measured for each of the  $12 \times 3 = 36$  treatment combinations.

**Usage**

data(potato)

**Format**

A data frame with 108 observations on the following 4 variables.

Yield Potato yield in lbs per plant

Variety Potato variety: Ajax Arran comrade British queen Duke of York Epicure Great Scot  
Iron duke K of K Kerrs pink Nithsdale Tinwald perfection Up-to-date

Fert Fertilizer type: B = basal manure, Cl = chloride addition, S = sulfur addition.

Patch Feld patch number 1 2 3 4 5 6 7 8 9

**Source**

Fisher, R. A. (1925) *Statistical Methods for Research Workers, 1st edition*. Oliver and Boyd, Edinburgh

Thanks to Bob O'Hara for finding a data entry error for this dataset for versions of asbio <= 1.8-2.

---

power.z.test

*Power analysis for a one sample z-test*

---

**Description**

A power analysis for a one sample  $z$ -test. The function requires  $\alpha$ ,  $\sigma$ , the effect size, the type of test (one tailed or two-tailed), and either power ( $1 - \beta$ ) or  $n$  (sample size). If  $n$  is provided, then power is calculated. Conversely, if one provides power, but not  $n$ , then the required  $n$  is calculated.

**Usage**

```
power.z.test(sigma = 1, n = NULL, power = NULL, alpha = 0.05, effect = NULL,
test = c("two.tail", "one.tail"), strict = FALSE)
```

**Arguments**

sigma	The population standard deviation.
n	The sample size. Not required if power is specified.
power	The desired power. Not required if n is specified.
alpha	Probability of type I error.
effect	Effect size.
test	One of two choices: "two.tail" or "one.tail".
strict	Causes the function to use a strict interpretation of power in a two-sided test. If strict = TRUE then power for a two sided test will include the probability of rejection in the opposite tail of the true effect. If strict = FALSE (the default) power will be half the value of $\alpha$ if the true effect size is zero.

**Value**

Returns a list

sigma	The prescribed population variance.
n	The sample size.
power	The power.
alpha	The type I error probability.
test	The type of test prescribed.
effect	The effect size.

**Author(s)**

Ken Aho

**References**

Bain, L. J., and M. Engelhardt (1992) *Introduction to Probability and Mathematical Statistics*. Duxbury press. Belmont, CA, USA.

**See Also**

[pnorm](#)

**Examples**

```
power.z.test(sigma=6, effect=5, power=.9, test="one.tail")
```

---

press

*prediction sum of squares*

---

**Description**

Calculates PREdiction Sum of Squares (*PRESS*) for a linear model.

**Usage**

```
press(lm, as.R2 = FALSE)
```

**Arguments**

lm	An object of class <code>lm</code> .
as.R2	Logical. Whether or not output should be expressed as predicted $R^2$ , i.e., $PRESS/TSS$ .

**Details**

The press statistic is calculated as:

$$\sum_{i=1}^n d_i^2$$

where

$$d_i = \frac{e_i}{1 - h_{ii}}$$

where  $h_{ii}$  is the  $i$ th diagonal element in the hat matrix.

**Value**

Returns the *PRESS* statistic.

**Author(s)**

Ken Aho

**References**

Kutner, M. H., Nachtsheim, C. J., Neter, J., and W. Li (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.

**See Also**

[cor](#)

**Examples**

```
Y <- rnorm(100)
X <- rnorm(100)
press(lm(Y ~ X))
```

---

Preston.dist

*Preston diversity analysis*

---

**Description**

A diversity and richness analysis method based on the Preston (1948) log-normal distribution.

**Usage**

```
Preston.dist(counts, start = 0.2, cex.octave = 1, cex.legend = 1, cex.pt = 1, ...)
```

**Arguments**

counts	Vector of counts for species in a community dataset.
start	Starting value for non-linear least squares estimation of $a$ in $n = n_0 \times e^{-aR^2}$ .
cex.octave	Character expansion for octave labels.
cex.legend	Character expansion for legend.
cex.pt	Character expansion for symbols.
...	Additional arguments from <a href="#">plot</a> .

**Details**

Preston (1948) proposed that after a  $\log_2$  transformation species abundances, grouped in bins representing a doubling of abundance (octaves), would be normally distributed. Thus, after this transformation most species in a sample would have intermediate abundance, and there would be relatively few rare or ubiquitous species. The Preston model is based on the Gaussian function:  $n = n_0 \times e^{-aR^2}$ , where,  $n_0$  is the number of species contained in the modal octave,  $n$  is the number of species contained in an octave  $R$  octaves from the modal octave, and  $a$  is an unknown parameter. The parameter  $a$  is estimated using the function [nls](#), using a starting value, 0.2, recommended by Preston. The area under Preston curve provides an extrapolated estimate of richness and thus an indication of the adequacy of a sampling effort. Preston called a line placed at the 0th octave the veil line. He argued that species with abundances below the veil line have not been detected due to inadequate sampling.

**Value**

Graph of the Preston log-normal distribution for a dataset given by "counts", and a summary of the analysis including the fitted Gaussian equation, the estimated number of species, and an estimate for the percentage of sampling that was completed i.e.  $[\text{length}(\text{counts})/\text{Est.no.of.spp}]*100$ .

**Author(s)**

Ken Aho

**References**

Preston, F.W. (1948) The commonness and rarity of species. *Ecology* 29, 254-283.

**See Also**

[dnorm](#), [nls](#)

**Examples**

```
data(BCI.count)
BCI.ttl<-apply(BCI.count,2,sum)
Preston.dist(BCI.ttl)
```



---

prostate	<i>Prostate cancer data</i>
----------	-----------------------------

---

**Description**

Hastie et al. (2001) describe a cancer research study that attempted to associate prostate specific antigens and a number of prognostic measures in the context of advanced prostate cancer.

Data in the experiment were collected from 97 men who were about to undergo radical prostatectomies.

**Usage**

```
data(prostate)
```

**Format**

A data frame with 97 observations on the following 4 variables.

PSA Serum prostate-specific albumin level (mg/ml).

vol Tumor volume (cc).

weight Prostate weight (g).

Gleason Pathologically determined grade of disease. Summed scores were either 6, 7, or 8 with higher scores indicating worse prognosis.

**Source**

Kutner, M. H., Nachtsheim, C. J., Neter, J., and W. Li (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.

**References**

Hastie, T., R. Tibshirani, and J. Friedman (2009) *The Elements of Statistical Learning: Data Mining, Inference, and Prediction, Second Edition*. Springer.

---

prp	<i>Perpendicularity</i>
-----	-------------------------

---

**Description**

Calculates a perpendicularity index,  $\eta$ , for animal spatial movements. The index has a [0, 1] range with 0 indicating a perfectly parallel movement with respect to boundary or edge and 1 indicating perfectly perpendicular movement. Other summaries are also provided.

**Usage**

```
prp(Time, S.X, S.Y, N.X, N.Y, habitat = NULL, near.angle = NULL,  
F.0.NA = TRUE)
```

**Arguments**

Time	A numeric vector containing the times when spatial coordinates were recorded.
S.X	X-coordinates of animal.
S.Y	Y-coordinates of animal.
N.X	X-coordinate of nearest point on boundary. These data can be obtained from function <code>near.bound</code> or from ARCGIS Near output.
N.Y	Y-coordinate of nearest point on boundary. These data can be obtained from function <code>near.bound</code> or from ARCGIS Near output.
habitat	A character vector of habitat categories.
near.angle	A numeric vector containing the angle of azimuth to the nearest point on the boundary with respect to a four quadrant system. NE = $0^\circ$ to $90^\circ$ , NW is $> 90^\circ$ and $\leq 180^\circ$ , SE is $< 0^\circ$ and $\leq -90^\circ$ is $> -90^\circ$ and $\leq -180^\circ$ . This output can be obtained from function <code>bound.angle</code> or from ARCGIS Near output.
F.0.NA	A logical argument specifying whether or not a time interval in which $F = 0$ should be made NA (see Figure from examples)

**Details**

This index for perpendicularity,  $\eta$  is based on the following rules:

if  $\delta \leq 90^\circ$  then  $\eta = \delta/90^\circ$ ; if  $90^\circ < \delta \leq 135^\circ$  then  $\eta = [90^\circ - (\delta - 90^\circ)]/90^\circ$ ; if  $135^\circ < \delta \leq 180^\circ$  then  $\eta = (\delta - 90^\circ)/90^\circ$

For notation create Figures from examples.

**Value**

Returns a list with four or five items.

lines	A matrix with $n - 1$ rows containing line lengths for the lines <i>A</i> , <i>B</i> , <i>C</i> , <i>D</i> , and <i>F</i> . See figure in examples below.
angles	A matrix with $n - 1$ rows containing line lengths for the angles $\kappa$ , $\gamma$ and $\delta$ . See Figure in examples below.
moment.by.moment	This component provides a matrix with $n - 1$ rows. Included are the columns: End.time, Eta.Index, Delta, Habitat, and Brdr chng. The columns Habitat, and Brdr chng are excluded if habitat = NULL or near.angle = NULL.
P.summary	Contains averages and standard errors for $\eta$ .
crossing.summary	Crossing binomial summaries. Provided if habitat and near.angle are specified.

**Author(s)**

Ken Aho

## References

Kie, J.G., A.A. Ager, and R.T. Bowyer (2005) Landscape-level movements of North American elk (*Cervus elaphus*): effects of habitat patch structure and topography. *Landscape Ecology* 20:289-300.

McGarigal K., SA Cushman, M.C. Neel, and E. Ene (2002) *FRAGSTATS: Spatial Pattern Analysis Program for Categorical Maps*. Computer software program produced by the authors at the University of Massachusetts, Amherst.

## See Also

[near.bound](#), [bound.angle](#)

## Examples

```
## Not run:
###Diagram describing prp output.
y<-rnorm(100,0,5)
plot(seq(1,100),sort(y),type="l",xaxt="n",yaxt="n",lwd=2,xlab="",ylab="")
op <- par(font=3)

segments(52,-12,46,sort(y)[46],lty=1,col=1,lwd=1)##A
segments(90,-8,85,sort(y)[85],lty=1,col=1,lwd=1)##B
segments(46,sort(y)[46],85,sort(y)[85],lty=1)##F
segments(90,-8,46,sort(y)[46],lty=2)##D
arrows(52,-12,90,-8,length=.1,lwd=3)##C
arrows(20,-12,20,8,lty=2,col="gray",length=.1)#North
arrows(20,sort(y)[46],95,sort(y)[46],length=.1,lty=2,col="gray")
arrows(20,-12,95,-12,length=.1,lty=2,col="gray")#East

text(20,9,"N",col="gray");text(97,-12,"E",col="gray");text(97,sort(y)[46],"E",
col="gray")
text(49.5,-12.5,"a");text(92.5,-8.5,"b")
text(45.5,-5.5,"A",font=4,col=1);text(70,-9,"C",font=4,col=1);text(91.5,-1.75,"B",
font=4,col=1)
text(44,sort(y)[46]+1,"c");text(67.5,-2.5,"D",font=4,col=1);text(65,3.9,"F",font=4,
col=1)
text(87,sort(y)[87]+1,"d");text(57,-10,expression(kappa),col=1);
text(81,sort(y)[87]-3,expression(gamma),col=1);text(57,1.3,expression(theta),col=1)
text(64,-11.5,expression(beta),col=1)

library(plotrix)
draw.arc(50,-12,6,1.35,col=1);draw.arc(50,-12,6,.3,col=1);draw.arc(50,-12,6,0.02,
col=1)
draw.arc(46,sort(y)[46],7,.01,col=1);draw.arc(46,sort(y)[46],7,.5,col="white")
draw.arc(85,sort(y)[85],6,-2.7,col=1);draw.arc(85,sort(y)[85],6,-1.4,col="white",
lwd=2)
legend("topleft",c(expression(paste(kappa," = acos[(",C^2," + ",X^2," - ",D^2,")
/2CX]")),
expression(paste(gamma," = acos[(",Y^2," + ",F^2," - ",D^2,")/2YF]")),
expression(paste(theta," = atan[(",y[f]," - ",y[n],")/((",x[f]," - ",x[n],")])),
expression(paste(beta," = atan[(",y[epsilon]," - ",y[alpha],")/((",x[epsilon],
```

```

" - ",x[alpha,")"])),
bty="n",cex=.9,inset=-.025)

###Figure for demo dataset.
bX<-seq(0,49)/46

bY<-c(4.89000,4.88200,4.87400,4.87300,4.88000,4.87900,4.87900,4.90100,4.90800,
4.91000,4.93300,4.94000,4.91100,4.90000,4.91700,4.93000,4.93500,4.93700,
4.93300,4.94500,4.95900,4.95400,4.95100,4.95800,4.95810,4.95811,4.95810,
4.96100,4.96200,4.96300,4.96500,4.96500,4.96600,4.96700,4.96540,4.96400,
4.97600,4.97900,4.98000,4.98000,4.98100,4.97900,4.98000,4.97800,4.97600,
4.97700,4.97400,4.97300,4.97100,4.97000)

X<-c(0.004166667,0.108333333,0.316666667,0.525000000,0.483333333,0.608333333,
0.662500000,0.683333333,0.900000000,1.070833333)
Y<-c(4.67,4.25,4.26,4.50,4.90,4.10,4.70,4.40,4.20,4.30)

plot(bX,bY,type="l",lwd=2,xlab="",ylab="",ylim=c(4,5.1))
lines(X,Y)

for(i in 1:9)arrows(X[i],Y[i],X[i+1],Y[i+1],length=.1,lwd=1,angle=20)
mx<-rep(1,9)
my<-rep(1,9)
for(i in 1:9)mx[i]<-mean(c(X[i],X[i+1]))
for(i in 1:9)my[i]<-mean(c(Y[i],Y[i+1]))
for(i in 1:9)text(mx[i],my[i],i,font=2,cex=1.3)

nn<-near.bound(X,Y,bX,bY)
prp(seq(1,10),X,Y,nn[,1],nn[,2])$moment.by.moment
par(op)

## End(Not run)

```

---

pseudo.v

*Jackknife pseudo-values*

---

## Description

The function returns jackknife pseudovalues which can then be used to create statistical summaries, e.g. the jackknife parameter estimate, and the jackknife standard error. The function can be run on univariate data (`matrix = FALSE`) or multivariate data (`matrix = TRUE`). In the later case matrix rows are treated as multivariate observations.

## Usage

```
pseudo.v(data, statistic, order = 1, matrix = FALSE)
```

**Arguments**

data	A vector ( <code>matrix = FALSE</code> ) or matrix ( <code>matrix = TRUE</code> ) of quantitative data.
statistic	A function whose output is a statistic (e.g. a sample mean). The function must have only one argument, a call to <code>data</code> .
order	The order of jackknifing to be used.
matrix	A logical statement. If <code>matrix = TRUE</code> then rows in the matrix are sampled as multivariate observations.

**Details**

In the first order jackknife procedure a statistic  $\hat{\theta}$  is calculated using all  $n$  samples, it is then calculated with the first observation removed  $\hat{\theta}_{-1}$ , with only the second observation removed,  $\hat{\theta}_{-2}$ , and so on. This process is repeated for all  $n$  samples. The resulting vector of size  $n$  contains pseudovalues for their respective observations.

**Value**

A vector of first-order jackknife pseudovalues is returned.

**Author(s)**

Ken Aho

**References**

Manly, B. F. J. (1997) *Randomization and Monte Carlo Methods in Biology*, 2nd edition. Chapman and Hall, London.

**See Also**

[empinf](#), [boot](#), [bootstrap](#)

**Examples**

```
data(cliff.sp)
siteCD1<-data.frame(t(cliff.sp[1,]))

#Shannon-Weiner diversity
SW<-function(data){
d<-data[data!=0]
p<-d/sum(d)
-1*sum(p*log(p))
}

pv<-pseudo.v(siteCD1,SW)
```

qq.Plot

*Normal quantile plots for single or multiple factor levels***Description**

Provides quantile plots for one or more factor levels overlaid on a single graph. If `plot.CI = TRUE`, then code for bootstrapped confidence provided in the documentation for `boot` is applied to create confidence envelopes. If `plot.CI = FALSE`, `qqnorm` and `qqline` are used to create overlaid normal probability plots given multiple categories in `x`.

**Usage**

```
qq.Plot(y, x = NULL, col = NULL, pch = NULL, main = "", R = 5000, fit.lty = 1,
env.lty = 2, conf = 0.95, type = "point", ylim = NULL, xlim = NULL, xlab = NULL,
ylab = NULL, plot.CI = FALSE, standby = TRUE, ...)
```

**Arguments**

<code>y</code>	The response variable
<code>x</code>	A categorical variable to subset <code>y</code>
<code>col</code>	A scalar or vector with length equivalent to the number of levels in <code>x</code> , describing colors of points and lines for levels in <code>x</code> .
<code>pch</code>	A scalar or vector with length equivalent to the number of levels in <code>x</code> , describing symbols for levels in <code>x</code> .
<code>main</code>	Main title.
<code>R</code>	Number of bootstrap samples for calculating confidence envelopes
<code>fit.lty</code>	Line type for fit line(s).
<code>env.lty</code>	Line type for fit line(s).
<code>conf</code>	Level of confidence in confidence envelopes.
<code>type</code>	Type of bootstrapped confidence envelope. One of "point" or "overall".
<code>xlim</code>	A two element vector defining the lower and upper <code>x</code> -axis limits .
<code>ylim</code>	A two element vector defining the lower and upper <code>y</code> -axis limits .
<code>xlab</code>	<code>X</code> -axis label.
<code>ylab</code>	<code>Y</code> -axis label.
<code>plot.CI</code>	Logical, specifying whether or not confidence ellipses should be plotted.
<code>standby</code>	Logical, specifying if observations should be standardized.
<code>...</code>	Other arguments from <code>plot</code> .

**Author(s)**

Ken Aho

**See Also**

[qqnorm](#), [qqline](#), [envelope](#), [boot](#)

**Examples**

```
y <- rnorm(50)
x <- c(rep(1, 25), rep(2, 25))
qq.Plot(y, x)
```

---

r.bw

*Biweight midvariance, and biweight midcorrelation.*

---

**Description**

Calculates biweight midvariance if one variable is given and biweight midvariances, midcovariance and midcorrelation if two variables are given. Biweight midcorrelation is a robust alternative to Pearson's  $r$ .

**Usage**

```
r.bw(X, Y=NULL)
```

**Arguments**

$X$                     A numeric vector  
 $Y$                     An optional second numeric variable.

**Details**

Biweight statistics are robust to violations of normality. Like the sample median the sample midvariance has a breakdown point of approximately 0.5. The triefficiency of the biweight midvariance was the highest for any of the 150 measures of scale compared by Lax (1985).

**Value**

Returns the biweight variance if one variable is given, and the biweight midvariances, midcovariance and midcorrelation if two variables are given.

**Author(s)**

Ken Aho

**References**

Lax, D. A. (1985) Robust estimators of scale: finite sample performance in long-tailed symmetric distributions. *Journal of the American Statistical Association*, 80 736-741.  
Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

**See Also**[cor](#), [r.pb](#)**Examples**

```
x<-rnorm(100)
y<-rnorm(100)
r.bw(x,y)
```

---

`r.dist`*Visualize the sampling distribution of Pearson's product moment correlation*

---

**Description**

Stumbling points for many methods of inference for the true correlation  $\rho$  and for independence are: 1) asymmetry, 2) explicit bounds on  $\rho$ , and 3) dependence on sample size, of the sampling distribution of  $r$ .

The functions here allow visualization of these characteristics. The algorithm used for the sampling distribution of  $r$  is based on the first two steps in an asymptotic series (see Kenney and Keeping 1951).

**Usage**

```
r.dist(rho, r, n)
see.r.dist.tck()
```

**Arguments**

<code>rho</code>	Population correlation
<code>r</code>	A numeric vector containing possible estimates of <i>rho</i> .
<code>n</code>	Sample size, an integer.

**Details**

All distributions are standardized to have an area of one.

**Author(s)**

Ken Aho

**References**

Kenney, J. F. and E. S. Keeping (1951) *Mathematics of Statistics, Pt. 2, 2nd ed.* Van Nostrand, Princeton, NJ.

Weisstein, E. W. (2012) Correlation Coefficient–Bivariate Normal Distribution. From MathWorld–A Wolfram Web Resource. <http://mathworld.wolfram.com/CorrelationCoefficientBivariateNormalDistribution.html>



**See Also**[cor](#)**Examples**

```
# dev.new(height=3.5)
op <- par(mfrow=c(1,2),mar=c(0,0,1.5,3), oma = c(5, 4.2, 0, 0))
vals <- r.dist(0.9, seq(-1, 1, .001), 5)
plot(seq(-1, 1, .001), vals, type = "l", ylab = "", xlab = "")
vals <- r.dist(0.5, seq(-1, 1, .001), 5)
lines(seq(-1, 1, .001), vals, lty = 2)
vals <- r.dist(0.0, seq(-1, 1, .001), 5)
lines(seq(-1, 1, .001), vals, lty = 3)
legend("topleft", lty = c(1, 2, 3), title = expression(paste(italic(n), " = 5")),
legend = c(expression(paste(rho, " = 0.9")),expression(paste(rho, " = 0.5")),
expression(paste(rho, " = 0"))),bty = "n")

vals <- r.dist(0.9, seq(-1, 1, .001), 30)
plot(seq(-1, 1, .001), vals, type = "l", xlab = "", ylab = "")
vals <- r.dist(0.5, seq(-1, 1, .001), 30)
lines(seq(-1, 1, .001), vals, lty = 2)
vals <- r.dist(0.0, seq(-1, 1, .001), 30)
lines(seq(-1, 1, .001), vals, lty = 3)
legend("topleft", lty = c(1, 2, 3), title = expression(paste(italic(n), " = 30")),
legend = c(expression(paste(rho, " = 0.9")),expression(paste(rho, " = 0.5")),
expression(paste(rho, " = 0"))), bty = "n")
mtext(side = 2, expression(paste(italic(f), "(" , italic(r), ")")), outer = TRUE, line = 3)
mtext(side = 1, expression(italic(r)), outer = TRUE, line = 3, at = .45)
par(op)
```

R.hat

*R hat MCMC convergence statistic***Description**

The degree of convergence of a random Markov Chain can be estimated using the Gelman-Rubin convergence statistic,  $\hat{R}$ , based on the stability of outcomes between and within  $m$  chains of the same length,  $n$ . Values close to one indicate convergence to the underlying distribution. Values greater than 1.1 indicate inadequate convergence.

**Usage**

```
R.hat(M, burn.in = 0.5)
```

**Arguments**

M	An $n \times m$ numeric matrix of Markov Chains.
burn.in	The proportion of each chains to be used as a burn in period. The default value, 0.5, means that only the latter half of the chains will be used in computing $\hat{R}$ .

**Details**

Gelman et al. (2003, pg. 296) provides insufficient details to reproduce this function. To get the real function see Gelman and Rubin (1992). The authors list one other change in their Statlab version of this function. They recommend multiplying  $\text{sqrt}(\text{postvar}/W)$  by  $\text{sqrt}((df + 3)/t(df + 1))$ . The original code and this function can produce estimates below 1.

**Author(s)**

Ken Aho and unknown StatLib author

**References**

Gelman, A. and D. B. Rubin (1992) *Inference from iterative simulation using multiple sequences (with discussion)*. *Statistical Science*, 7:457-511.

Gelman, A., Carlin, J. B., Stern, H. S., and D. B. Rubin (2003) *Bayesian Data Analysis, 2nd edition*. Chapman and Hall/CRC.

---

r.pb	<i>Percentage bend correlation</i>
------	------------------------------------

---

**Description**

The percentage bend correlation is a robust alternative to Pearson's product moment correlation.

**Usage**

```
r.pb(X, Y, beta = 0.2)
```

**Arguments**

X	A quantitative vector
Y	A second quantitative vector
beta	Bend criterion

**Details**

The percentage bend correlation belongs to class of correlation measures which protect against marginal distribution ( $X$  and  $Y$ ) outliers. In this way it is similar to Kendall's  $\tau$ , Spearman's  $\rho$ , and biweight midcovariance. A second class of robust correlation measures which take in to consideration the overall structure of the data ( $O$  estimators) are discussed by Wilcox (2005, pg. 389). A value for the bend criterion beta is required in the R.pb function; beta = 0.2 is recommended by Wilcox (2005).

**Value**

A dataframe with the correlation, test statistic and  $P$ -value for the null hypothesis of independence are returned.

**Author(s)**

Ken Aho

**References**

Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

**See Also**[corr, r.bw](#)**Examples**

```
x<-rnorm(100)
y<-rnorm(100)
r.pb(x,y)
```

---

Rabino\_CO2

*CSIRO d13C-CO2 data from Rubino et al., A revised 1000 year atmospheric 13C-CO2 record from Law Dome and South Pole, Antarctica*

---

**Description**

Rabino et al. (2013) provided: CSIRO  $\delta^{13}\text{C}$  and  $\text{CO}_2$  measures covering 1000 years.

**Usage**

```
data("Rabino_CO2")
```

**Format**

Sample.type A factor with levels firn and ice.

depth Depth of core (in meters).

effective.age Age of  $\text{CO}_2$  (in years AD).

d13C.CO2  $\delta^{13}\text{C}$  (per mille).

CO2  $\text{CO}_2$  level (in ppm).

uncertainty Uncertainty in measures (in ppm ( $\text{CO}_2$ ) or per mille ( $\delta^{13}\text{C}$ )).

**Source**

Rubino, M., Etheridge, D. M., Trudinger, C. M., Allison, C. E., Battle, M. O., Langenfelds, R. L., ... & Jenk, T. M. (2013). A revised 1000 year atmospheric  $\delta^{13}\text{C}$ - $\text{CO}_2$  record from Law Dome and South Pole, Antarctica. *Journal of Geophysical Research: Atmospheres*, 118(15), 8482-8499

**Examples**

```

data(Rabino_CO2)
data(Rabino_del13C)

op <- par(mar=c(5,4.5,1,4.5))
with(Rabino_del13C, plot(effective.age,
d13C.CO2, xlab = "Year", type='p',
col = 1, pch = 21, bg = 'red', ylab = ''))
axis(2, col = 'red', col.axis = 'red')
mtext(side = 2, expression(paste(delta, ' ', '
'^13,C (per mille)'), col = 'red',
line = 3, cex = 1.2)
par(new = TRUE)

with(Rabino_CO2, plot(effective.age,
CO2, type='p', col=1,pch = 21,
bg = 'blue', axes = FALSE, xlab = "", ylab = ""))
axis(4, col = 'blue', col.axis = 'blue')
mtext(side=4,expression(paste('Atmospheric ',
CO[2], ' (ppm)'),
line = 3, col = 'blue', cex = 1.2)
par(op)

```

---

rat

*Rat glycogen data from Sokal and Rohlf (2012)*


---

**Description**

This dataset from Sokal and Rohlf (2012) can be used to demonstrate pseudoreplication. Six rats were randomly given one of three treatments: "control", "compound 217", and "compound 217 + sugar". After a short period of time the rats were euthanized and the glycogen content of their livers was measured. Two glycogen measurements were made for three different preparations of each liver. Clearly the liver preparations and measurements on those preparations are nested in each rat, and are not independent.

**Usage**

```
data(rat)
```

**Format**

A data frame with 36 observations on the following 4 variables.

glycogen A numeric vector describing glycogen levels. Units are arbitrary.

diet Nutritional compound: 1 = "control", 2 = "compound 217", 3 = "compound 217 + sugar".

rat Rat animal number.

liver Liver preparation.

measure Measurement number.

**Source**

Sokal, R. R., and Rohlf, F. J. (2012) *Biometry, 4th edition*. W. H. Freeman and Co., New York.

---

 refinery

*Refinery CO dataset*


---

**Description**

In the early 1990s an oil refinery northeast of San Francisco agreed with local air quality regulators [the Bay Area Air Quality Management District (BAAQMD)] to reduce carbon monoxide emissions. Baselines for reductions were to be based on measurements of CO made by refinery personnel, and by independent measurements from BAAQMD scientists for the roughly the same time period

**Usage**

```
data(refinery)
```

**Format**

The dataframe contains three columns:

CO Carbon monoxide. Measured in ppm.

Source The source of measurements; either refinery or BAAQMD.

Date Month/Day/Year

---

 rinvchisq

*Random draws from a scaled inverse chi-square distribution*


---

**Description**

The distribution is an important component of Bayesian normal hierarchical models with uniform priors.

**Usage**

```
rinvchisq(n, df, scale = 1/df)
```

**Arguments**

n	The number of random draws.
df	Degrees of freedom parameter.
scale	Scale non-centrality parameter.

**Details**

Code based on a function with same name in package **goeR**.

**See Also**

The function is a wrapper for [rchisq](#).

---

rmvm

*A multivariate normal dataset for data mining*

---

**Description**

Contains a  $Y$  variable constrained to be a random function of fifteen  $X$  variables, which, in turn, are generated from a multivariate normal distribution with no correlation between dimensions.

**Usage**

```
data("rmvm")
```

**Format**

A data frame with 500 observations on the following 16 variables.

$Y$  A response vector defined to be:  $Y = X_1 + X_2 + X_3 + X_4 + X_5 + X_6 + X_7 + X_8 + X_9 + X_{10} + X_{11} + X_{12} + X_{13} + X_{14} + X_{15} + \epsilon$  where  $\epsilon \sim N(0, 1)$ .

$X_1$  A random predictor

$X_2$  A random predictor

$X_3$  A random predictor

$X_4$  A random predictor

$X_5$  A random predictor

$X_6$  A random predictor

$X_7$  A random predictor

$X_8$  A random predictor

$X_9$  A random predictor

$X_{10}$  A random predictor

$X_{11}$  A random predictor

$X_{12}$  A random predictor

$X_{13}$  A random predictor

$X_{14}$  A random predictor

$X_{15}$  A random predictor

## Details

Data used by Derryberry et al. (in review) to consider high dimensional model selection applications.

## References

Derryberry, D., Aho, K., Peterson, T., Edwards, J. (In review). Finding the "best" second order regression model in a polynomial number of steps. *American Statistician*.

## Examples

```
## Code used to create data
## Not run:
sigma <- matrix(nrow = 15, ncol = 15, 0)
diag(sigma) = 1
mvn <- rmvnorm(n=500, mean=rnorm(15), sigma=sigma)
Y <- mvn[,1] + mvn[,2] + mvn[,3] + mvn[,4] + mvn[,4] + mvn[,5] + mvn[,6] + mvn[,7] +
mvn[,8] + mvn[,9] + mvn[,10] + mvn[,11] + mvn[,12] + mvn[,13] + mvn[,14] + mvn[,15] + rnorm(500)
rmvm <- data.frame(cbind(Y, mvn))
names(rmvm) <- c("Y", paste("X", 1:15, sep = ""))

## End(Not run)
```

---

samp.dist

*Animated and/or snapshot representations of a statistic's sampling distribution*

---

## Description

This help page describes a series of **asbio** functions for depicting sampling distributions. The function `samp.dist` samples from a parent distribution without replacement with sample size = `s.size`, `R` times. At each iteration a statistic requested in `stat` is calculated. Thus a distribution of `R` statistic estimates is created. The function `samp.dist` shows this distribution as an animated `anim = TRUE` or non-animated `anim = FALSE` density histogram. Sampling distributions for up to four different statistics utilizing two different parent distributions are possible using `samp.dist`. Sampling distributions can be combined in various ways by specifying a function in `func` (see below). The function `samp.dist.n` was designed to show (with animation) how sampling distributions vary with sample size, and is still under development. The function `samp.dist.snap` creates snapshots, i.e. simultaneous views of a sampling distribution at particular sample sizes. The function `dirty.dist` can be used to create contaminated parent distributions.

## Usage

```
samp.dist(parent = NULL, parent2 = NULL, biv.parent = NULL, s.size = 1, s.size2
= NULL, R = 1000, nbreaks = 50, stat = mean, stat2 = NULL, stat3 = NULL, stat4
= NULL, xlab = expression(bar(x)), func = NULL, show.n = TRUE, show.SE = FALSE,
anim = TRUE, interval = 0.01, col.anim = "rainbow", digits = 3, ...)
```

```

samp.dist.snap(parent = NULL, parent2 = NULL, biv.parent = NULL, stat = mean,
stat2 = NULL, stat3 = NULL, stat4 = NULL, s.size = c(1, 3, 6, 10, 20, 50),
s.size2 = NULL, R = 1000, func = NULL, xlab = expression(bar(x)),
show.SE = TRUE, fits = NULL, show.fits = TRUE, xlim = NULL, ylim = NULL, ...)

samp.dist.method.tck()

samp.dist.tck(statc = "mean")

samp.dist.snap.tck1(statc = "mean")

samp.dist.snap.tck2(statc = "mean")

dirty.dist(s.size, parent = expression(rnorm(1)),
cont = expression(rnorm(1, mean = 10)), prop.cont = 0.1)

samp.dist.n(parent, R = 500, n.seq = seq(1, 30), stat = mean, xlab = expression(bar(x)),
nbreaks = 50, func = NULL, show.n = TRUE,
show.SE = FALSE, est.density = TRUE, col.density = 4, lwd.density = 2,
est.ylim = TRUE, ylim = NULL, anim = TRUE, interval = 0.5,
col.anim = NULL, digits = 3, ...)

```

## Arguments

parent	A vector or vector generating function, describing the parental distribution. Any collection of values can be used. When using random value generators for parental distributions, for CPU efficiency (and accuracy) one should use <code>parent = expression(rpdf(s.size, ...))</code> . Datasets exceeding 100000 observations are not recommended.
parent2	An optional second parental distribution (see <code>parent</code> above), useful for the construction of sampling distributions of test statistics. When using random value generators use <code>parent2 = expression(rpdf(s.size2, ...))</code> .
biv.parent	A bivariate (two column) distribution.
s.size	An integer defining sample size (or a vector of integers in the case of <code>samp.dist.snap</code> ) to be taken at each of <code>R</code> iterations from the parental distribution.
s.size2	An optional integer defining a second sample size if a second statistic is to be calculated. Again, this will be a vector of integers in the of <code>samp.dist.snap</code> .
R	The number of samples to be taken from parent distribution(s).
nbreaks	Number of breaks in the histogram.
stat	The statistic whose sampling distribution is to be represented. Will work for any summary statistic that only requires a call to data; e.g. <code>mean</code> , <code>var</code> , <code>median</code> , etc.
stat2	An optional second statistic. Useful for conceptualizing sampling distributions of test statistics. Calculated from sampling <code>parent2</code> .
stat3	An optional third statistic. The sampling distribution is created from the same sample data used for <code>stat</code> .



stat4	An optional fourth statistic. The sampling distribution is created from the same sample data used for stat2.
xlab	X-axis label.
func	An optional function used to manipulate a sampling distribution or to combine the sampling distributions of two or more statistics. The function must contain the following arguments (although they needn't all be used in the function): s.dist, s.dist2, s.size, and s.size2. When sampling from a single parent distribution use s.dist3 in the place of s.dist2. For an estimator involving two parent distributions and four statistics, six arguments will be required: s.dist, s.dist2, s.dist3, s.dist4, s.size, and s.size2, s.dist3, and as non-fixed arguments (see example below).
show.n	A logical command, TRUE indicates that sample size for parent will be displayed.
show.SE	A logical command, TRUE indicates that bootstrap standard error for the statistic will be displayed.
anim	A logical command indicating whether or not animation should be used.
interval	Animation speed. Decreasing interval increases speed.
col.anim	Color to be used in animation. Three changing color palettes: <a href="#">rainbow</a> , <a href="#">gray</a> , <a href="#">heat.colors</a> , or "fixed" color types can be used.
digits	The number of digits to be displayed in the bootstrap standard error.
fits	Fitted distributions for somp.dist.snap A function with two argument: s.size and s.size2
show.fits	Logical indicating whether or not fits should be shown (fits will not be shown if no fitting function is specified regardless of whether this is TRUE or FALSE
xlim	A two element numeric vector defining the upper and lower limits of the X-axis.
ylim	A two element numeric vector defining the upper and lower limits of the Y-axis.
statc	Presets for certain statistics. Currently one of "custom", "mean", "median", "trimmed mean", "Winsorized mean", "Huber estimator", "H-L estimator", "sd", "var", "IQR", "MAD", " $(n-1)S^2/\sigma^2$ ", "F*", "t* (1 sample)", "t* (2 sample)", "Pearson correlation" or "covariance".
cont	A distribution representing a source of contamination in the parent population. Used by function dirty.dist.
prop.cont	The proportion of the parent distribution that is contaminated by code.
n.seq	A range of sample sizes for somp.dist.n
est.density	A logical command for somp.dist.n. if TRUE then a density line is plotted over the histogram. Only used if fix.n = true.
col.density	The color of the density line for somp.dist.n. See est.density above.
lwd.density	The width of the density line for somp.dist.n. See est.density above.
est.ylim	Logical. If TRUE Y-axis limits are estimated logically for the animation in somp.dist.n. Consistent Y-axis limits make animations easier to visualize. Only used if fix.n = TRUE.
...	Additional arguments from <a href="#">plot.histogram</a> .

## Details

Sampling distributions of individual statistics can be created with `samp.dist`, or the function can be used in more sophisticated ways, e.g. to create sampling distributions of ratios of statistics, i.e.  $t^*$ ,  $F^*$  etc. (see examples below). To provide pedagogical clarity animation for figures is provided. To calculate bivariate statistics, specify the parent distribution with `biv.parent` and the statistic with `func` (see below).

Two general uses of the function `samp.dist` are possible. 1) One can demonstrate the accumulation of statistics for a single sample size using animation. This is useful because as more and more statistics are acquired the frequentist paradigm associated with sampling distributions becomes better represented (i.e the number of estimates is closer to infinity). This is elucidated by allowing the default `fix.n = TRUE`. Animation will be provided with the default `anim = TRUE`. Up to two parent distributions, up to two sample sizes, and up to four distinct statistics (i.e. four distinct sampling distributions, representing four distinct estimators) can be used. The arguments `stat` and `stat3` will be drawn from `parent`, while `stat3` and `stat4` will be drawn from `parent2`. These distributions can be manipulated and combined in an infinite number of ways with an auxiliary function called in the argument `func` (see examples below). This allows depiction of sampling distributions made up of multiple estimators, e.g. test statistics. 2) One can provide simultaneous snapshots of a sampling distribution at a particular sample size with the function `samp.dist.snap`.

Loading the package **tecltk** allows use of the functions `samp.dist.tck`, `samp.dist.method.tck`, `samp.dist.snap.tck1` and `samp.dist.snap.tck2`, which provide interactive GUIs that run `samp.dist`.

## Value

Returns a representation of a statistic's sampling distribution in the form of a histogram.

## Author(s)

Ken Aho

## Examples

```
## Not run:
##Central limit theorem
##Snapshots of four sample sizes.
samp.dist.snap(parent=expression(rexp(s.size)), s.size = c(1,5,10,50), R = 1000)

##sample mean animation
samp.dist(parent=expression(rexp(s.size)), col.anim="heat.colors", interval=.3)

##Distribution of t-statistics from a pooled variance t-test under valid and invalid assumptions
#valid
t.star<-function(s.dist1, s.dist2, s.dist3, s.dist4, s.size = 6, s.size2 =
s.size2){
MSE<-(((s.size - 1) * s.dist3) + ((s.size2 - 1) * s.dist4))/(s.size + s.size2-2)
func.res <- (s.dist1 - s.dist2)/(sqrt(MSE) * sqrt((1/s.size) + (1/s.size2)))
func.res}

samp.dist(parent = expression(rnorm(s.size)), parent2 =
expression(rnorm(s.size2)), s.size=6, s.size2 = 6, R=1000, stat = mean,
```

```

stat2 = mean, stat3 = var, stat4 = var, xlab = "t*", func = t.star)

curve(dt(x, 10), from = -6, to = 6, add = TRUE, lwd = 2)
legend("topleft", lwd = 2, col = 1, legend = "t(10)")

#invalid; same population means (null true) but different variances and other distributional
#characteristics.
samp.dist(parent = expression(runif(s.size, min = 0, max = 2)), parent2 =
expression(rexp(s.size2)), s.size=6, s.size2 = 6, R = 1000, stat = mean,
stat2 = mean, stat3 = var, stat4 = var, xlab = "t*", func = t.star)

curve(dt(x, 10),from = -6, to = 6,add = TRUE, lwd = 2)
legend("topleft", lwd = 2, col = 1, legend = "t(10)")

## Pearson's R
require(mvtnorm)
BVN <- function(s.size) rmvnorm(s.size, c(0, 0), sigma = matrix(ncol = 2,
nrow = 2, data = c(1, 0, 0, 1)))
samp.dist(biv.parent = expression(BVN(s.size)), s.size = 20, func = cor, xlab = "r")

#Interactive GUI, require package 'tcltk'
samp.dist.tck("S^2")
samp.dist.snap.tck1("Huber estimator")
samp.dist.snap.tck2("F*")

## End(Not run)

```

---

samp.dist.mech

*Animated representation of sampling distribution basics*


---

## Description

Mountain goats are randomly sampled 10 at a time and weighed [goat weights are normal  $N(90.5, 225)$ ], a mean weight is calculated from these measures and added to collection of mean weights in the form of a histogram.

## Usage

```
samp.dist.mech(rep, int = 0.05)
```

```
samp.dist.mech.tck()
```

## Arguments

rep	Number of samples. Should not greatly exceed 100.
int	The time interval for animation (in seconds). Smaller intervals speed up animation

**Note**

Nice goat image from <https://all-free-download.com/>

**Author(s)**

Ken Aho

---

savage

*Mammalian BMR and biomass data from Savage et al. (2004)*

---

**Description**

Compilation of mammalian BMR and biomass data from the large data sets used in the studies of Hart (1971), Heusner (1991), Lovegrove (2000, 2003) and White & Seymour (2003). Data compiled by Savage (2004).

**Usage**

```
data("savage")
```

**Format**

A data frame with 1006 observations on the following 9 variables.

Order Mammal order.

Family Mammal family.

Species Mammal genus and species.

Mass Biomass in grams.

BMR Basal metabolic rate in watts

AvgMass Average mass, given multiple reports for a particular species.

AvgBMR Average BMR, given multiple reports for a particular species.

References Authorities from whom data were obtained.

Notes Note concerning a repeated species name.

**Source**

Savage, 548 V.M., Gillooly, J.F., Woodruff, W.H., West, G.B., Allen, A.P., Enquist, B.J., Brown, J.H. (2004) The predominance of quarter-power scaling in biology. *Functional Ecology*, 18, 257-282.

## References

- Hart, J.S. (1971) *Rodents in Comparative Physiology of Thermoregulation*, Vol. II Mammals (ed. G.C. Whitrow), pp. 2-149. Academic Press, New York.
- Heusner, A.A. (1991) Size and power in mammals. *Journal of Experimental Biology* 160, 25-54.
- Lovegrove, B.G. (2000) The zoogeography of mammalian basal metabolic rate. *American Naturalist* 156, 201-219.
- Lovegrove, B.G. (2003) The influence of climate on the metabolic rate of small mammals: a slow-fast metabolic continuum. *Journal of Comparative Physiology B* 173, 87-112.
- White, C.R. and Seymour, R.S. (2003) Mammalian basal metabolic rate is proportional to 584 body mass  $2/3$ . *Proceedings of the National Academy of Sciences*, 100, 4046-4049.

---

sc.twin

*Matched pairs schizophrenia data*

---

## Description

Scientists have long been concerned with identifying physiological characteristics which result in a disposition for schizophrenia. Early studies suggested that the volume of particular brain regions of schizophrenic patients may differ from non-afflicted individuals. However these studies often contained confounding variables (e.g. socioeconomic status, genetics) which obscured brain volume/ schizophrenia relationships (Ramsey and Schafer 1997). To control for confounding variables Suddath et al. (1990) examined 15 pairs of monozygotic twins where one twin was schizophrenic and the other was not. Twins were located from an intensive search throughout the United States and Canada. The authors used magnetic resonance imaging to measure brain volume of particular regions in the twin's brains.

## Usage

```
data(sc.twin)
```

## Format

The dataframe has 2 columns:

unaffected Left hippocampus volumes for unaffected twins.

affected Left hippocampus volumes for affected twins.

---

`se.jack`*Jackknife standard error from a set of pseudovalues*

---

**Description**

Calculates the conventional jackknife standard error from a set of pseudovalues. The function `se.jack` provides Tukey's jackknife estimator. The function `se.jack` provides a measure associated with first order jackknife estimates of species richness (Heltsche and Forester 1983).

**Usage**

```
se.jack(x)
```

```
se.jack1(x)
```

**Arguments**

`x` A numeric vector of pseudovalues, for instance from function [pseudo.v](#).

**Author(s)**

Ken Aho

**References**

Heltsche, J. F., and N. E. Forrester (1983) Estimating species richness using the jackknife procedure. *Biometrics* 39: 1-12.

**See Also**

[pseudo.v](#)

**Examples**

```
trag <- c(59, 49, 75, 43, 94, 68, 77, 78, 63, 71, 31, 59, 53, 48, 65, 73, 50, 59, 50, 57)
p <- pseudo.v(trag, statistic = mean)
se.jack(p[,2])
```

---

`sedum.ts`*CO2 exchange time series data*

---

**Description**

Gurevitch et al. (1986) demonstrated time series analysis with data describing change in CO<sub>2</sub> concentration of airstreams passing over a *Sedum wrightii* test plant.

**Usage**

```
data(sedum.ts)
```

**Format**

A data frame with 24 observations on the following 3 variables.

`exchange` CO<sub>2</sub> exchange, measured as: [change in CO<sub>2</sub> concentration (g/mg)]/ plant fresh mass (g). Thus units are 1/mg. Positive values indicate net CO<sub>2</sub> uptake while negative values indicate net CO<sub>2</sub> output.

`time` A numeric vector indicating two hour intervals

`treatment` Dry = water withheld for several week, Wet = plant well watered.

**Source**

Gurevitch, J. and S. T. Chester, Jr (1986) Analysis of repeated measures experiments. *Ecology* 67(1): 251-255.

---

`see.accPrec.tck`*Interactive depiction of precision and accuracy*

---

**Description**

Slider GUI for examining the interaction of precision and accuracy.

**Usage**

```
see.accPrec.tck()
```

**Author(s)**

Ken Aho

see.ancova.tck

*Visualize ANCOVA mechanics*

---

**Description**

An interactive GUI to view ANCOVA mechanics. Exp. power tries to simulate explanatory power in the concomitant variable. It simply results in  $(1 - \text{Exp. power}) \times \text{Residual SE}$ .

**Usage**

```
see.ancova.tck()
```

**Author(s)**Ken Aho

---

see.anova.tck

*Interactive depiction of the ANOVA mechanism*

---

**Description**

Slider control of the means and (constant) variability of three factor level populations. An ANOVA is run based on a random sample of these populations.

**Usage**

```
see.anova.tck()
```

**Author(s)**Ken Aho

---

see.cor.range.tck

*Depict the effect of range on correlation*

---

**Description**

Function interactively depicts the effect of the data range on association measures.

**Usage**

```
see.cor.range.tck(sd = 0.5)
```



**Arguments**

sd Amount of noise added to linear association. Residuals around line pulled from a normal distribution centered at zero with this standard deviation.

**Author(s)**

Ken Aho

**References**

Based on a figure from [https://en.wikipedia.org/wiki/Correlation\\_and\\_dependence](https://en.wikipedia.org/wiki/Correlation_and_dependence)

---

see.exppower.tck      *Visualize exponential power functions*

---

**Description**

Visualize exponential power functions, including a Gaussian distribution.

**Usage**

see.exppower.tck()

**Details**

The normal distribution and Gaussian distribution are based on an exponential power function:

$$f(x) = \exp(-|x|^m)$$

Letting  $m = 2$  results in a Gaussian distribution. Standardizing this so that the area under the curve = 1 results in the standard normal distribution.

**Author(s)**

Ken Aho

**See Also**

[book.menu](#)

---

see.HW

*Visualize the Hardy Weinberg equilibrium*

---

### Description

Allows interactive depiction of the Hardy Weinberg equilibrium.

### Usage

see.HW(parg)  
see.HW.tck()

### Arguments

parg                    Proportion of the allele  $p$  in the population, i.e. a number between 0 and 1.

### Details

Solves and depicts the Hardy Weinberg equilibrium, i.e:

$$pp + 2pq + qq = 1$$

### Author(s)

Ken Aho

---

see.lma.tck

*ANOVA linear models*

---

### Description

Derives ANOVA linear model using matrix algebra

### Usage

see.lma.tck()

### Author(s)

Ken Aho

---

 see.lmr.tck

*Regression linear model derivation from linear algebra*


---

**Description**

Given Y and X matrices a regression linear model is demonstrated using matrix algebra.

**Usage**

```
see.lmr.tck()
pm1(Y, X, sz=1, showXY = TRUE)
```

**Arguments**

Y	Response variable
X	Explanatory variables
sz	Text expansion factor
showXY	Logical, indicating whether or not X and Y matrices should be shown.

**Details**

X requires a Y intercept variable  $X_0$  and at least one other variable.

**Author(s)**

Ken Aho

**See Also**

[lm](#)

---

 see.lmu.tck

*Unbalanced and balanced linear models*


---

**Description**

The default design is balanced, as a result Type I = Type II = Type III SS. A student can then delete one or more Y responses, and corresponding X responses to see create an unbalanced design. Now the types of SS will no longer be equal. Furthermore, the order that X1 and X2 are specified will now matter in the case of Type I SS, although it will not matter for type II and III SS.

**Usage**

```
see.lmu.tck()

pm(Y, X1, X2, X1X2, change.order = FALSE, delete = 0)
```

**Arguments**

Y	Response variable.
X1	First column in design matrix with effect coding.
X2	Second column in design matrix.
X1X2	An interaction column. The product of design matrix columns one and two
change.order	A logical command specifying whether or not the order of X1 and X2 should changed in the model specification.
delete	when delete != 0 an observation number to be deleted.

**Author(s)**

Ken Aho

**See Also**

[lm](#)

**Examples**

```
if(interactive()){  
  if(any(names(sessionInfo())$otherPkgs=="asbio")) vignette(package = "asbio", "typeISS_key")  
}
```

---

see.logic

*Interactive worksheet for logical and fallacious arguments*

---

**Description**

It is vital that scientists understand what logical and fallacious arguments are. This worksheet provides a pedagogical tool for considering logic.

**Usage**

```
see.logic()
```

**Author(s)**

Ken Aho

**References**

Salmon, W (1963) *Logic*. Prentice-Hall

**See Also**

[book.menu](#)

**Examples**

```
## Not run:  
see.logic()  
  
## End(Not run)
```

---

see.M

*Visualization of the M-estimation function*

---

**Description**

The function provides interactive visualization of robust  $M$  estimation of location.

**Usage**

```
see.M()
```

**Details**

The value  $c = 1.28$  gives 95 percent efficiency of the mean given normality. The sample median and mean can be considered special cases of  $M$ -estimators. The value  $c = 0$  provides the sample median, while the value,  $c = \infty$  gives the sample mean.

**Author(s)**

Ken Aho

**References**

Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

**See Also**

[huber.mu](#), [huber.NR](#)

---

`see.mixedII`*Depiction of the effect of random level selection on inferences concerning fixed effects*

---

**Description**

The levels for a fixed factor are shown in rows, while the columns are levels for a random factor. Thus, the table depicts a mixed model. Assume that the values in the table are population means. For instance, the true mean of random level R1 for the fixed level F1 is 1. Using information from all random factor levels, the null hypothesis for the fixed factor is true. That is,  $\mu_{F1} = \mu_{F2} = \mu_{F3}$ . However when we select a subset of random levels, this is obscured. In fact, for any subset of random factor levels it appears as if there is evidence against  $H_0$ , i.e. there appears to be variability among the fixed factor level means. Thus, to avoid inflation of type I error (rejection of a true null hypothesis) we must consider the interaction of the random and fixed factors when considering inference for the fixed factor level populations.

**Usage**`see.mixedII()`**Author(s)**

Ken Aho, thanks to Ernest Keeley

**References**

Maxwell, S. E., and H. D. Delaney (2003) *Designing Experiments and Analyzing Data: A Model Comparison Perspective, 2nd edition*. Routledge Academic.

---

`see.mnom.tck`*Interactive depiction of the multinomial distribution*

---

**Description**

tcltk GUI representation of the multinomial in a simple (binomial) context.

**Usage**`see.mnom.tck()`**Author(s)**

Ken Aho

---

`see.move`*Interactive visualization of least squares regression.*

---

**Description**

Scatterplot points can be moved with `see.move`, while points can be added and deleted with `see.adddel`. The function `see.move` is an appropriation from **tcltk** demos, with a few bells and whistles added.

**Usage**

```
see.move()  
see.adddel()
```

**Author(s)**

the R Development Core Team for `see.move`, Ken Aho for `see.adddel`.

---

`see.nlm`*Visualize important non-linear functions*

---

**Description**

A number of important equation forms require that their parameters be estimated using the non-linear least squares. Here are six.

**Usage**

```
see.nlm()
```

**Author(s)**

Ken Aho

**References**

Crawley, M. J. (2007) *The R Book*. Wiley.

---

`see.norm.tck`*Visualize pdfs*

---

**Description**

Interactive GUIs for visualizing how distributions change with changing values of pdf parameters, e.g.  $\mu$  and  $\sigma$ . The basic ideas here are lifted largely from a clever function from Greg Snow's package **TeachingDemos**. The functions `see.pdfdriver.tck` and `see.pdfdriver` are **tcltk** utility functions.

**Usage**

```
see.norm.tck()
see.normcdf.tck()
see.beta.tck()
see.betacdf.tck()
see.bin.tck()
see.bincdf.tck()
see.chi.tck()
see.chicdf.tck()
see.disc.unif.tck()
see.disc.unifcdf.tck()
see.exp.tck()
see.expcdf.tck()
see.F.tck()
see.Fcdf.tck()
see.gam.tck()
see.gamcdf.tck()
see.geo.tck()
see.geocdf.tck()
see.hyper.tck()
see.hypercdf.tck()
see.logis.tck()
see.logiscdf.tck()
see.nbin.tck()
see.nbincdf.tck()
see.lnorm.tck()
see.lnormcdf.tck()
see.pois.tck()
see.poiscdf.tck()
see.t.tck()
see.tcdf.tck()
see.unif.tck()
see.unifcdf.tck()
see.weib.tck()
see.weibcdf.tck()
see.pdfdriver.tck()
```



```
see.pdfdriver(pdf, show.cdf = TRUE)
```

### Arguments

pdf	Name of probability density function
show.cdf	Logical, indicating whether or not the cumulative distribution function should be shown.

### Author(s)

Ken Aho

### Examples

```
## Not run:
see.norm.tck()

## End(Not run)
```

---

```
see.power
```

*Interactive depiction of type I and type II error and power*

---

### Description

Provides an interactive pedagogical display of power.

### Usage

```
see.power(alpha = NULL, sigma = NULL, n = NULL, effect = NULL,
test = "lower", xlim = c(-3, 3), strict = FALSE)

see.power.tck()
```

### Arguments

alpha	Type I error.
sigma	Standard deviation of underlying population.
n	sample size
effect	Effect size
test	Type of test, one of c("lower", "upper", "two").
xlim	X-axis limits
strict	Causes the function to use a strict interpretation of power in a two-sided test. If <code>strict = TRUE</code> then power for a two sided test will include the probability of rejection in the opposite tail of the true effect. If <code>strict = FALSE</code> (the default) power will be half the value of $\alpha$ if the true effect size is zero.

**Details**

The function `see.power` provides an interactive display of power. The function `see.power.tck` provides a **tcltk** GUI to manipulate `see.power`

**Author(s)**

Ken Aho

---

`see.rEffect.tck`      *Visualize random effects model*

---

**Description**

An experiment to ascertain the effect of two randomly selected brands of soil fertilizer on wheat yield. In the upper figure two brands of fertilizer (1 and 2) are randomly chosen from a population of potential choices. The mean yields produced by the population of fertilizers  $E(Y|A_i)$  are normally distributed. That is, it is possible to select a factor level that will result in very small average yields, or one that will result in large average yields, but it is more likely that a chosen factor level will produce some intermediate average effect. We proceed with the experiment by assigning two experimental units (two wheat fields) to each fertilizer. We assume that the yield of fields is normally distributed for each fertilizer, and furthermore that the factor levels are homoscedastic. We weigh our evidence against the  $H_0$  of a non-zero population variance by estimating the variability among factor levels. The more that yield varies with respect to nutrient treatments the more evidence we will have against  $H_0$ .

**Usage**

`see.rEffect.tck()`

**Author(s)**

Ken Aho

---

`see.regression.tck`      *Demonstration of regression mechanics*

---

**Description**

Population and sample regression lines are interactively depicted. The same random observations generated by the true error distribution is used for both models.

**Usage**

`see.regression.tck()`

**Author(s)**

Ken Aho

---

`see.roc.tck`*Interactive depiction of ROC curves*

---

**Description**

Sliders allow users to change distinctness of dichotomous classes (success and failure). This will affect the ROC curve. One can also change the criteria defining what constitutes a success. While this will not change the ROC curve (which compares true positive and false negative rates at all possible success cutoff), it will change empirical rates of true positives, true negatives, false positives, and false negatives given the defined cutoff.

**Usage**`see.roc.tck()`**Author(s)**

Ken Aho, inspired by a graphical demo at <http://www.anaesthetist.com/mnm/stats/roc/Findex.htm>

---

`see.smooth.tck`*Interactive smoother demonstrations*

---

**Description**

LOWESS, kernel, and spline smoothers are depicted, using **tcltk** widgets.

**Usage**`see.smooth.tck()`**Author(s)**

Ken Aho, appropriated ideas from demo in library **tcltk**.

**See Also**

[loess](#), [ksmooth](#), [smooth.spline](#)

see.ttest.tck      *Visualize t-tests*

---

**Description**

Interactive GUI for demonstrating *t*-tests

**Usage**

see.ttest.tck()

**Author(s)**

Ken Aho

---

see.typeI\_II      *Interactive depiction of type I and II error*

---

**Description**

The function provides a **tcltk** driver illustrating type I, type II error, and power.

**Usage**

see.typeI\_II()

**Author(s)**

Ken Aho

**See Also**

[see.power,power.z.test](#)

---

selftest.se.tck1      *Interactive self-testing questions*

---

**Description**

These functions provide interactive multiple-choice questions.

**Usage**

selftest.se.tck1()

**Author(s)**

Ken Aho

---

 Semiconductor

*Split plot computer chip data from Littell et al. (2006)*


---

**Description**

Littell et al. (2006) use the data here to introduce analysis of split plot designs using mixed models. Twelve silicon wafers were randomly selected from a lot, and were randomly assigned to four different processing modes. Resistance on the chips was measured in four different positions (four different chips) on each wafer. Mode of processing and position of chips were fixed factors, while wafer was a random effect. The experimental units with respect to process are the wafers. The experimental units with respect to position are individual chips. Thus the wafer is the whole plot, whereas the positions (chips) are split plot units

**Usage**

```
data(Semiconductor)
```

**Format**

The dataframe contains four columns:

Resistance The response variable of interest. Measured in ohms.

Process The explanatory variable of interest. The type of process used to create the computer chips. A factor with 4 levels.

Wafer The whole plot containing four chips. There were four wafers tested, i.e. four levels, 1, 2, 3, 4.

Chip Position on the wafer. These are split plots within the whole plots. Four levels: 1, 2, 3, 4.

**Source**

Littell, R. C., Milliken, G. A., Stroup, W. W., Wolfinger, R. D., and O. Schabenberger (2006) *SAS for Mixed Models 2nd ed.* SAS press.

---

 SexDeterm

*Fern environmental sex determination data*


---

**Description**

Sex determination (male and female) data at ecologically relevant glucose, N, and P concentrations and stoichiometries, at both ambient and elevated levels of CO<sub>2</sub>. The term "ameristic" denotes gametophytes with only male gametangia, while the term "meristic" refers to gametophytes with female or female and male gametangia.

**Usage**

```
data("SexDeterm")
```

**Format**

A data frame with 156 observations on the following 11 variables.

`CO2.Level` a factor with levels Ambient Elevated CO2 levels

`Block` a numeric vector, the elevated CO2 experiment was completed in 2 blocks

`Glucose.Level` the number of C atoms relative to the number of P atoms, with 5 indicating the presence of 6 micromolar glucose and 0 indicating the absence of glucose in the growth media

`N.Level` the number of N atoms relative to the number of P atoms

`P.Level` the number of P atoms relative to the number of N atoms

`C.N.P` the ratio of C to N to P atoms, a factor with levels 1:1 1:2 1:3 1:4 16:1 16:2 16:3 16:4 32:1 32:2 32:3 32:4 48:1 48:2 48:3 48:4 5:1:1 5:1:2 5:1:3 5:1:4 5:16:1 5:16:2 5:16:3 5:16:4 5:32:1 5:32:2 5:32:3 5:32:4 5:48:1 5:48:2 5:48:3 5:48:4

`Total.Gametophyte.No.` the total number of gametophytes in each population

`No..of.Ameristic.Gametophytes` the number of ameristic (male) gametophytes in each gametophyte population

`No..of.Meristic.Gametophytes` the number of meristic (female and hermaphrodite) gametophytes in each gametophyte population

`Ameristic.Meristic.Ratio` the ratio of ameristic gametophytes to meristic gametophytes (sex ratio)

`Pct..Ameristic.Gametophytes` the percentage of ameristic gametophytes per total gametophyte population

**References**

Goodnoe, T. T., Hill, J. P., Aho, K. (2016) Effects of variation in carbon, nitrogen and phosphorous molarity and stoichiometry on sex determination in the fern *Ceratopteris richardii*. *Botany* 94(4): 249-259.

**Examples**

```
data(SexDeterm)
```

---

shad

*American gizzard shad data*

---

**Description**

Hollander and Wolfe (1999) describe young of year lengths at four sites for American gizzard shad, *Dorosoma cepedianum*, a fish of the herring family.

**Usage**

```
data(shad)
```

**Format**

A data frame with 40 observations on the following 2 variables.

length Fish length in cm

site a factor with levels I II III IV

**Source**

Hollander, M., and D. A. Wolfe (1999) *Nonparametric Statistical Methods*. New York: John Wiley & Sons.

---

 shade.norm

*Shading functions for interpretation of pdf probabilities.*


---

**Description**

Creates plots with lower, upper, two-tailed, and middle of the distribution shading for popular pdfs.

**Usage**

```
shade.norm(x = NULL, from = NULL, to = NULL, sigma = 1, mu = 0,
tail = "lower", show.p = TRUE, show.d = FALSE, show.dist = TRUE, digits = 5,
legend.cex = .9, shade.col="gray",...)
```

```
shade.t(x = NULL, from = NULL, to = NULL, nu = 3, tail = "lower",
show.p = TRUE, show.d = FALSE, show.dist = TRUE, digits = 5, legend.cex = .9,
shade.col="gray",...)
```

```
shade.F(x = NULL, from = NULL, to = NULL, nu1 = 1, nu2 = 5,
tail = "lower", show.p = TRUE, show.d = FALSE, show.dist = TRUE,
prob.to.each.tail = 0.025, digits = 5, legend.cex = .9, shade.col="gray",...)
```

```
shade.chi(x = NULL, from = NULL, to = NULL, nu = 1, tail = "lower",
show.p = TRUE, show.d = FALSE, show.dist = TRUE, prob.to.each.tail = 0.025,
digits = 5, legend.cex = .9, shade.col="gray",...)
```

```
shade.bin(x=NULL, from=NULL, to=NULL, n=1, p=0.5, tail="X=x", show.p=TRUE,
show.dist=TRUE, show.d=FALSE, legend.cex = .9, digits=5, ...)
```

```
shade.poi(x=NULL, from=NULL, to=NULL, lambda=5, tail="X=x", show.p=TRUE,
show.dist=TRUE, show.d=FALSE, legend.cex = .9, digits=5, ...)
```

```
shade.wei(x = NULL, from = NULL, to = NULL, theta = 1, beta = 1, tail = "lower",
show.p = TRUE, show.d = FALSE, show.dist = TRUE, prob.to.each.tail = 0.025,
digits = 5, legend.cex = 0.9, shade.col = "gray", ...)
```

**Arguments**

<code>x</code>	A quantile, i.e. $X = x$ , or if <code>tail = "two.custom"</code> in <code>shade.norm</code> , a two element vector specifying the upper bound of the lower tail and the lower bound of the upper tail.
<code>from</code>	To be used with <code>tail = "middle"</code> ; the value $a$ in $P(a < X < b)$ .
<code>to</code>	To be used with <code>tail = "middle"</code> ; the value $b$ in $P(a < X < b)$ .
<code>sigma</code>	Standard deviation for the normal distribution.
<code>mu</code>	Mean of the normal distribution.
<code>tail</code>	One of four possibilities: "lower" provides lower tail shading, "upper" provides upper tail shading, "two" provides two tail shading, and "middle" provide shading in the middle of the pdf, between "from" and "to". The additional option "two.custom" is allowed for <code>shade.norm</code> and <code>shade.t</code> . This allows calculation of asymmetric two tailed probabilities. It requires that the argument <code>x</code> is a two element vector with elements denoting the upper bound of the lower tail and the lower bound of the upper tail. For discrete pdfs (binomial and Poisson) the possibility " <code>x=x</code> " is also allowed, and will be equivalent to the density. Two tailed probability is not implemented for <code>shade.poi</code> .
<code>show.p</code>	Logical; indicating whether probabilities are to be shown.
<code>show.d</code>	Logical; indicating whether densities are to be shown.
<code>show.dist</code>	Logical; indicating whether parameters for the distribution are to be shown.
<code>nu</code>	Degrees of freedom.
<code>nu1</code>	Numerator degrees of freedom for the $F$ -distribution.
<code>nu2</code>	Denominator degrees of freedom for the $F$ -distribution.
<code>prob.to.each.tail</code>	Probability to be apportioned to each tail in the $F$ and Chi-square distributions if <code>tail = "two"</code> .
<code>digits</code>	Number of digits to be reported in probabilities and densities.
<code>n</code>	The number of trials for the binomial pdf.
<code>p</code>	The binomial probability of success.
<code>lambda</code>	The Poisson parameter (i.e. rate).
<code>legend.cex</code>	Character expansion for legends in plots.
<code>shade.col</code>	Color of probability shading.
<code>theta</code>	Pdf parameter.
<code>beta</code>	Pdf parameter.
<code>...</code>	Additional arguments to <code>plot</code> .

**Value**

Returns a plot with the requested pdf and probability shading.

**Note**

Lower-tailed chi-squared probabilities are not plotted correctly for  $df < 3$ .



**Author(s)**

Ken Aho

**Examples**

```

## Not run:
##normal
shade.norm(x=1.2,sigma=1,mu=0,tail="lower")
shade.norm(x=1.2,sigma=1,mu=0,tail="upper")
shade.norm(x=1.2,sigma=1,mu=0,tail="two")
shade.norm(from=-.4,to=0,sigma=1,mu=0,tail="middle")
shade.norm(from=0,to=0,sigma=1,mu=0,tail="middle")
shade.norm(x=c(-0.2, 2),sigma=1,mu=0,tail="two.custom")

##t
shade.t(x=-1,nu=5,tail="lower")
shade.t(x=-1,nu=5,tail="upper")
shade.t(x=-1,nu=5,tail="two")
shade.t(from=.5,to=.7,nu=5,tail="middle")

##F
shade.F(x=2,nu1=15,nu2=8,tail="lower")
shade.F(x=2,nu1=15,nu2=8,tail="upper")
shade.F(nu1=15,nu2=8,tail="two",prob.to.each.tail=0.025)
shade.F(from=.5,to=.7,nu1=15,nu2=10,tail="middle")

##Chi.sq
shade.chi(x=2,nu=5,tail="lower")
shade.chi(x=2,nu=5,tail="upper")
shade.chi(nu=7,tail="two",prob.to.each.tail=0.025)
shade.chi(from=.5,to=.7,nu=5,tail="middle")

##binomial
shade.bin(x=5,n=20,tail="X=x",show.d=TRUE)
shade.bin(x=5,n=20,tail="lower")
shade.bin(x=5,n=20,tail="two")
shade.bin(from=8,to=12,n=20,tail="middle")

##Poisson
shade.poi(x=5,lambda=6,tail="X=x",show.d=TRUE)
shade.poi(x=5,lambda=7,tail="lower")
shade.poi(x=5,lambda=8,tail="upper")
shade.poi(from=8,to=12,lambda=7,tail="middle")

## End(Not run)

```

**Description**

Provides **tcltk** GUIs to manage **asbio shade** functions.

**Usage**

shade.bin.tck()

shade.chi.tck()

shade.F.tck()

shade.norm.tck()

shade.poi.tck()

shade.t.tck()

**Author(s)**

Ken Aho

**See Also**

[shade](#)

---

simberloff

*Compilations of genus and species counts from Simberloff (1970)*

---

**Description**

A compilation of taxonomic (species and genus) counts for a wide array of organism groups for island and associated mainland locations. Taken from Simberloff (1970).

**Usage**

```
data("simberloff")
```

**Format**

A data frame with 204 observations on the following 12 variables.

Location Island and mainland location.

Designation A factor with levels Island Mainland.

Hypothesized.source Hypothesized mainland location for particular island location.

No.spp. The number of species

Obs.S.G Observed species/genus (S/G) ratio

E.S.G. Expected S/G ratio, based on random sampling from mainland pool of species.  
 prop. .obs. .cogeners The proportion of observed cogeners, only reported for bird species.  
 prop. .exp. .cogeners The proportion of expected cogeners based on random sampling from the associated mainland pool of species, only reported for bird species.  
 Authority Source of information for compilation.  
 Life.form A factor with levels Ants Land birds Passerine birds Vascular plants.  
 Notes.1 Notes from Simberloff (1970)  
 Notes.2 Additional notes from Simberloff (1970)

### Source

Simberloff, D. (1970) Taxonomic diversity of island biotas. *Evolution* 24, 23-47.

---

skew	<i>Sample skewness and kurtosis</i>
------	-------------------------------------

---

### Description

Functions for skewness and kurtosis.

### Usage

```
skew(x,method="unbiased")
```

```
kurt(x,method="unbiased")
```

### Arguments

x	A vector of quantitative data.
method	The type of method used for computation of skew and kurtosis. Two choices are possible for skewness: "moments" and "unbiased", and three choices are possible for kurtosis: "unbiased", "moments", and "excess".

### Details

Aside from centrality and variability we can describe distributions with respect to their shape. Two important shape descriptors are skewness and kurtosis. Skewness describes the relative density in the tails of a distribution while kurtosis describes the peakedness of a distribution. When quantified for a population skewness and kurtosis are denoted as  $\gamma_1$  and  $\gamma_2$  respectively. For a symmetric distribution skewness will equal zero; i.e.  $\gamma_1 = 0$ . A distribution with more density in its right-hand tail will have  $\gamma_1 > 0$ , while one with more density in its left-hand tail will have  $\gamma_1 < 0$ . These distributions are often referred to as positively-skewed and negatively-skewed respectively. If a distribution is normally peaked (mesokurtic) then  $\gamma_2 = 3$ . As a result the number three is generally subtracted from kurtosis estimates so that a normal distribution will have  $\gamma_2 = 0$ . Thus strongly peaked (leptokurtic) distributions will have  $\gamma_2 > 0$ , while flat-looking (platykurtic) distributions will have a kurtosis  $\gamma_2 < 0$ .

Several types of skewness and kurtosis estimation are possible.

For method of moments estimation let:

$$m_j = (1/n) \sum_i (X_i - \bar{X})^j,$$

then the method of moments skewness is:  $m_3/m_2^{3/2}$ , the method of moments kurtosis is:  $m_4/m_2^2$ , and the excess method of moments kurtosis is  $m_4/m_2^2 - 3$ .

These estimators are biased low, particularly given small sample sizes. A more complex estimator is required to account for this bias. This is provided by method = "unbiased" in skew and kurt.

### Value

Output will be the sample skewness or kurtosis.

### Author(s)

Ken Aho

### Examples

```
exp<-rexp(10000)
skew(exp)
kurt(exp)
```

---

SM.temp.moist

*Alpine soil temperature and moisture time series*

---

### Description

Soil temperature and water availability from Mt. Washburn in Yellowstone National Park. Data were taken at soil depth of 5cm from a late snowmelt site at UTM 4960736.977 544792.225 zone 12T NAD 83, elevation 3070m.

### Usage

```
data(SM.temp.moist)
```

### Format

A data frame with 30 observations on the following 4 variables.

year A numeric vector describing year.

day The "day of year", whereby Jan 1 = day 1 and Dec 32 = day 365 (366 for leap years).

Temp\_C Temperature in degrees Celsius.

Moisture Soil water availability sensor reading. A reading of 35 is approximately equal to -1.5 MPa.

**Source**

Aho, K. (2006) *Alpine Ecology and Subalpine Cliff Ecology in the Northern Rocky Mountains*. Doctoral dissertation, Montana State University, 458 pgs.

---

 snore

*Snoring and heart disease contingency data*


---

**Description**

Norton and Dunn (1985) compiled data from four family practice clinics in Toronto to quantify the association between snoring and heart disease for 2484 subjects.

**Usage**

```
data(snore)
```

**Format**

A data frame with 2484 observations on the following 3 variables.

snoring A factor with levels every.night nearly.ever.night never occasional

ord.snoring Agresti (21012) transformed the explanatory levels to ordinal values in his analysis of this data.

disease Presence/absence of heart disease

**Source**

Norton, P. G., and E. V. Dunn (1985) Snoring as a risk factor for disease: an epidemiological survey. *British Medical Journal* 291: 630-632.

---

 so2.us.cities

*SO2 data for 32 US cities with respect to 6 explanatory variables*


---

**Description**

Of concern for public health officials and biologists are models of air pollution as a function of environmental characteristics. Using a meta-analysis of government publications Sokal and Rolf (1995) compiled an interesting dataset which investigates air pollution (measured as annual mean SO<sub>2</sub> concentration per m<sup>3</sup>) as a function of six environmental variables for 32 cities in the United States. Whenever the data were available they are based on averages of three years 1969, 1970, and 1971.

**Usage**

```
data(so2.us.cities)
```

**Format**

The dataset contains 8 variables:

City US city.

Y Average annual SO<sub>2</sub> concentration per m<sup>3</sup>.

X1 Average annual temperature (degrees Celsius).

X2 Number of industrial companies with more than 20 employees.

X3 Population size (1970 census) in thousands.

X4 Average Annual average wind speed.

X5 Average Annual precipitation (cm).

X6 Average number of days with precipitation.

**Source**

Sokal, R. R., and F. J. Rohlf (2012) *Biometry, 4th ed.* Freeman.

---

stan.error	<i>Variance and standard error estimators for the sampling distribution of the sample mean</i>
------------	--

---

**Description**

Estimator for the variance for the sampling distribution of the sample mean, i.e.  $S^2/n$ , and the standard deviation of the sampling distribution, i.e.  $S/\sqrt{n}$ .

**Usage**

```
stan.error(x)
stan.error.sq(x)
```

**Arguments**

x A vector of quantitative data.

**Author(s)**

Ken Aho

**See Also**

[sd](#)

---

starkey

*DEM data from the Starkey experimental forest in NE Oregon*

---

### Description

UTM northing and easting data along with 18 other environmental variables describing the Starkey experimental forest.

### Usage

`data(starkey)`

---

suess

*del14C in the atmosphere from 1700-1950*

---

### Description

Six reservoir model prediction of the  $\delta^{14}\text{C}$  in the atmosphere from approximately 1700-1950 as provided by Bacastow and Keeling (1973).

### Usage

`data("suess")`

### Format

A data frame with 149 observations on the following 3 variables.

Year Year

de114C Levels of  $\delta^{14}\text{C}$

Source Sources used by Bacastow et al. (1973). lermanN = Northern Hemisphere measures from Lerman (1970), lermanS = Southern Hemisphere measures from Lerman (1970), suess = Northern Hemisphere measures from Suess (1955, 1965), stuiver = Northern Hemisphere measures from Stuiver (1963).

### Source

Bacastow, R., Keeling, C. D., Woodwell, G. M., & Pecan, E. V. (1973). Atmospheric carbon dioxide and radiocarbon in the natural carbon cycle. II. Changes from AD 1700 to 2070 as deduced from a geochemical model (No. CONF-720510-). Univ. of California, San Diego, La Jolla; Brookhaven National Lab., Upton, NY (USA).

## References

Secondary sources used by Bacastow et al. (1973):

Lerman, J. C., Mook, W. G., & Vogel, J. C. (1970). C14 in tree rings from different localities. In *Radiocarbon Variations and Absolute Chronology*. Proceedings, XII Nobel Symposium. New York: Wiley. p (pp. 275-301).

Stuiver, M. (1963). Yale natural radiocarbon measurements IX. *Radiocarbon*, 11, 545-658.

Suess, H. E. (1965). Secular variations of the cosmic-ray-produced carbon 14 in the atmosphere and their interpretations. *Journal of Geophysical Research*, 70(23), 5937-5952.

Suess, H. E. (1955). Radiocarbon concentration in modern wood. *Science*, 122(3166), 415-417.

## Examples

```
data(suess)
with(suess, plot(Year, del14C, col = Source, pch = as.numeric(Source)))
with(suess, legend("topright", legend = levels(Source), col = 1:4, pch = 1:4))
lines(lowess(suess$Year, suess$del14C, f = .25), lwd = 2)
```

---

trag

*Salsify height dataset*

---

## Description

Heights of salsify *Tragapogon dubius* at the Barton Road long term experimental site in Pocatello Idaho.

## Usage

```
data(trag)
```

## Format

A data frame with 20 observations on the following variable.

height *T. dubius* plant height in cm



---

transM	<i>Transition matrix analysis</i>
--------	-----------------------------------

---

### Description

Creates a plot showing expected numbers of individuals in specified age classes or life stages given survivorship probabilities from a transition matrix (cf. Caswell 2000). The function `anm.transM` provides an animated view of the population growth curves. The function `anm.TM.tck` provides a **tcltk** GUI to run `anm.TM.tck`.

### Usage

```
transM(A, init, inter = 100, stage.names = c("All grps", 1:(ncol(A))),
leg.room = 1.5, ...)
```

```
anm.transM(A, init, inter=100, stage.names =c("All grps", 1:(ncol(A))),
leg.room = 1.5, anim.interval=0.1,...)
```

```
anm.TM.tck()
```

### Arguments

A	Transition matrix containing survivorship probabilities and fecundities see Caswell (2000).
init	A numeric vector containing initial numbers in each age class of interest.
inter	Number of time intervals for which population numbers are to be calculated.
stage.names	A character vector giving life stage names.
leg.room	A Y-axis multiplier intended to create room for a legend.
anim.interval	Speed of animation in frames per second.
...	Additional arguments for <code>plot</code>

### Value

Returns a plot and proportions of the population in each age class for the number of time intervals in `inter`.

### Author(s)

Ken Aho

### References

Caswell, H (2000) *Matrix Population Models: Construction, Analysis and Interpretation, 2nd Edition*. Sinauer Associates, Sunderland, Massachusetts.

Gurevitch, J., Scheiner, S. M., and G. A. Fox (2006) *The Ecology of Plants*. Sinauer.

**Examples**

```
#Endangered cactus data data from Gurevitch et al. (2006)
A<-matrix(nrow=3,ncol=3,data=c(.672,0,.561,0.018,0.849,0,0,0.138,0.969),
byrow=TRUE)
init<-c(10,2,1)
transM(A,init,inter=100,stage.names=c("All","Sm. Juv. ","Lg. Juv. ","Adults"),
xlab="Years from present",ylab="n")
#animated version
## Not run:
anm.transM(A,init,inter=100,stage.names=c("All","Sm. Juv. ","Lg. Juv. ","Adults"),
xlab="Years from present",ylab="n")

## End(Not run)
```

---

trim.me

*Trim data*


---

**Description**

Trims observations above and below the central  $(1 - 2\lambda)$  part of an an ordered vector of data.

**Usage**

```
trim.me(Y, trim = 0.2)
```

**Arguments**

Y                    A vector of quantitative data.  
trim                Proportion (0-1) to be trimmed from each tail of an ordered version of Y.

**Value**

Returns a trimmed data vector.

**Author(s)**

Ken Aho

**Examples**

```
x<-c(2,1,4,5,6,2.4,7,2.2,.002,15,17,.001)
trim.me(x)
```

---

trim.ranef.test	<i>Robust test for random factors using trimmed means.</i>
-----------------	--

---

**Description**

Provides a robust hypothesis test for the null:  $Var(X) = 0$ , for a population of random factor levels.

**Usage**

```
trim.ranef.test(Y, X, tr = 0.2)
```

**Arguments**

Y	Vector of response data. A quantitative vector.
X	Vector of factor levels
tr	Amount of trimming. A number from 0-0.5.

**Details**

Robust analyses for random effect designs are particularly important since standard random effects models provide poor control over type I error when assumptions of normality and homoscedasticity are violated. Specifically, Wilcox (1994) showed that even with equal sample sizes, and moderately large samples, actual probability of type I error can exceed 0.3 if normality and homoscedasticity are violated.

**Value**

Returns a list with three components dataframe describing numerator and denominator degrees of freedom, the  $F$  test statistic and the  $p$ -value.

**Note**

code based on Wilcox (2005)

**Author(s)**

Ken Aho

**References**

Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

**Examples**

```
rye<-c(50,49.8,52.3,44.5,62.3,74.8,72.5,80.2,47.6,39.5,47.7,50.7)
nutrient<-factor(c(rep(1,4),rep(2,4),rep(3,4)))
trim.ranef.test(rye,nutrient,tr=.2)
```

---

`trim.test`*Robust one way trimmed means test.*

---

**Description**

A robust heteroscedastic procedure using trimmed means.

**Usage**

```
trim.test(Y, X, tr = 0.2)
```

**Arguments**

Y	A vector of responses. A quantitative vector
X	A vector of factor levels.
tr	The degree of trimming. A value from 0-0.5.

**Details**

The method utilized here is based on the simple idea of replacing means with trimmed means and standard error estimates, based on all the data, with the standard error of the trimmed mean (Wilcox 2005). The method has the additional benefit of being resistant to heteroscedasticity due to the use of the Welch method for calculating degrees of freedom. With no trimming the degrees of freedom reduce to those of the one way Welch procedure in [oneway.test](#).

**Value**

Returns a dataframe with numerator and denominator degrees of freedom, a test statistic, and a  $p$ -value based on the  $F$ -distribution.

**Note**

code based on Wilcox (2005)

**Author(s)**

Ken Aho

**References**

Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

**See Also**

[oneway.test](#)

**Examples**

```
rye<-c(50,49.8,52.3,44.5,62.3,74.8,72.5,80.2,47.6,39.5,47.7,50.7)
nutrient<-factor(c(rep(1,4),rep(2,4),rep(3,4)))
trim.test(rye,nutrient,tr=.2)
```

---

tukey.add.test	<i>Tukey's test of additivity.</i>
----------------	------------------------------------

---

**Description**

With an RBD we are testing the null hypothesis that there is no treatment effect in any block. As a result randomized block designs including RBDs, Latin Squares, and spherical repeated measures assume that there is no interaction effect between blocks and main factors (i.e. main effects and block are additive). We can test this assumption with the Tukey's test for additivity. We address the following hypotheses:

$H_0$ : Main effects and blocks are additive, versus  $H_A$ : Main effects and blocks are non-additive.

**Usage**

```
tukey.add.test(y, A, B)
```

**Arguments**

y	Response variable. Vector of quantitative data.
A	Main effects. Generally a vector of categorical data.
B	Blocking variable. A vector of categories (blocks).

**Details**

Tukey's test for additivity is best for detecting simple block x treatment interactions; for instance, when lines in an interaction plot cross. As a result interaction plots should be used for diagnosis of other types of interactions. A high probability of type II error results from the inability Tukey's additivity test to detect complex interactions (Kirk 1995). As a result a conservative value of should be used, i.e. 0.1 - 0.25.

**Value**

Returns a table with test results.

**Author(s)**

Original author unknown. Modified by K. Aho

**References**

Kutner, M. H., Nachtsheim, C. J., Neter, J., and W. Li. (2005) *Applied Linear Statistical Models, 5th edition*. McGraw-Hill, Boston.

Kirk, R. E. 1995. *Experimental Design*. Brooks/Cole. Pacific Grove, CA.

**Examples**

```
treatment<-as.factor(c(36,54,72,108,144,36,54,72,108,144,36,54,72,108,144))
block<-as.factor(c(rep(1,5),rep(2,5),rep(3,5)))
strength<-c(7.62,8.14,7.76,7.17,7.46,8,8.15,7.73,7.57,7.68, 7.93,7.87,7.74, 7.8,7.21)
tukey.add.test(strength,treatment,block)
```

---

 veneer

*Veneer data from Littell et al. (2002)*


---

**Description**

Four examples of each of five brands of a synthetic wool veneer material were subjected to a friction test and a measure of wear was determined for each experimental unit.

**Usage**

```
data(veneer)
```

**Format**

A data frame with 20 observations on the following 2 variables.

wear a numeric vector

brand a factor with levels ACME AJAX CHAMP TUFFY XTRA

**Source**

Littell, R. C., Stroup, W. W., and R. J. Freund (2002) *SAS for Linear Models*. John Wiley and Associates.

---

 Venn

*Venn probability diagrams for an event with two outcomes*


---

**Description**

The user specifies the probabilities of two outcomes, and if applicable, their intersection. A Venn diagram is returned. The universe, S, will generally not have unit area, but in many applications will be a good approximation. The area of the intersection will also be an approximation.

**Usage**

```
Venn(A, B, AandB = 0, labA = "A", labB = "B", cex.text = .95, ...)
```

```
Venn.tck()
```

**Arguments**

A	Probability of event A
B	Probability of event B
AandB	Probability of the intersection of A and B
labA	Label assigned to event A in the diagram
labB	Label assigned to event B in the diagram
cex.text	Character expansion for text.
...	Additional arguments from <code>plot</code>

**Value**

A Venn diagram is returned.

**Author(s)**

K. Aho

**References**

Bain, L. J., and M. Engelhardt (1992) *Introduction to Probability and Mathematical Statistics*. Duxbury press. Belmont, CA, USA.

**Examples**

```
Venn(A=.3,B=.2,AandB=.06)
```

---

vs

*Scandinavian site by species community matrix*


---

**Description**

Scandinavian, lichen, bryophyte, and vascular plant data from Vare et al. (1995).

**Usage**

```
data(vs)
```

**Format**

A data frame with 24 observations (sites) on 44 variables (species).

**Details**

Lifted from dataframe {varespec} in package **vegan**.

**Source**

The dataset {varespec} in package **vegan**

**References**

Vare, H., Ohtonen, R., and J. Oksanen (1995) Effects of reindeer grazing on understory vegetation in dry *Pinus sylvestris* forests. *Journal of Vegetation Science* 6: 523-530.

---

wash.rich

*Species richness and environmental variables from Mt Washburn*

---

**Description**

Aho and Weaver (2010) examined the effect of environmental characteristics on alpine vascular plant species richness on Mount Washburn (3124m) a volcanic peak in north-central Yellowstone National Park.

**Usage**

```
data(wash.rich)
```

**Format**

A data frame with 40 observations on the following 7 variables.

site Site identifier.

Y Species richness.

X1 Percent Kjeldahl (total) soil N.

X2 Slope in degrees.

X3 Aspect in degrees from true north.

X4 Percent cover of surface rock.

X5 Soil pH.

**Source**

Aho, K., and T. Weaver (2010) Ecology of alpine nodes: environments, communities, and ecosystem evolution (Mount Washburn; Yellowstone Natl. Park). *Arctic, Antarctic, and Alpine Research*. 40(2): 139-151.



---

webs

*Spider web length data*

---

### Description

Gosline et al. (1984) applied heat to strands of spider web to determine whether the structure underlying webs was rubber-like. Data are estimated from a scatterplot in Gosline et al..

### Usage

```
data(webs)
```

### Format

The dataframe contains 4 columns

**obs** Observation number.

**relative length** Relative strand strand length after heat application.

**temp.C** Temp in degrees Celsius.

**residuals** Residuals from the linear model `length~temp.C`.

### Source

Gosline, J. M., Denny, M. W. and Demont, M. E. (1984). Spider silk as rubber. *Nature* 309, 551-552.

---

wheat

*Agricultural randomized block design*

---

### Description

Allard (1966) sought to quantify variation in the yield in wheat grasses. Five wheat crosses were selected from a breeding program and were grown at four randomly selected locations where the wheat would be grown commercially. At each location crosses (families) were randomly assigned to particular sections of fields, i.e. at each location a one way randomized block design was conducted.

### Usage

```
data(wheat)
```

**Format**

The dataframe has four columns:

**yield** Refers to wheat yield.

**loc** Refers to randomly selected locations where wheat were grown commercially. A factor with four levels: 1, 2, 3, 4.

**block** Refers to the replicate block within location. A factor with four levels: 1, 2, 3, 4. Within each block five wheat crosses were randomly assigned and grown.

**cross** Refers to wheat crosses. A factor with five levels: 1, 2, 3, 4, 5.

**Source**

Littell, R. C., Milliken, G. A., Stroup, W. W., Wolfinger, R. D., and O. Schabenberger (2006) *SAS for Mixed Models 2nd ed.* SAS press.

---

whickham

*Whickham contingency table data for smokers and survivorship*

---

**Description**

Appleton et al. (1996) summarized a study from the Whickham district of England to quantify the association of smoking, age, and death. 1,314 women were interviewed in the early 1970s with respect to their smoking habits. Twenty years later the women were relocated and classified with respect to survival at the time of the follow up (yes or no), whether they smoked at the time of the original interview (yes or no), and age at the time of the original study (1 = 18-24, 2 = 35-64, 3 = >65).

**Usage**

`data(whickham)`

**Format**

A data frame with 12 observations on the following 4 variables.

`age` A factor with levels 1 2 3.

`survival` A factor with levels N Y.

`smoke` A factor with levels N Y.

`count` Cross-classification count.

**Source**

Appleton, D. R., French, J. M., Vanderpump, M. P. J. (1996) Ignoring a covariate: AN example of Simpson's paradox. *The American Statistician* 50(4): 340-341.

---

`wildebeest`*Wildebeest carcass categorical data*

---

**Description**

To test the "predation-sensitive food" hypothesis, which predicts that both food and predation limit prey populations, Sinclair and Arcese (1995) examined wildebeest (*Connochaetes taurinus*) carcasses in the Serengeti. The degree of malnutrition in animals was measured by marrow content since marrow will contain the last fat reserves in ungulates. Carcasses were cross-classified with respect to three categorical variables: sex (M, F), cause of death (predation, non-predation), and marrow type (SWF = Solid White Fatty, indicating healthy animals, OG = Opaque Gelatinous, indicating malnourishment, and TG = Translucent Gelatinous, the latter indicating severe malnourishment).

**Usage**

```
data(wildebeest)
```

**Format**

A data frame with 12 observations on the following 4 variables.

`marrow` A factor with levels OG SWF TG.

`sex` A factor with levels F M.

`predation` A factor with levels N P.

`count` Count in each cell

**Source**

Sinclair, A. R. E., and P. Arcese (1995) Population consequences of predation-sensitive foraging: the Serengeti wildebeest. *Ecology* 76(3): 882-891.

---

`win`*Winsorize data*

---

**Description**

Winsorizes the proportion of ordered data given by  $\lambda$  from each tail.

**Usage**

```
win(x, lambda = 0.2)
```

**Arguments**

x	A vector of data.
lambda	A proportion from 0-1 giving the amount of data to be Winsorized in each tail of an ordered dataset.

**Details**

In Winsorization we we replace responses that are not in the central  $1 - 2\lambda$  part of an ordered sample with the minimum and maximum responses of the central part of the sample.

**Value**

Returns Winsorized data.

**Author(s)**

Ken Aho

**References**

Wilcox, R. R. (2005) *Introduction to Robust Estimation and Hypothesis Testing, Second Edition*. Elsevier, Burlington, MA.

**Examples**

```
x<-c(2,1,4,5,6,2.4,7,2.2,.002,15,17,.001)
win(x)
```

---

wine

*White wine quality data for data mining*

---

**Description**

These data concern white variants of the Portuguese "Vinho Verde" wine. Quality is an ordinal variable based on the median assessment of of at least 3 wine experts. Each expert graded wine quality between 0 (very bad) and 10 (excellent).

**Usage**

```
data("wine")
```

**Format**

A data frame with 4898 observations on the following 12 variables.

Y Wine quality.

X1 Volatile acidity.

X2 Citric acid content.

X3 Residual Sugar content.

X4 Chloride content.

X5 Free sulfur dioxide content.

X6 Total sulfur dioxide content.

X7 Density.

X8 pH:  $-\log_{10} [H^+]$ .

X9 Sulphate content.

X10 Alcohol content.

X11 Fixed acidity.

**Source**

Paulo Cortez (Univ. Minho), Antonio Cerdeira, Fernando Almeida, Telmo Matos and Jose Reis (CVRVV) @ 2009

**References**

Past Usage:

P. Cortez, A. Cerdeira, F. Almeida, T. Matos, Reis, J.(2009). Modeling wine preferences by data mining from physicochemical properties. *Decision Support Systems* 47(4):547-553.

---

world.co2

*World CO2 levels, by country, from 1980 to 2006*

---

**Description**

The Carbon Dioxide Information Analysis Center (CDIAC) has compiled extensive data, detailing total carbon dioxide emissions from the consumption and flaring of fossil fuels (in millions of metric tons of carbon dioxide). Data can be broken down by country. More up-to-date data can be found in this package at [world.emissions](http://world.emissions).

**Usage**

```
data(world.co2)
```

**Format**

The dataframe contains 16 columns

Year The year of CO<sub>2</sub> measure (1980-2006).

Afghanistan CO<sub>2</sub> emissions in Afghanistan from 1980-2006 (1x10<sup>6</sup> metric tons).

Belgium CO<sub>2</sub> emissions in Belgium...

Brazil CO<sub>2</sub> emissions in Brazil...

Canada CO<sub>2</sub> emissions in Canada...

China CO<sub>2</sub> emissions in China...

Finland CO<sub>2</sub> emissions in Finland...

Ghana CO<sub>2</sub> emissions in Ghana...

Italy CO<sub>2</sub> emissions in Italy...

Japan CO<sub>2</sub> emissions in Japan...

Kenya CO<sub>2</sub> emissions in Kenya...

Mexico CO<sub>2</sub> emissions in Mexico...

Saudi.Arabia CO<sub>2</sub> emissions in Saudi Arabia...

United.Arab.Emirates CO<sub>2</sub> emissions in the United Arab Emirates..

United.States CO<sub>2</sub> emissions in United States...

World.Total CO<sub>2</sub> emissions totals for the world...

**Source**

The U.S. Carbon Dioxide Information Analysis Center (CDIAC).

---

world.emissions

*Greenhouse gas emissions from Our World in Data*

---

**Description**

A subset of the complete CO<sub>2</sub> and Greenhouse Gas Emissions dataset maintained by Our World in Data (<https://ourworldindata.org/>) through 2019. The data follow a format of 1 row per “country” per year.

**Usage**

```
data("world.emissions")
```

**Format**

A data frame with 23708 observations on the following 15 variables.

`iso_code` Three-letter summary code for countries (ISO 3166-1 alpha-3).

`country` A character vector identifying country.

`year` Year data were collected, 1750-2019

`co2` Annual production-based emissions of carbon dioxide (CO<sub>2</sub>), measured in million tonnes. This is based on territorial emissions, which do not account for emissions from traded goods.

`coal_co2` Annual production-based emissions of CO<sub>2</sub> from coal, measured in million tonnes.

`flaring_co2` Annual production-based emissions of CO<sub>2</sub> from flaring, measured in million tonnes.

`gas_co2` Annual production-based emissions of CO<sub>2</sub> from gas, measured in million tonnes.

`oil_co2` Annual production-based emissions of CO<sub>2</sub> from oil, measured in million tonnes.

`other_industry_co2` Annual production-based emissions of CO<sub>2</sub> from other industry sources, measured in million tonnes. Based on territorial emissions,.

`total_ghg` Total greenhouse gas emissions, including land use change and forestry, measured in million tonnes of CO<sub>2</sub>-equivalents.

`methane` Total methane emissions, measured in million tonnes of CO<sub>2</sub>-equivalents.

`nitrous_oxide` Total nitrous oxide emissions, measured in million tonnes of CO<sub>2</sub>-equivalents.

`primary_energy_consumption` Primary energy consumption, measured in terawatt-hours per year.

`population` Population by country, available from 1800 to 2021 based on Gapminder data, HYDE, and UN Population Division (2019) estimates.

`gdp` Gross domestic product measured in international-\$ using 2011 prices to adjust for price changes over time (inflation) and price differences between countries. Calculated by multiplying GDP per capita with population.

`continent` Continent. Caribbean countries are distinguished from other North American countries. Additionally a level called "Redundant" is included to parse redundant entries in the country column, e.g., the "countries" Libya and Africa contain redundant information.

**Details**

Thanks to BIOL 6651 students at ISU who annotated these data: Laurel Faurot, Sawyer Finley, Spencer Roop, Therese Balkenbush, Lauren Tucker, Jessica Call and Riley Lanfear.

**Source**

<https://github.com/owid/co2-data>

**References**

According to Our World in Data (<https://ourworldindata.org/>), CO<sub>2</sub> data are sourced from the Global Carbon Project (<https://www.globalcarbonproject.org>) which releases updates of CO<sub>2</sub> emissions data annually. Greenhouse gas emissions (including methane, and nitrous oxide) are sourced from the CAIT Climate Data Explorer (<https://www.climatewatchdata.org:443/?source=cait>), and downloaded from the Climate Watch Portal (<https://www.climatewatchdata>).

org. Energy consumption data this data are sourced from a combination of two sources The Statistical Review of World Energy <https://www.bp.com/en/global/corporate/energy-economics/statistical-review-of-world-energy.html> and World Bank Development Indicators <https://databank.worldbank.org/source/world-development-indicators>. Although The Statistical Review of World Energy is published annually, it does not provide data for all countries. For countries absent from this dataset, we calculated primary energy by multiplying the World Bank, World Development Indicators metric Energy use per capita by total population figures. The World Bank sources its metric from the International Energy Agency (IEA). Other variables were collected from a variety of sources including the United Nations, Gapminder, and the Maddison Project Database.

### Examples

```
data(world.emissions)
```

---

world.pop	<i>Population levels in various countries from 1980-2006</i>
-----------	--

---

### Description

Population levels of 13 countries from 1980-2006. Population numbers are rounded to the nearest 100,000. More up-to-date data can be found in this package at [world.emissions](#)

### Usage

```
data(world.pop)
```

### Format

The dataframe contains 14 columns

Year The year of population measurements (1980-2006)

Afghanistan Population in Afghanistan from 1980-2006, rounded to the nearest 100,000.

Brazil Population in Brazil...

Canada Population in Canada...

China Population in China...

Finland Population in Finland...

Italy Population in Italy...

Japan Population in Japan...

Kenya Population in Kenya...

Mexico Population in Mexico...

Saudi.Arabia Population in Saudi Arabia...

United.Arab.Emirates Population in the United Arab Emirates...

United.States Population in United States...

World.Total Population totals for the world...



**Source**

US census bureau: <https://www.census.gov/programs-surveys/international-programs/about/idb.html>

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